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## Temperature dependent pressure induced lineshape of O<sub>3</sub> rotational transitions in air

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#### 9 Abstract

The pressure induced broadening of a series of pure rotational transitions of ozone have been measured as a function of temperature. Results of experiments are compared with calculations employing the complex semiclassical theory of Robert and Bonamy. This set of rotational transitions is the dominant feature of the

13 millimeter and submillimeter ozone spectra to be measured in the upcoming EOS-MLS mission.
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15 Keywords: Ozone; Linewidths; Pressure broadening; Atmospheric Spectra; Lineshape

#### 1. Introduction

17 Increased monitoring and improved modeling of ozone in the terrestrial atmosphere has continued to push the state-of-the-art for ozone spectroscopy. Many missions involving satellite, balloon, aircraft

and ground-based measurements have produced valuable data sets regarding ozone concentrations, in both columns and profiles. Methods utilizing emissive remote sensing have proven to be extremely
 valuable due to the broad range of spatial and temporal coverage available [1–5]. The earth observing

system—microwave limb sounder (EOS-MLS) instrument [1], part of NASA's AURA spacecraft, will take advantage of these factors by continuously monitoring ozone profiles through limb-sounding

25 measurements in a sun-synchronous orbit. Since ozone radiates energy through the rotational band at 25 the temperatures found in the troposphere and stratosphere, observation of these discrete air broadened 26 signals in the 240 and 640 GHz radiometers will directly identify the concentration of ozone along

the line of sight. Designed improvements in sensitivity, efficiency and frequency coverage compared

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- 1 to the UARS-MLS (in operation since 1991) will allow unprecedented signal-to-noise ratios for the strongest transitions found in these bands.
- 3 For processing of the radiative signatures into meaningful concentration profiles it is imperative that accurate and precise spectroscopic parameters be used to analyze the observed lineshapes. Ro-
- 5 tational transition frequencies, as well as intensities, are known to sufficient accuracy and precision as catalogued in the JPL millimeter and submillimeter spectral line database [6] and in HITRAN
- 7 [7]. These parameters are well understood quantum mechanically, and where not directly measured, can be interpolated. However, radiative molecules in perturbed environments (such as the terrestrial
- 9 atmosphere) experience broadening and/or shifting of the natural lineshape. Such effects are typically directly proportional to the number of perturbing species (pressure) and inversely proportional to the
- 11 log of the temperature. Furthermore, a decrease in collisional cross-section is generally observed at elevated rotational quanta. Currently, the state-of-the-art semi-classical treatment [8] that describes
- 13 these foreign gas perturbations can reproduce these trends and recent progress [9] has improved the accuracy to a few percent. However, recent and future missions require accuracies for pressure
- 15 broadening parameters to better than a few percent. Nonetheless, the theory confirms the functional form of the pressure and temperature dependencies within the atmospheric temperature range, and
- 17 thus insures the reliability of the empirical use of this model. Theory has been developed alongside the abundance of rotationally resolved *vibrational* spectra, for which a much greater amount of data
- 19 is available in comparison to the rotational band. Comparisons of infrared and pure rotational lineshape parameters are quite favorable for this species [10], in agreement with the results of theoretical
- 21 predictions.

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In this paper new measurements of pure rotational transition lineshapes of a series of transitions in the EOS-MLS bands is reported as well as new semi-classical calculations of the same parameters.

In depth comparisons to existing rotational and vibrational ( $v_1$  band only) data, will be made for

0

25 similar type transitions.

#### 2. Experimental details

Measurements were carried out with the submillimeter radiation passed twice through a 0.5 m length, 7.3 cm diameter, temperature controlled glass cell. The entire experimental design is shown
 in Fig. 1. A liquid-helium cooled InSb bolometer was used for detection of the frequency modulated

source. The mm and submm sources consisted of a Hewlett Packard phase-locked sweep synthesizer operating at  $\sim 12$  GHz followed by an active sextupler (Millitech or Agilent) that pumps either a Custom-Microwave whisker contacted diode, a n-harmonic generator ( $x_2$ ,  $x_3$ ), or a JPL-built antipar-

allel planar Schottky diode odd-harmonic multiplier  $(x_7)$  [11]. The implementation of this multiplier chain (opposed to a phase-locked mm-wave source) provides an easily tunable, stable, synthesized

35 radiation source for performing spectroscopy and linewidth measurements.

