

**Coulomb's law**

$$F = k \frac{qQ}{r^2}$$

**Electric Field**

$$\vec{E} = \frac{\vec{F}}{q}$$

Field of a point charge

$$E = k \frac{Q}{r^2}$$

Electric field inside a capacitor

$$E = \frac{\eta}{\epsilon_0}$$

Principle of superposition

$$\vec{E}_{net} = \sum_{i=1}^N \vec{E}_i$$

Electric flux

$$\Phi_E = \int \vec{E} \cdot d\vec{A}$$

**Gauss's law**

$$\Phi = \oint \vec{E} \cdot d\vec{A} = \frac{Q_{in}}{\epsilon_0}$$

**Electric potential**

$$V = \frac{U}{q}$$

$$\Delta V = V_f - V_i = - \int_i^f \vec{E} \cdot d\vec{s}$$

For a point charge  $V(r) = \frac{1}{4\pi\epsilon_0} \frac{Q}{r}$ 

For a parallel-plate capacitor

$$V = Es$$

**Potential Energy**

$$U = qV$$

Two point charges

$$U = k \frac{qQ}{r}$$

**Capacitors**

$$C = \frac{Q}{\Delta V}$$

Parallel-plate  $C = \epsilon_0 \frac{A}{d}$ 

Capacitors connected in parallel

$$C_{eq} = C_1 + C_2 + \dots$$

Capacitors connected in series

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$$

Energy stored in a capacitor

$$U = \frac{Q^2}{2C}$$

**Ohm's law**

$$V = IR$$

$$I = \frac{dQ}{dt}$$

$$R = \rho \frac{l}{A}$$

$$\sum I_{in} = \sum I_{out}$$

$$\sum \Delta V_i = 0$$

**Power**

$$P = IV$$

**Resistors connected in series**

$$R_{eq} = R_1 + R_2 + R_3 + \dots$$

**Resistors connected in parallel**

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$$

**The potential difference across a charging capacitor in RC circuit**

$$V(t) = \epsilon(1 - e^{-t/RC})$$

**A magnetic field exerts a force**

$$d\vec{F} = I d\vec{l} \times \vec{B}$$

$$\vec{F} = I \vec{l} \times \vec{B}$$

$$\vec{F} = q\vec{v} \times \vec{B}$$

**The Biot-Savart Law**

$$\vec{B} = \frac{\mu_0 q \vec{v} \times \hat{r}}{4\pi r^2}$$

$$d\vec{B} = \frac{\mu_0 I d\vec{s} \times \hat{r}}{4\pi r^2}$$

**The magnetic field of:**

**A straight line wire**

$$B = \frac{\mu_0 I}{2\pi r}$$

**A solenoid**

$$B = \mu_0 n I$$

**Magnetic flux**

$$\Phi_B = \int \vec{B} \cdot d\vec{A}$$

**Inductance**

$$L = \frac{\Phi_B}{I}$$

$$L = \frac{\mu_0 N^2 A}{l}$$

$$\varepsilon = -L \frac{dI}{dt}$$

**Energy stored in an inductor**

$$U = L \frac{I^2}{2}$$

**“Discharged” LR circuit**

$$I = I_0 e^{-t/\tau}; \tau = L/R$$

**Maxwell’s equations**

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q}{\varepsilon_0}$$

$$\oint \vec{B} \cdot d\vec{A} = 0$$

$$\varepsilon = \oint \vec{E} \cdot d\vec{s} = -\frac{d\Phi_B}{dt}$$

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I + \mu_0 \varepsilon_0 \frac{d\Phi_E}{dt}$$

$$\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$$

**The Poynting vector**

$$\vec{S} = \frac{1}{\mu_0} (\vec{E} \times \vec{B})$$

$$E_0 = cB_0$$

**Malus’s Law**

$$I = I \cos^2 \theta$$

**Traveling Wave**

$$y(x, t) = A \sin(kx \pm \omega t + \varphi_0)$$

$$k = \frac{2\pi}{\lambda}; \omega = \frac{2\pi}{T};$$

$$v = \lambda f; v = \frac{\omega}{k}$$

**Interference**

$$\Delta\varphi = 2\pi \frac{\Delta r}{\lambda} + \Delta\varphi_0 = m2\pi \text{ (constr)}$$

$$\Delta\varphi = 2\pi \frac{\Delta r}{\lambda} + \Delta\varphi_0$$

$$= (m + \frac{1}{2})2\pi \text{ (destr)}$$

$$A = \left| 2a \cos\left(\frac{\Delta\varphi}{2}\right) \right|$$

**Standing Waves**

$$A(x) = 2a \sin(kx)$$

$$\lambda_m = \frac{2L}{m}; f_m = m \frac{v}{2L}$$

**Double Slit**

$$y_m = \frac{m\lambda L}{d}$$

**Diffraction grating**

$$d \sin \theta_m = m\lambda$$

$$y_m = L \tan \theta_m$$

**Thin-lens equation:**

$$\frac{1}{f} = \frac{1}{s} + \frac{1}{s'}$$

$$m = -\frac{s'}{s}; \quad |m| = \frac{h'}{h}$$

**Snell's Law:**

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\text{TIR: } \sin \theta_c = \frac{n_2}{n_1}$$

$$n = \frac{c}{v}$$

**Constants**

Charge of a proton/electron

$$e = \pm 1.60 \cdot 10^{-19} \text{ C}$$

Electron mass

$$m = 9.11 \cdot 10^{-31} \text{ kg}$$

Proton mass  $m = 1.67 \cdot 10^{-27} \text{ kg}$

Permittivity of free space

$$\epsilon_0 = 8.85 \cdot 10^{-12} \text{ C}^2/\text{Nm}^2$$

Permeability of free space

$$\mu_0 = 4\pi \cdot 10^{-7} \text{ Tm/A}$$

$$k = \frac{1}{4\pi\epsilon_0} = 8.99 \cdot 10^9 \text{ Nm}^2/\text{C}^2$$

$$c = \frac{1}{\sqrt{\epsilon_0\mu_0}} = 3.0 \cdot 10^8 \text{ m/s}$$

**Kinematic eq-ns with const. Acc.:**

$$v(t) = v_{0x} + at$$

$$x(t) = x_0 + v_{0x}t + (1/2)at^2$$

$$v^2 = v_{0x}^2 + 2a(x - x_0)$$

**Centripetal acceleration**

$$a_R = v^2/r$$

**Misc Formulas:**

Circumference of a circle =  $2\pi R$

Area of a circle =  $\pi R^2$

Surface area of a sphere =  $4\pi R^2$

Volume of sphere =  $(4/3)\pi R^3$

Volume of cylinder =  $\pi R^2 L$

**Right triangle:**

$$\sin \theta = a/c$$

$$\cos \theta = b/c$$

$$\tan \theta = a/b$$

$$c^2 = a^2 + b^2$$

