

4.33 a) Given total bandwidth  $B_{w_{tot}} = 30 \text{ MHz}$  (one-way)  
channel bandwidth  $B_w = 200 \text{ KHz}$

$$\Rightarrow \text{total radio channel } S = \frac{B_{w_{tot}}}{B_w} = \frac{30 \times 10^6}{200 \times 10^3} = \underline{\underline{150}}$$

b) number of users that can be served by a base station during fully loaded operation =  $8 \times 64 = \underline{\underline{512}}$

c) Given  $n=4$ ,  $\sigma = 8 \text{ dB}$ ,  $U(\gamma) = 0.9$ , from Figure 4.18, we have  $P_r(R) = 0.73$ , where  $\gamma = -90 \text{ dBm}$ .

$$P_r(R) = \text{Pr}[P_r(R) > \gamma] = Q\left[\frac{\gamma - \overline{P_r(R)}}{\sigma}\right] = 0.73$$

$$\Rightarrow \frac{\overline{P_r(R)} - \gamma}{\sigma} = 0.61 \Rightarrow \overline{P_r(R)} = 0.61\sigma + \gamma = 0.61 \times 8 + (-90) = -85.12 \text{ dBm}$$

$$\Rightarrow \overline{P_L(R)} = P_t \text{ (dBm)} - \overline{P_r(R)} \text{ (dBm)}$$

$$= 10 \log_{10}(20/10^{-3}) - (-85.12) = 128.13 \text{ dB}$$

Assume  $d_0 = 1 \text{ km}$ ,  $G_r = 0 \text{ dB} = 1$ , miscellaneous loss  $L = 0 \text{ dB} = 1$ , given  $G_t = 10 \text{ dB} = 10$ ,  $f_c = 1960 \text{ MHz}$  (corresponding to the largest  $\overline{P_L}(d_0)$ ), we have  $\lambda = \frac{c}{f_c} = 0.153 \text{ (m)}$

$$\Rightarrow \overline{P_L}(d_0) = -10 \log_{10} \left[ \frac{G_t \cdot G_r \cdot \lambda^2}{(4\pi)^2 \cdot d_0^2} \right] = -10 \log_{10} \left[ \frac{10 \times 1 \times (0.153)^2}{(4\pi)^2 \times (1000)^2} \right] = 88.3 \text{ dB}$$

Since  $\overline{P_L}(R) = \overline{P_L}(d_0) + 10 \cdot n \log_{10} \frac{R}{d_0}$ , for  $n=4$ , we have

$$R = 10^{\frac{\overline{P_L}(R) - \overline{P_L}(d_0)}{10n}} \cdot d_0$$

$$= 10^{\frac{128.13 - 88.3}{40}} \cdot 1 = 9.88 \text{ (Km)}$$

4.33 Cont'd

$$\Rightarrow N = \frac{\text{Total Area}}{2.6R^2} = \frac{2500}{2.6 \times 9.88^2} \approx \underline{\underline{10}}$$

(d) Let's first relate the channel number to it's frequency

	Channel Number	Center Frequency (MHz)
Reverse Channel	$1 \leq N \leq 150$	$0.2N + 1879.9$
Forward Channel	$1 \leq N \leq 150$	$0.2N + 1929.9$

We can see that the forward and reverse channel each pair are separated by 80 MHz.

Since the cluster size is equal to 4, we divide the 150 radio channel into  $4 \times 3 = 12$  subsets. The following chart illustrates these 12 subsets.

1A	2A	3A	4A	1B	2B	3B	4B	1C	2C	3C
1	2	3	4	5	6	7	8	9	10	11
13	14	15	16	17	18	19	20	21	22	23
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮
133	134	135	136	137	138	139	140	141	142	143
145	146	147	148	149	150					

It can be seen from the chart that each subset contains about 12 channels. In each subset, the closest adjacent channel is 12 channels away. In a four cell radio system, each cell uses channel chosen from the set  $iA + jB + kC$ , where  $i$  is an integer from 1 to 4. Each cell can use about 37 channels. The adjacent cells

4.33 Cont'd

g) Given Probability of Blocking = 5%

Number of user channels per cell:  $C = 38 \times 8 = 304$

Assume traffic intensity per user  $A_u = uH = 3 \times \frac{2}{60} = 0.1$  Erlangs