Table 1 lists the frequencies and quanta of the measured transitions. A simulation of the mm-wave transitions in the 230–252 GHz range is shown in Fig. 2. Spectral lineshapes were measured over a 16

-20 MHz interval about each line center as the pressure and temperature were systematically adjusted.
 Modulation depths of 2–4 MHz were sufficient for producing high signal-to-noise (S/N) second derivative spectra. The modulation depth is chosen for optimal S/N at higher pressures, therefore

41 resulting in over-modulated low pressure spectra. See Fig. 3 for typical baseline-subtracted sweeps

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Fig. 1. Experimental setup for measurement of O<sub>3</sub> linewidths.

Table	1				
Ozone	transitions	examined	in	this	study

$\overline{J_{K_a^\prime K_c^\prime}^\prime}$	$J_{K_a,K_c}$	v (MHz)	$\log(I_{ba})$
51,5	40,4	208642.44	$-4.17^{a}$
7 <sub>1,7</sub>	60,6	249788.60	-3.90
83,5	9 <sub>2,8</sub>	244158.04	-4.55
9 <sub>1,9</sub>	80,8	288959.14	$-3.68^{a}$
10 <sub>2,8</sub>	101,9	249961.96	-3.76
$12_{0,12}$	11 <sub>1,11</sub>	243453.70	-3.76
$12_{2,10}$	121,11	242318.74	-3.72
141,13	$14_{0,14}$	195430.51	$-3.92^{a}$
142,12	141,13	237146.19	-3.69
161,15	$16_{0,16}$	231281.49	-3.83
162,14	161,15	235709.84	-3.67
154,12	163,13	247761.77	-4.42
156,10	165,11	625371.47	-3.87
181,17	180,18	273050.90	-3.76
182,16	181,17	239093.26	-3.66
20 <sub>2,18</sub>	201,19	248183.38	-3.66
25 <sub>1,25</sub>	240,24	610365.33	-2.92
245,19	254,22	206132.05	$-4.72^{b}$
281,27	$28_{0,28}$	535922.77	$-3.62^{a}$
301,29	300,30	591249.01	-3.64
3110,22	30 <sub>9,21</sub>	2543208.40	$-2.76^{a}$
37 <sub>9,29</sub>	368,28	2509560.44	$-3.00^{a}$

<sup>a</sup>These transitions are calculated only in this study.

<sup>b</sup>This transition was previously measured in Ref. [13].



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Fig. 2. Simulation of  $O_3$  rotational transitions in the 230–252 GHz region, all half-widths are 2.9 MHz/Torr, traces are depicted for 1.3 (thin spikes) and 133 Torr (partially resolved) of air.



Fig. 3. The  $14_{2,12} \leftarrow 14_{1,13}$  transition measured at 0.069–0.582 Torr and 220 K shown between 237140 and 237152 MHz. Graphs are depicted at full scale(left) and  $10 \times$  (right).

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- 1 at various pressures during a fixed-temperature run. At low pressure, the linewidth is dominated by the modulation and the influence of pressure broadening on the instrumental lineshape is observed
- 3 only in the increased spacing between the side-lobes of the second derivative spectra. Each scan is preceded and followed by a scan of the cell with no absorber present for a reliable baseline
- 5 subtraction. For application of the convolution method [12] to the spectra it is imperative that all reference and test spectra are completely enclosed within the given scan range.
- Ozone is produced in modest amounts through cryogenic trapping of the output of an ozonizer on silica gel immersed in a dry ice/ethanol bath at 190 K. Initial pumping on the trap reduces the
   9 O<sub>2</sub> partial pressure to a minimum prior to flowing the O<sub>3</sub> through the spectrometer.
- The spectrometer cell is temperature controlled by flowing  $N_{2(l)}$  cooled methanol through a sleeve surrounding the cell. The gases flowing through the cell rapidly thermally equilibrate. Maximum flow
- speeds of  $\sim 24$  l/s were found to give more consistent results; no pressure gradient was observed across the flow cell. The temperature is monitored using a pair of 'T' type thermocouples, one
- imbedded in the coolant sleeve and the other resting in an ice bath. The coolant temperature can be regulated to within  $2^{\circ}$  of the desired temperature down to 190 K. The teflon windows are inset
- inside the cooling jacket to minimize thermal gradients in the white cell; secondary windows were used to keep atmospheric moisture from condensing on the cold teflon surface. The total pressure
- is monitored with a calibrated capacitance manometer for the most accurate determination of the
- 19 pressures. The pressure gauge showed deviations of less than 0.25% from actual pressure in a comparison to a standard.

