

Homework IV

➤ **Section 14.3**

Integrate $\frac{z^2 - 4}{z^2 + 4}$ counterclockwise around the circle:

2) $|z-1|=2$

3) $|z+3i|=2$

Using Cauchy's integral formula (and showing the details), integrate counterclockwise (or as indicated)

6) $\oint_C \frac{e^{3z}}{3z-i} dz, C : |z|=1$

10) $\oint_C \frac{e^z}{z-2i} dz, C : |z-2i|=4$

12) $\oint_C \frac{\tan z}{z-i} dz, C$ the boundary of the triangle with vertices 0, $-1+2i$ and $1+2i$

➤ **Section 14.4**

Integrate counterclockwise around the circle $|z|=2$. (n is a positive integer). Show the details of your work.

2) $\frac{\sin z}{(z-i\pi/2)^4}$

4) $\frac{\cos z}{z^{2n+1}}$

Integrate around C . Show the details.

13) $\frac{e^{z/2}}{(z-a)^4}$, C the circle $|z-2-i|=3$ (CCW)