$\Rightarrow$  number of users that can be supported per cell at

$$\text{start-up} = U = A/C = 300/0.1 = \underline{\underline{3000}}$$

$\Rightarrow$  maximum number of subscribers that can be supported

$$\text{at start up } \text{User number} = U \cdot \text{Cell number} = 3000 \times 10 = \underline{\underline{3 \times 10^4}}$$

$$h) \text{ cost per user} = \frac{3.5 \times 10^7 \times 10\%}{3 \times 10^4} = \underline{\underline{\$116.67}}$$

$$5.1 \quad c = \lambda f \Rightarrow \lambda = \frac{c}{f} = \frac{3 \cdot 10^8 \text{ m/s}}{1.95 \cdot 10^9 \text{ Hz}} = 0.154 \text{ m}$$

$$f_d = \frac{v}{\lambda} \cos \theta \quad f_{d_{\max}} = \frac{v}{\lambda} ; -f_{d_{\max}} = -\frac{v}{\lambda}$$

$$v = 1 \text{ km/hr} \Rightarrow v = 0.278 \text{ m/s} \Rightarrow f_d = 1.8 \text{ Hz}$$

$$v = 5 \text{ km/hr} \Rightarrow v = 1.39 \text{ m/s} \Rightarrow f_d = 9.03 \text{ Hz}$$

$$v = 100 \text{ km/hr} \Rightarrow v = 27.8 \text{ m/s} \Rightarrow f_d = 180.5 \text{ Hz}$$

$$v = 1000 \text{ km/hr} \Rightarrow v = 278 \text{ m/s} \Rightarrow f_d = 1805 \text{ Hz}$$

$\therefore$  @ 1 km/hr, spectral edges are 1949.9999982 mHz  
and 1950.0000018 mHz

@ 5 km/hr, spectral edges are 1949.99999097 mHz  
and 1950.00000903 mHz

@ 100 km/hr, edges are 1949.9998195 mHz  
and 1950.0001805 mHz

@ 1000 km/hr, edges are 1949.998195 mHz  
1950.001805 mHz

5.7 (a)  $T_s = \frac{1}{100 \text{ kbps}} = 10^{-5} \text{ s}$ .

$0 \leq \sigma_r \leq 10^{-6} \text{ s}$

$\Rightarrow \sigma_r \leq \sigma_r$  if  $\sigma_r \leq \frac{1}{10} T_s \Rightarrow$  flat fading

$T_s \geq 10 \sigma_r \quad \sigma_r \leq \frac{T_s}{10}$

(b)  $f_d = \frac{v}{\lambda}$

$c = \lambda f$

$\lambda = c/f = 3 \cdot 10^8 / 5.8 \cdot 10^9 \approx \underline{0.05 \text{ m}}$

velocity =  $\frac{30 \text{ miles}}{\text{hr}} \cdot \frac{1 \text{ hr}}{3600 \text{ sec}} \cdot \frac{5280 \text{ '}}{1 \text{ mile}} \cdot \frac{12 \text{ '}}{1 \text{ '}} \cdot \frac{2.54 \text{ cm}}{1 \text{ '}} \cdot \frac{1 \text{ m}}{100 \text{ cm}}$   
 $= \frac{30 \cdot 5280 \cdot 12 \cdot 2.54}{3600 \cdot 100} = 13 \text{ m/s}$

$f_d = \frac{13}{0.05} = \underline{260 \text{ Hz}}$

5.7 Cont'd.

Coherence Time Define  $\left[ \begin{matrix} 90\% \\ 50\% \end{matrix} \right]$

$T_c \approx \frac{1}{f_m} = \underline{0.004 \text{ s}}$

$T_c \approx \frac{9}{10 \cdot f_m} = \frac{1}{5 f_m} = \underline{0.00125 \text{ s}}$

(c) Here we have  $f_d = 260 \text{ Hz}$ ;  $T_s \approx 10^{-5} \text{ s}$ ;  $T_c \approx 10^{-3} \text{ s}$

slow fading  $\Rightarrow T_s \ll T_c$  here  $10^{-5} \ll 10^{-3}$

slow fading

d) pick your  $T_c$ , then

# bits sent =  $R_b \cdot T_s = \frac{10^5 \text{ b}}{\text{s}} \cdot 10^{-3} \text{ s} \approx \underline{100}$