#### 21 3. Analysis of measurements

The O<sub>3</sub> rotational transitions at these temperatures and pressures consist of a lineshape that is a combination of the Doppler and the Lorentz components convolved with the instrument function. The convolution method of Pickett [12] was used to compare two scans at the same temperature and obtain a differential Lorentzian half-width, induced entirely by the increased number of foreign gas

- perturbers in the higher pressure scan. This method for determination of pressure broadening due to a foreign gas does not require an analytical representation of the instrumental lineshape or precise
- knowledge of the concentration of the absorber. An experimental spectrum S(v, p) (see Fig. 3) at the pressure p is given by

$$S(v, p) = \int_{-\infty}^{\infty} S_{\mathbf{r}}(v', p') L(v - v', p - p') dv'$$
  
=  $S_{\mathbf{r}}(v', p') L(v - v', p - p'),$  (1)

$$L(v - v', p - p') = \frac{I\Delta v_{\Gamma}^2}{\Delta v_{\Gamma}^2 + (v - v' + \Delta v_{\delta})^2},$$
(2)

where  $S_r(v', p')$  is a reference spectrum taken at a lower pressure p' with half-width  $\Gamma(p')$  and shift 31  $\delta(p')$ . L(v - v', p - p') is a Lorentzian function the half-width  $(\Delta v_{\Gamma})$  and shift  $(\Delta v_{\delta})$  of which are

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1 dependent only upon the change in pressure due to additional broadening gas. The intensity factor, *I*, contains the Fourier constant and scales the spectra by peak height. This Lorentzian formulation,

3 as opposed to one scaled to peak area, provides minimal correlation between the parameters  $\Delta v_{\Gamma}$ and  $\Delta v_{\delta}$ .

$$\Delta v_{\Gamma} = \Gamma(p) - \Gamma(p'), \tag{3}$$

$$\Delta v_{\delta} = \delta(p) - \delta(p'). \tag{4}$$

- 5 An advantage of the convolution method for lineshape analysis is that the information regarding instrumental effects, Doppler broadening, and all sources of pressure broadening common to both
- 7 the low- and high-pressure samples is contained in the reference spectrum. The convolution method allows pressure broadening to be determined in the regime where there are other contributions
- 9 to the lineshape. For example, if  $S_r(v', p')$  is a Gaussian, S(v, p) will be a Voigt profile. The requirements for the method to be valid are that the absolute pressure of the broadened molecule
- 11 remain constant as the foreign gas is varied, that the absorption of the reference spectrum be linear at the line center and that the power and instrument function be constant over the broadened line 13 profile.

The parameters of the Lorentzian are varied within a non-linear least-squares-fit to minimize the difference between the convoluted spectrum and the test spectrum. Generally, all pressures in a given run are compared for generation of a data table, *N* pressure measurements in a given run

- 17 gives N(N-1)/2 data points. From eight to thirteen pressure measurements were made in any given run. At least eight runs at five different temperatures between 180 and 300 K were done
- 19 for each transition in this study (56–121 data points per run, 8–13 runs per line, ~400–1000 convolution generated data points per line). Each convolution fit provides a data point consist-
- 21 ing of differential pressure, differential half-width, differential shift and temperature for each transition. For all transitions in this study the differential shifts were found to be randomly dispersed
- 23 about zero shift. Furthermore, removing this parameter from the convolutions (i.e.  $\Delta v_{\delta} = 0$ ) did not change the differential half-widths. For determination of lineshape parameters the pressure broad-
- 25 ening is assumed to have a linear pressure and power-law temperature dependence as shown in Eq. (5).

$$\Delta v_{\Gamma} = \gamma_o \left( p - p' \right) \left( \frac{296}{T} \right)^n,\tag{5}$$

$$\Gamma(\gamma_o, n, p, T) = \gamma_o \ p \ \theta^{\ n}, \tag{6}$$

$$\Delta(\gamma_o, n, p, T) = [(\Delta \gamma_o \ p \ \theta^{\ n})^2 + (\Delta n \ln(\theta) \ \gamma_o \ p \ \theta^{\ n})^2 + (\Delta p \ \gamma_o \ \theta^{\ n})^2 + (\Delta \theta \ \gamma_o \ n \ p \theta^{\ n-1})^2 + 2\chi_{\gamma_o n} \Delta \gamma_o \Delta n \ln(\theta) \gamma_o \ p^2 \theta^{\ 2n} + 2\chi_{\gamma_o p} \Delta \gamma_o \Delta p \gamma_o \ p \theta^{\ 2n} + 2\chi_{\theta n} \Delta \theta \Delta n \ln(\theta) \ (\gamma_o \ p)^2 n \ \theta^{\ 2n-1}]^{1/2},$$
(7)

27 where

$$\theta = \left(\frac{296}{T}\right), \quad \Delta\theta = \left(\frac{296}{T^2}\right)\Delta T,$$
(8)

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Fig. 4. Temperature normalized data set for the  $16_{1,15} \leftarrow 16_{0,16}$  transition at 231281.49 MHz.

