## Memorization Track for Calculus 1A / 1B [Alt. Semester]

## Discussion of the Role of Memorization in Calculus I

Students often ask (usually just before a test), "What do I need to memorize?" The underlying assumption is that mathematics can be mastered, in large part, through memorization. You might assume that if you memorize all the formulas just before the test, you will be an A student. But success in mathematics requires a combination of **knowing the facts/formulas** <u>AND</u> being able to **recognize key patterns and structures** <u>AND</u> **understanding/insight**. If you eliminate any one of these, your results will be substantially diminished.

Solving problems in mathematics requires recognition of their structures and how various mathematical methods can be applied. Thus, developing the ability to **recognize patterns and structures**, is one of the most important skills in mathematics. Exposure to numerous problems and putting in many hours of practice is the key to building up both your ability to recognize these patterns/structures and building your understanding/insight. With these key elements in place, and having common formulas and identities (the required tools) **both understood and memorized**, ensures that you can solve problems quickly and confidently.

So, in parallel with teaching the concepts and methods of Calculus, we require that students develop a mental library of the key facts and relationships needed to efficiently solve typical problems. The sooner this mental library is established the better. The schedule outlined here is the <u>minimum</u> schedule that students must follow. <u>Lawyer's caveat</u>: Nothing in this summary exempts you from any requirement to learn and develop skills related to any material taught in class or more rudimentary knowledge not specifically listed.

Note that developing a solid understanding of key concepts can reduce (but not eliminate) the need for memorization. For example, should you memorize the value of  $\csc(5\pi/3)$  or should you become skilled at rapidly deriving the value (e.g., via a sketch of the unit circle)? It is your choice, but make sure you can come up with the value of any of the six trigonometric functions for any of the 16 standard angles. Similarly, should you memorize the formulas for  $\cos(2x)$  and  $\sin(2x)$ , or do you just memorize the formulas for  $\cos(x \pm y)$  and  $\sin(x \pm y)$ , and then set y = x? It is up to you. Do you memorize the identities involving  $\tan(x)$  and  $\sec(x)$  or  $\cot(x)$  and  $\csc(x)$ , or do learn how to derive them from  $\sin^2(x) + \cos^2(x) = 1$ ? Again, it is up to you. Just make sure you can rapidly access all of the relationships listed by the dates required. Quizzes and tests will presume you have acquired this knowledge once each date is passed.

Note that this list takes many items for granted. For example, the multiplication tables are not listed nor are many basic relationships of elementary geometry. **The list is selective and is not exhaustive**. It should be considered a good "minimum tool kit" focused on the most useful items encountered in Calculus I (which become the basis for Calculus II) and nothing more. You should enlarge this minimum knowledge base as you practice solving problems.

So **memorize these items (or learn how to quickly derive them)** to make sure that you can access them quickly when needed, but also do as many problems as possible to build your ability to recognize the underlying **patterns and structures** of problems and to build your **understanding/insight**.

Your success depends on all three.

## Memorization Track ("Off Semester" Schedule 2012/13)

(Note: Any content taught in class, whether presented before or after these dates, is IN ADDITION to this list)

