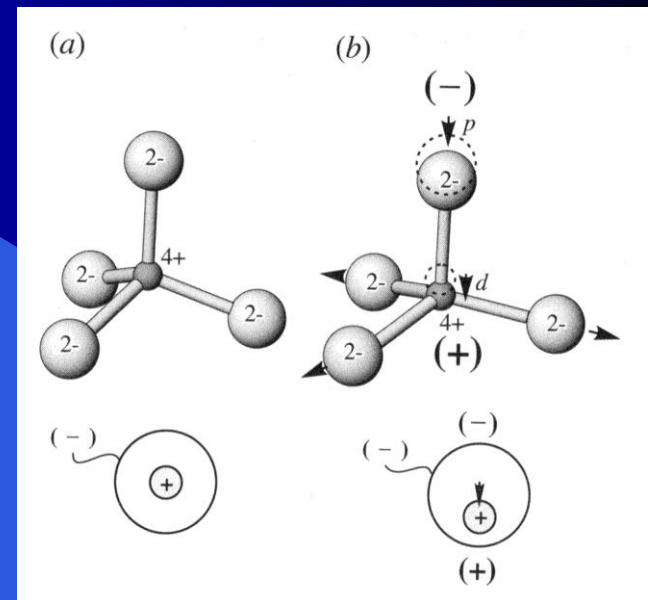


Earth Materials I – Piezoelectricity, Density, and Magnetic Susceptibility

Piezoelectricity

Figure 6.14 Piezoelectricity. (a) A silicon tetrahedron consists of a Si^{4+} centered within four O^{2-} . The positive charge is centered within the negative charge as is shown schematically with the two circles below. (b) If deformed by pressing downward at p , an O^{2-} and the Si^{4+} are moved downward distance d and the three O^{2-} on the base are spread outward. Because only one O^{2-} moves down, the center of the positive charge on the Si^{4+} is moved downward relative to the center of mass of the negative charge on the four O^{2-} . This charge displacement produces a voltage, that is positive on the bottom and negative on top.

The crystal CANNOT have a center of symmetry. Common piezoelectric minerals are quartz, topaz, and tourmaline



Density and Specific Gravity

The specific gravity ($G = \rho/\rho_{\text{H}_2\text{O}}$) of a mineral is a function of how tightly the ions/atoms are packed (the packing index) and the chemical composition. The packing index is

$$PI = \frac{V_I}{V_C} \times 100$$

where PI is the packing index, V_I = the total volume of the ions in the unit cell based on their ionic radii, and V_C = the volume of the unit cell.

Note that for Density and Specific Gravity have the same numerical value. However specific gravity is unitless. Density is reported either as g/cm^3 (cgs units) or kg/m^3 (SI units).

The specific gravity of a mineral can be determined by using a pycnometer



Magnetism in minerals

- A spinning electron produces a magnetic field (Bohr magnetic moment).
- Bohr magnetic moment can be cancelled if there are two electrons in an orbital.
- In order for a mineral to be magnetic it must have orbitals with unpaired electrons.
- The most important elements are the transition metals (Fe, Mn, Ti, and Cr) that have only partially filled 3d orbitals.
- The strength of the magnetic moment depends on the number of unpaired electrons.
- Fe^{3+} and Mn^{2+} have 5 unpaired 3d electrons and thus the largest magnetic moment.
- The nature of the magnetic behavior of a mineral that contains these transition metals depends on how the magnetic moments of the atoms/ions are oriented within the crystal structure.

Diamagnetism – all orbitals of the atoms/ions contain paired electrons. No magnetic behavior. When placed in a magnetic field diamagnetic minerals will be slightly repelled.