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$$\sigma_{\max} = \Delta(\gamma_o, n, p, 180). \tag{9}$$

Values of the dependent variable  $\Delta v_{\Gamma}$  are used to determine the coefficients,  $\gamma_o$  and n, of Eq. (5) 3 based on a parametric fit to all temperature and differential pressure data. The parametric fit also provides the correlation coefficient between the errors of the linear pressure dependence and the 5 exponential temperature dependence. Correlations between  $\Delta \gamma_o$  and  $\Delta n$ , of 0.6–0.8 are typically obtained. Fig. 4 shows the complete data set for the  $16_{1,15} \leftarrow 16_{0,16}$  transition when the temper-

- 7 ature exponent n = 0.710 is used to normalize the pressure dependence to the reference value of 296 K. Table 2 shows the values of the parameters determined in the parametric fits. Eq. (6) allows
- 9 calculation of the pure Lorenztian broadened width of a transition at arbitrary pressure and temperature. For calculation of the propagated error in the half-width (see Eq. (7)) the necessary  $1\sigma$  errors
- 11 (following each parameter, in units of last reported digit) and determined correlation coefficients for each transition are included in Table 2.
- For calculation of random errors derived from the parameters given in Table 2, the recommended values for the pressure and temperature errors and corresponding correlation coefficients are:  $\Delta p =$
- 15 0.25% *p* (Baratron calibration);  $\Delta T = 1$  K (*T*-type thermocouple 200–350 K),  $\chi_{Tn} = 1.0$  and  $\chi_{\gamma_o p} = 1.0$ . Note that  $\chi_{pn} = 0$ ,  $\chi_{pT} = 0$  and  $\chi_{qT} = 0$  have been assumed for Eq. (7). These values give a maximum
- 17 random error of 1.8-4.5% over the range of stratospheric temperatures (180-300 K) and pressures (< 100 mb). The random error typically increases 1-2.5% from 300 K down to 180 K primarily
- 19 because of the increase in the relative error of the temperature measurement compounded with the larger pressure-broadened half-width at lower temperature. Maximum error values calculated at 180 K
- 21 for each transition are shown in Table 2 to indicate the maximum error for the coldest stratospheric temperatures.

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# Table 2 Measured ozone pressure induced half-width parameters determined in this study

$J_{K_a^\prime,K_c^\prime}^\prime$	$J_{K_a,K_c}$	γ <sub>o</sub> (296) (MHz/Torr)	n	$\chi_{\gamma_o n}$	$2\sigma_{\max}{}^{a}$
71,7	60,6	3.236(8)	0.674(9)	0.7767	2.3%
83,5	9 <sub>2,8</sub>	3.181(17)	0.749(18)	0.8103	3.8%
$10_{2,8}$	101,9	3.157(6)	0.675(7)	0.7079	2.1%
$12_{0,12}$	$11_{1,11}$	3.062(10)	0.685(14)	0.7435	2.9%
$12_{2,10}$	121,11	3.103(7)	0.663(8)	0.6934	2.1%
141,13	$14_{0,14}$	2.9199			
$14_{2,12}$	$14_{1,13}$	3.037(10)	0.693(10)	0.8123	2.6%
161,15	$16_{0,16}$	2.986(8)	0.710(9)	0.7352	2.3%
162,14	161,15	2.971(8)	0.677(9)	0.7718	2.3%
154,12	163,13	3.014(15)	0.685(14)	0.8368	3.2%
156,10	165,11	$2.988(19)^{b}$	$0.745(25)^{b}$	0.6539	4.5%
181,17	$18_{0,18}$	3.0591	0.629		$\sim \! 10\%$
182.16	181.17	2.980(7)	0.692(8)	0.7529	2.2%
$20_{2,18}$	201,19	2.949(5)	0.680(5)	0.6754	1.8%
301,29	300,30	2.8615	0.543		$\sim 10\%$
251,25	240,24	2.7246	0.638		$\sim 10\%$

<sup>a</sup>See Eq. (9).

