

Physics I. Formula Sheet

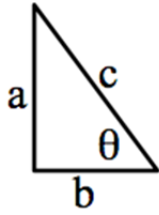
Right triangle:

$$\sin \theta = a/c$$

$$\cos \theta = b/c$$

$$\tan \theta = a/b$$

$$c^2 = a^2 + b^2$$



Quadratic Formula:

$Ax^2 + Bx + C = 0$ has solutions:

$$x = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$$

Misc Formulas:

Circumference of a circle = $2\pi R$

Area of a circle = πR^2

Surface Area of a Sphere = $4\pi R^2$

Volume of sphere = $(4/3)\pi R^3$

Volume of cylinder = $\pi R^2 L$

Differentiation:

$$dx^n/dx = nx^{n-1} \quad (n \neq 0)$$

$$d\cos(x)/dx = -\sin(x) \quad (x \text{ in radians})$$

$$d\sin(x)/dx = \cos(x) \quad (x \text{ in radians})$$

$$d(f(x) + g(x))/dx = df(x)/dx + dg(x)/dx$$

Integration:

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

1-D Motion:

displacement = Δx

$$v_{\text{average}}: \Delta x/\Delta t = (x_2 - x_1)/(t_2 - t_1)$$

$$a_{\text{average}}: \Delta v/\Delta t = (v_2 - v_1)/(t_2 - t_1)$$

Given $x(t)$

$$v(t) = dx/dt \quad (\text{instantaneous})$$

$$a(t) = dv/dt = d^2x/dt^2 \quad (\text{instantaneous})$$

1-D Motion with Const. Acc.:

$$x(t) = x_0 + v_{0x}t + (1/2)at^2$$

$$v(t) = v_0 + at$$

$$v^2 = v_0^2 + 2a(x - x_0)$$

Projectile Motion:

$$x(t) = x_0 + v_{0x}t$$

$$v_x(t) = v_{0x}$$

$$a_x(t) = 0$$

$$y(t) = y_0 + v_{0y}t + (1/2)a_y t^2$$

$$v_y(t) = v_{0y} + a_y t$$

$$a_y(t) = a_y$$

Acceleration due to gravity:

$$g = 9.8 \text{ m/s}^2 \text{ downward}$$

Equations connect. trans./rotat. motion

$$v_{\text{tan}} = R\omega$$

$$a_{\text{tan}} = R\alpha$$

Rotat. kinematic eq-ns with const. angular acceleration

$$\omega(t) = \omega_0 + \alpha t$$

$$\theta(t) = \theta_0 + \omega_0 t + (1/2)\alpha t^2$$

$$\omega^2 = \omega_0^2 + 2\alpha(\theta - \theta_0)$$

Centripetal acceleration:

$$a_r = v^2/R; \quad a_R = \omega^2 R$$

Newton 2nd law

$$\sum \vec{F} = m\vec{a}$$

Friction Forces:

$$F_S \leq \mu_s N$$

$$F_k = \mu_k N$$

Work and Kinetic Energy

$$W = \vec{F} \cdot \vec{s}$$

$$W = \int_{x_i}^{x_f} F_x dx$$

$$K = (1/2)mv^2$$

$$W_{\text{net}} = \Delta K$$

$$\Delta K = K_f - K_i$$

Potential Energy:

For gravity on earth's surface:

$$F = mg$$

$$U(y) = U_0 + mgy$$

For a spring:

$$F = -kx$$

$$U(x) = (1/2)kx^2$$

$$W = -\frac{k}{2}(x_f^2 - x_i^2)$$

With conservative forces only:

$$E_{\text{tot}} = K + U$$

$$E_f = E_i$$

With non-conservative forces:

$$E_f = E_i + W_{NC}$$

Power

$$P_{\text{avg}} = W/t$$

$$P = dW/dt$$

$$P = \vec{F} \cdot \vec{v}$$

$$\vec{a} \cdot \vec{b} = ab \cos \theta$$

$$\vec{a} \cdot \vec{b} = a_x b_x + a_y b_y + a_z b_z$$