Spring 2024

Quiz Solution

1. In this case, there are six possibilities:

 $(2W,2B),\ (2W,2R),\ (2W,2G),\ (2B,2R),\ (2B,2G),\ (2R,2G)$

So the desired probability is

$$\frac{\binom{4}{2}\binom{2}{2} + \binom{4}{2}\binom{6}{2} + \binom{4}{2}\binom{3}{2} + \binom{2}{2}\binom{6}{2} + \binom{2}{2}\binom{3}{2} + \binom{6}{2}\binom{3}{2}}{\binom{15}{4}}$$

2. Since

$$A = \{\text{sum of the throws equals } 4\} = \{(1,3), (2,2), (3,1)\}$$
$$B = \{\text{at least one of the throws show a } 3\}$$
$$= \{(1,3), (3,1), (2,3), (3,2), (3,3), (3,4), (4,3), (3,5), (5,3), (3,6), (6,3)\}$$

and

$$A \cap B = \{(1,3), (3,1)\}$$

we see that

$$P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{2/36}{11/36} = \frac{2}{11}$$