<sup>b</sup>These values calculated from measured N<sub>2</sub> and O<sub>2</sub> values using Eq. (12).

Proper application of the convolution method requires attention to a few key spectroscopic issues.
 Spectra should have minimal fluctuations in power and spectral dispersion as well as sufficiently
 weak absorption. Weak absorption was routinely checked through measurements of AM spectra indicating the maximum absorptions were 10% or less for the given partial pressure of absorber.

5 Fluctuations in power and dispersion have been minimized through alignment and multiplier tuning to insure contributions to systematic error in the line broadening parameters are much less than 1%.

7 Bias due to correlations between parameters have been minimized within the convolution algorithm as well as during the parametric fitting.

#### 9 4. Theoretical considerations

#### 4.1. Complex Robert–Bonamy formalism

A more complete description of the complex Robert-Bonamy (CRB) formalism [8] can be found in Refs. [17–19] here only the salient features are presented. The formalism is a semi-classical development based on the resolvent operator formalism of Baranger [20], Kolb [21], and Greim [22]

- (BKG) and is complex valued thus the half-width and line shift are obtained from a single calculation. The application of linked-cluster techniques [23] eliminates the awkward cutoff procedure
- that characterized earlier theories [24–26]. The intermolecular dynamics are correct to second-order in time utilizing curved rather than straight line trajectories based on the isotropic part of the
- 17 in time utilizing curved rather than straight line trajectories based on the isotropic part of the

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- 1 intermolecular potential. This has important consequences in the description of close intermolecular collisions (small impact parameters). Also important for close collision systems is the incorporation
- 3 in the CRB theory of a short range (Lennard–Jones 6–12 [27]) atom–atom component to the intermolecular potential. This component has been shown to be essential for a proper description of
- 5 pressure broadening, especially in systems where electrostatic interactions are weak [28]. The notion of strong and weak collisions adopts the definition of Oka [29].
- 7 The half-width,  $\gamma$ , and shift,  $\delta$ , of a rotation band transition  $f \leftarrow i$  are given in the CRB formalism by minus the imaginary part and the real part, respectively, of the diagonal elements of the complex
- 9 relaxation matrix. In the mean-relative-thermal-velocity (mrtv) computational form, the half-width and line shift are usually expressed in terms of the Liouville scattering matrix ([20,30])

$$(\gamma - i\delta)_{f \leftarrow i} = \frac{n_2 \bar{v}}{2\pi c} \sum_{J_2} \langle J_2 | \rho_2 | J_2 \rangle \int_0^\infty 2\pi b [1 - e^{-S_2}] \, \mathrm{d}b, \tag{10}$$

- 11 where  $\bar{v}$  is the mean relative thermal velocity,  $\rho_2$  and  $n_2$  are the density operator and number density of perturbers, and b is the impact parameter.  $S_2$  is the second order term in the expansion of the 13 Liouville scattering matrix which depends on the intermolecular potential.
- The  $S_2$  term is complex valued and anisotropic. The potential employed in the calculations consists of the leading electrostatic components for the  $O_3$ -X pair consisting of the dipole and quadrupole
- moments of  $O_3$  with the quadrupole moment of  $N_2$  or  $O_2$ , and an atom-atom component [31,17]). 17 The atom-atom potential is defined as the sum of pair-wise Lennard-Jones 6–12 interactions [27]

between atoms of the radiating molecules (labeled 1) and the perturbing molecule (labeled 2),

$$V^{at-at} = \sum_{i=1}^{n} \sum_{j=1}^{m} 4\varepsilon_{ij} \left\{ \frac{\sigma_{ij}^{12}}{r_{1i,2j}^{12}} - \frac{\sigma_{ij}^{6}}{r_{1i,2j}^{6}} \right\}.$$
(11)