Latart	Content to be Memorized on Able to be Derived	Defeneres
Date Date	(Note: Understanding will dramatically reduce the need for rote memorization)	References
Sept. 14 <sup>th</sup> (Note: All Calculus 1A	Definition of inverse functions and their relationship to their corresponding original function (including domains and ranges), definition/meaning of logarithms, plots of log functions for bases <1 or >1, laws of logarithms	Dugopolski Section 1.9 and 3.5 plus Hass 1.5 (especially the table in the middle of page 41)
Material	including change of base formula, value of log(1) or $\log_a(a^q)$ . Definition of	the initiale of page (1)
known by 3 <sup>rd</sup> class session)	inverse trig functions, plots for $\sin^{-1}(x)$ , $\cos^{-1}(x)$ , $\tan^{-1}(x)$ , and values of any trig function of any inverse trig function (i.e., What is $trig_1(trig_2^{-1}(a/b))$ ?)	
Sept. 21 <sup>st</sup>	<b>D</b> erivative formulas for logarithms and for $\sin^{-1}(x)$ , $\cos^{-1}(x)$ , $\tan^{-1}(x)$	See classroom handout for derivation method
Nov. 8 <sup>th</sup>	L'Hospital's Rule	Hass Sec 4.6, Thm 6
Nov. 14 <sup>th</sup>	The formula for Newton's Method and definitions of Hyperbolic functions	Hass page 292 & 221
Nov. 21 <sup>st</sup>	<b>Basic anti-derivatives including for</b> $\sin^{-1}(x)$ , $\cos^{-1}(x)$ , $\tan^{-1}(x)$ , $\ln(x)$ and meaning/conventions of sigma notation	Hass Appendix pg R-2 and page 325
<b>Dec.</b> 10 <sup>th</sup>	General meaning of the definite integral and its notation	Hass page 333
(Final Exam)		
Feb. 2 <sup>nd</sup>	Basic rules of algebra including all basic operations with fractions, common factoring forms (including $a^2 - b^2$ and $a^3 \pm b^3$ ). Basic properties of plain geometry, Pythagorean Formula, and formulas for the perimeter, area, and volumes of common geometric objects. Interval notation.	Basic Algebra Guide Sec. 1 & 2, Text iii, 1 <sup>st</sup> column of pg iv, top of pg vi, and Dugopolski Ch 1 top of pg 12.
Feb. 15 <sup>th</sup>	Properties and formulas for linear and quadratic equations including standard forms, y-intercept, x-intercept(s)/root(s), vertices, and plots. Also, meaning of roots/radicals, and laws of exponents.	Dugopolski pgs 36-42 and pgs 116-119, Basic Algebra Guide Sec 3&4.
Feb. 22 <sup>nd</sup>	Definition of radian measure, arc length formula ( $s = r\theta$ ), and formula for converting deg to/from radians ( $Deg/180 = Rad / \pi$ ). Six trigonometric functions: Definitions, plots, domains, ranges, roots, values at standard angles, and basic identities (See summary of basic identities below this table)	Text vii, identities summarized below, and Dugopolski pgs 209-212
Mar. 9 <sup>th</sup> (Exam I)	Exponential functions (base <1 and >1), value of $a^0$ , slope of $e^x$ at x=0, and properties of higher order polynomials (behavior at infinity, possible number and minimum number of real roots, potential shapes). Be able to sketch the exponentials and know the approximate value of $e^n$ for $n = 0, \pm 1, \pm 2, \pm 3$ from which you can derive $n = \pm 4, \pm 5, \pm 6,$	Plots top row pg xiii and plots on page xi. Your instructor will discuss general properties of higher order polynomials.
Mar. 30 <sup>th</sup>	Laws of limits, the limit definition of the derivative, and the Product and Quotient Rules	Table Hass page 65 and "General formulas" on page R-2 (back of book)
Apr. 13 <sup>th</sup>	Derivatives of trigonometric and exponential functions	Trig & Expon rules R-2
Apr. 27 <sup>th</sup>	Chain rule and its application in conjunction with the Product and Quotient	"Outside-Inside" Rule
(Exam II)	Rules for any algebraic combination of functions previously taught.	pg 10/ & 1nm 3 pg 166
May 13 <sup>th</sup> (Final Exam)	Implicit differentiation	Section 3.6

- Trigonometric identities:  $\sin^2(\theta) + \cos^2(\theta) = 1$ ,  $\tan^2(\theta) + 1 = \sec^2(\theta)$  and  $1 + \cot^2(\theta) = \csc^2(\theta)$ . Also, know the identities for  $\sin(x \pm y)$  and  $\cos(x \pm y)$  [implying formulas for  $\sin(2x)$  and  $\cos(2x)$ , and that  $\sin^2(x) = (1 - \cos(2x))/2$  and  $\cos^2(x) = (1 + \cos(2x))/2$ ].
- Triangle identities: Law of Sines and Law of Cosines (seeDugopolski Section 3.9)