Magnetic behavior

- Paramagnetism – magnetic moments of constituent atoms/ions are not aligned. The net magnetic moment is zero. Applying a magnetic field leads to a slight alignment of the magnetic moments. Magnetic susceptibility is a measure of the strength of the magnetic moment. This depends on chemical composition and crystal structure.
- Ferromagnetism – magnetic moments of the constituent atoms/ions become aligned forming magnetic domains. Application of an external magnetic field leads to the alignment of the magnetic domains and permanent magnetism.
- Ferrimagnetism – there are some unpaired electrons that can form magnetic domains that can be aligned when placed in a magnetic field. Currie T and remnant magnetism.
- Antiferrimagnetism – minerals in which antiparallel spins completely cancel to yield zero net magnetic moments.

	Spin Configuration	μ_B	No External Field	In External Field	External Field Removed
(a) Diamagnetic	Quartz (SiO ₂)				
	Si ⁴⁺ (↑↓)(↑↓)(↑↓) 3p	0			
	2O ²⁻ (↑↓)(↑↓)(↑↓) 3p	0	Net = 0	Weak Repulsion	Net = 0
(b) Paramagnetic	Olivine (Fe ₂ SiO ₄)				
	2Fe ²⁺ (↑↓)(↑)(↑)(↑)(↑) 3d	+8			
	Si ⁴⁺ (↑↓)(↑↓)(↑↓) 3p 4O ²⁻ (↑↓)(↑↓)(↑↓) 2p	0	Net = 0	Weak Attraction	Net = 0
		8			
(c) Ferromagnetic	Iron (Fe)				
	Fe (↑↓)(↑↓)(↑↓)(↑)(↑) 3d	+2			
		2	Net = 0	Strong Attraction	Net Magnetization
(d) Ferrimagnetic	Magnetite				
	^{IV} Fe ²⁺ (↑↓)(↑)(↑)(↑)(↑)	+4			
	^{VI} Fe ³⁺ (↑)(↑)(↑)(↑)(↑)	+5			
	^{IV} Fe ³⁺ (↓)(↓)(↓)(↓)(↓)	-5			
4O ²⁻ (↑↓)(↑↓)(↑↓) 2p	0				
		4	Net = 0	Moderate Attraction	Net Magnetization
(e) Anti-ferromagnetic	Ilmenite (<-183C)				
	^{VI} Fe ²⁺ (↑↓)(↑)(↑)(↑)(↑)	+4			
	^{VI} Fe ²⁺ (↑↓)(↓)(↓)(↓)(↓)	-4			
	^{VI} 2Ti ⁴⁺ (↑↓)(↑↓)(↑↓)	0			
3p	0				
		0	Net = 0	Repelled	Net = 0

Figure 6.13 Magnetism. See text for discussion. (a) Diamagnetism in quartz. Neither Si⁴⁺ nor O²⁻ has unpaired electrons so neither has a Bohr magnetic moment μ_B . (b) Paramagnetism in olivine. The Fe²⁺ has a net Bohr magnetic moment, but in the absence of an external magnetic field, the orientations are random. (c) Ferromagnetism in native iron. Each iron atom has two unpaired electrons and a Bohr magnetic moment of 2. Domains within the mineral have uniform magnetic orientation. (d) Ferrimagnetism in magnetite. The ^{IV}Fe³⁺ and ^{VI}Fe³⁺ each has five unpaired electrons but with opposite spins so their net magnetic moments cancel. The ^{IV}Fe²⁺ has a net magnetic moment and causes the magnetite to have ferromagnetic properties. (e) Antiferromagnetism in ilmenite below -183°C. Fe²⁺ in adjacent sites has antiparallel spins. Net magnetic moments cancel. Antiferromagnetic materials are repelled by a magnet.

Magnetic Susceptibility

Magnetic susceptibility characterizes the ability of a substance to be magnetized when exposed to external magnetic field. In magnetically isotropic substances, it is defined as follows

$$M = k H,$$

where M represents the vector of the induced magnetization (in SI of units in A/m), H is the vector of the intensity of magnetic field (also in A/m) and k is the magnetic susceptibility (dimensionless scalar entity). In some substances, the susceptibility is constant, while in the others it is a complex function of the field intensity.