- 19 The subscripts 1*i* and 2*j* refer to the *i*th atom of molecule 1 and the *j*th atom of molecule 2, respectively, *n* and *m* are the number of atoms in molecules 1 and 2, respectively, and  $\varepsilon_{ij}$  and  $\sigma_{ij}$ 21 are the Lennard–Jones parameters for the atomic pairs. The heteronuclear atom–atom parameters can
- be constructed from homonuclear atom-atom parameters ( $\varepsilon_i$  and  $\sigma_i$ ) by the combination rules of Hirschfelder et al. [32] or Good and Hope [33].
- The atom-atom distance,  $r_{ij}$  is expressed in terms of the center of mass separation, R, via the expansion of Sack [34]. The expansion in (1/R) must be truncated, sufficient order must be chosen to insure the convergence of calculated half-widths and line shifts. The order of the expansion has
- been discussed by Labani et al. [35] and by Gamache et al. [31,17,18]. Here the formulation of Neshyba and Gamache [31] expanded to eighth order is used.
- 29 The isotropic component of the atom-atom potential is used to define the trajectory of the collision within the semiclassical model of Robert and Bonamy [8]. The temperature dependence of the
- half-width was taken as its usual form [36,37] as discussed earlier for the laboratory measurements (see Eq. (6)). The reference temperature,  $T_0 = 296$  K, is not restricted to this value but is the usual choice.
- Eq. (6) is approximate. Simplified models for the temperature dependence of the half-width have been discussed by Birnbaum [38] or Bonamy et al. [39]. The methods are based on the temperature

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Table 3						
Molecular	moments	used	in	the	CRB	calculations

Molecule	Multipole moment (esu)	Ref.
O <sub>3</sub>	$m = 0.532 \times 10^{-18}$	[44]
	$Q_{xx} = -1.40  imes 10^{-26}$	[44]
	$Q_{yy} = -0.70 \times 10^{-26}$	[44]
	$Q_{zz} = 2.10 \times 10^{-26}$	[44]
$N_2$	${ m Q}_{zz} = -1.4  imes 10^{-26}$	[45]
O <sub>2</sub>	${ m Q}_{zz} = -0.4  imes 10^{-26}$	[46]

dependence of the terms in the intermolecular potential. Unfortunately, the intermolecular potentials that mimic the true interaction generally contain too many terms for the analysis of Refs. [38] and
 [39]. The intermolecular potential employed in the calculations presented here contains 170 terms.

However, the general forms of the dependencies can still be of value.

5 Better models have been proposed for the temperature dependence of the half-width. Pack [40], in a study of  $CO_2$  broadened by He and Ar, proposed a polynomial in T for the temperature

7 dependence of the half-width;  $\gamma = c_1 T^{-1} + c_2 + c_3 T^1$ . More recently in a study of the temperature dependence of the half-width of the 500.4 GHz transition ( $34_{2,32} \leftarrow 34_{1,33}$ ) of the ground vibrational

9 state of ozone Gamache [41], at the suggestion of Rossi [42], proposed a double power law model;  $\gamma(T) = b_0 \{T_0/T\}^{b_1} + b_2 \{T_0/T\}^{b_3}$ , which correctly modeled the temperature dependence when the

11 temperature range was large. For the temperature range considered in this paper, Eq. (6) is an appropriate model.

#### 13 4.2. Theoretical calculations

Calculations of the half-width and line shift based on the CRB formalism were made for the 22 pure rotational transitions of  $O_3$  listed in Table 1 at 150, 225, 296, 350 and 450 K with  $N_2$  and  $O_2$  as the perturbing gases. The CRB formalism yields the half-width and line shift from a single calculation and there are no adjustable parameters or cutoff procedure [43] in the formalism.

All molecular parameters used in this work are the best available values from the literature. No

19 molecular constants have been adjusted to give better agreement with experiment. The dipole and quadrupole moments of ozone are taken from Ref. [44]. The quadrupole moment of nitrogen is from

21 Mulder et al. [45] and that for oxygen is from Stogryn and Stogryn [46]. The numerical values are listed in Table 3. The atom-atom parameters were obtained using the standard combination rules [32]

23 with the atom-atom parameters for homonuclear diatomics determined by Bouanich [47] by fitting to second virial coefficient data. These parameters are reported in Table 4. The atom-atom potential

25 is expanded to eighth-order in the molecular centers of mass separation. In the parabolic trajectory approximation the isotropic part of the interaction potential is taken into account in determining the

27 distance, effective velocity, and force at closest approach [8]. To simplify the trajectory calculations the isotropic part of the atom-atom expansion is fit to an isotropic Lennard-Jones 6-12 potential,

29 giving  $\varepsilon/k = 43.9$  K and  $\sigma = 3.15$  Å for the ozone-nitrogen collision pair and  $\varepsilon/k = 51.73$  K and  $\sigma = 3.01$  Å for the ozone-oxygen collision pair.

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Table 4

Values of the heteronuclear atom-atom parameters for the collision pairs

Atomic pair	σ (Å)	$\varepsilon/k_{\rm B}(K)$
O–N	3.148	43.90
0–0	3.010	51.73

Table 5

CRB calculated half-widths and line shifts at 296 K in units of MHz/Torr for  $N_2$ -,  $O_2$ -, and air-broadening of ozone transitions in the rotation band

$J_{K_a^\prime K_c^\prime}^\prime$	$J_{K_a,K_c}$	$\gamma_o(N_2)$	$\delta_o(\mathrm{N}_2)$	$\gamma_o(O_2)$	$\delta_o(\mathrm{O}_2)$	$\gamma_o(\mathrm{air})$	$\delta_o(\mathrm{air})$
156,10	165,11	3.099	-0.004	2.680	-0.006	3.011	-0.004
379,29	368,28	2.768	0.004	2.293	0.001	2.668	0.003
3110,22	309,21	2.828	0.009	2.369	0.000	2.732	0.007
245,19	254,22	2.842	0.002	2.360	0.005	2.741	0.003
161,15	$16_{0,16}$	3.053	0.005	2.470	0.010	2.931	0.006
16 <sub>2,14</sub>	161,15	3.021	-0.001	2.472	0.001	2.906	-0.001
14 <sub>2,12</sub>	14 <sub>1,13</sub>	3.091	-0.001	2.565	-0.001	2.981	-0.001
182,16	181,17	2.966	-0.001	2.403	0.003	2.848	0.000
$12_{2,10}$	$12_{1,11}$	3.165	0.000	2.666	-0.002	3.060	0.000
120,12	$11_{1,11}$	3.210	0.006	2.664	0.010	3.095	0.007
154,12	163,13	3.049	0.000	2.572	-0.006	2.949	-0.001
202,18	$20_{1,19}$	2.924	-0.002	2.357	0.003	2.805	-0.001
7 <sub>1,7</sub>	60,6	3.299	-0.005	2.838	0.001	3.202	-0.004
83,5	9 <sub>2,8</sub>	3.296	0.008	2.873	-0.004	3.207	0.005
102,8	101,9	3.234	0.001	2.766	0.000	3.136	0.001
14 <sub>1,13</sub>	$14_{0,14}$	3.115	0.005	2.555	0.011	2.997	0.006
5 <sub>1,5</sub>	$4_{0,4}$	3.312	-0.009	2.874	0.001	3.220	-0.007
181,17	$18_{0,18}$	3.001	0.008	2.406	0.014	2.876	0.009
9 <sub>1,9</sub>	80,8	3.275	-0.002	2.783	0.004	3.172	-0.001
281,27	$28_{0,28}$	2.845	0.010	2.304	0.005	2.731	0.009
301,29	300,30	2.824	0.009	2.299	-0.006	2.714	0.006
251,25	24 <sub>0,24</sub>	2.875	-0.007	2.309	-0.011	2.756	-0.008

To evaluate the reduced matrix elements rotational-vibrational wave functions are needed. The ground vibrational state wavefunctions used in the calculations are determined with the Watson–
 Hamiltonian constants of Camy–Peyret and Flaud [48]. The molecular constants for N<sub>2</sub> and O<sub>2</sub> are

from Huber and Herzberg [49].

5 Using Eq. (6) with the temperatures and corresponding calculated half-widths a least-squares fit can be made to determine the temperature exponent, n, and the correlation coefficient of the fit. The

7 uncertainty of the calculated temperature exponents is determined for each transition by the following procedure. Values of n are determined using any two of the five calculated points. This generates ten

9 2-points values of n. The uncertainty assigned to the calculation is the maximum difference between the least-squares fit value and the ten 2-points values.

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Fig. 5. Theoretical calculations of the temperature dependence of the pressure-induced half-width exhibiting (a) normal power-law behavior for the  $7_{1,7} \leftarrow 6_{0,6}$  transition and (b) deviations from the power-law expression for the  $18_{1,17} \leftarrow 18_{0,18}$  transition of O<sub>3</sub>.

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Table 6

Temperature dependence of the air-broadened half-width of ozone transitions in the rotation band with the estimated error in parenthesis, correlation coefficient, R, of the fits, and reduced temperature range fit

$J_{K_a^\prime,K_c^\prime}^\prime$	$J_{K_a,K_c}$	n (150–450 K)	R	n (225–350 K)
5 <sub>1,5</sub>	40,4	0.830(14)	0.99997	0.823
71,7	60,6	0.820(12)	0.99998	0.82
83,5	9 <sub>2,8</sub>	0.790(13)	0.99998	0.78
9 <sub>1,9</sub>	80,8	0.810(13)	0.99998	0.806
10 <sub>2,8</sub>	101,9	0.790(20)	0.99995	0.78
$12_{2,10}$	$12_{1,11}$	0.780(35)	0.99983	0.77
$12_{0,12}$	$11_{1,11}$	0.800(39)	0.99981	0.78
14 <sub>1,13</sub>	$14_{0,14}$	0.790(64)	0.99943	0.76
142,12	$14_{1,13}$	0.780(55)	0.99955	0.76
161,15	160,16	0.790(72)	0.99923	0.76
16 <sub>2,14</sub>	161,15	0.790(76)	0.99912	0.76
154,12	163,13	0.790(71)	0.99924	0.76
156,10	165,11	0.790(55)	0.99954	0.77
182,16	181,17	0.800(86)	0.99881	0.77
181,17	$18_{0,18}$	0.810(94)	0.99870	0.770
202,18	201,19	0.820(92)	0.99876	0.79
25 <sub>1,25</sub>	$24_{0,24}$	0.820(92)	0.99877	0.790
245,19	254,22	0.830(96)	0.99875	0.80
281,27	$28_{0,28}$	0.840(89)	0.99889	0.808
301,29	300,30	0.830(86)	0.99893	0.806
3110,22	309,21	0.810(72)	0.99922	0.79
379,29	368,28	0.820(73)	0.99920	0.79

#### 1 4.3. Theoretical results

The air-broadened half-widths for the 22 transitions studied were determined from the N<sub>2</sub>- and O<sub>2</sub>-broadened half-widths using Eq. (12). The calculated N<sub>2</sub>-, O<sub>2</sub>-, and air-broadened half-width and line shift are given in Table 5.

$$\gamma_{\rm air} = 0.79 \gamma_{\rm N_2} + 0.21 \gamma_{\rm O_2}. \tag{12}$$

5 The temperature dependence parameters, n, of the air-broadened half-widths given by Eq. (6) are

given in tables along with the estimated error and the correlation coefficient of the fit. Fig. 5 shows 7 plots of  $\ln[\gamma(T)/\gamma(T_0)]$  versus  $\ln[T_0/T]$  for air-broadening of the  $7_{1,7} \leftarrow 6_{0,6}$  and  $18_{1,17} \leftarrow 18_{0,18}$ transitions of O<sub>3</sub>. The first of these figures is an example for which the model (Eq. (6)) is a

9 good approximation to the temperature dependence of the half-width. The correlation coefficient for the fit of this line is 0.99997. However, for the second figure  $(18_{1,17} \leftarrow 18_{0,18}$  transition) the

11 fit over the temperature range 150–450 K is not correctly modeled by Eq. (6), with a correlation coefficient of 0.99870. As discussed by Gamache [41] when the temperature range is large, expression

13 6 does not fit the data accurately and a more complex model is needed. The measured temperature

15 exponents were from a fit of the range 180–300 K. The last column of Table 6 gives the temperature

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- 1 exponent determined from the CRB calculations over the range 225–350 K. The change in temperature range yields temperature exponents that are on average 3% lower with a maximum low-
- 3 ering of  $\sim$ 5%. The temperature exponents determined from the reduced temperature range are in better agreement with the measured values. There is also the question of the difference between
- 5 mean-relative-thermal-velocity (mrtv) calculations versus calculations made including the average over the relative velocity [41]. In the study of Ref. [41] the difference between the two methods of
- 7 calculation was  $\sim$ 5% for the temperature dependence of the half-width.

#### 5. Discussion

#### 9 5.1. Sources of error

The possible experimental sources of error have been minimized. However, the assumption that the gas flowing through the spectrometer has reached thermal equilibrium with the cell is considered as a potential source of systematic error in the temperature measurement. Another potential source for systematic error is the assumption that the absorber partial pressure is constant throughout an experimental run. These possibilities and the influence on the reported parameters will now be discussed

15 discussed.

As mentioned previously, the convolution method requires the absorber partial pressure to remain 17 constant for reliable results. Experimentally, the  $O_3$  partial pressure was often variable. Ideally, the partial pressure was kept to  $\sim 1$  mTorr, but weaker transitions often required up to 15 mTorr O<sub>3</sub> for sufficient S/N. In runs where the partial pressure was > 10 mTorr a significant decrease in 19 the  $O_3$  partial pressure could be observed as the buffer gas pressure was *increased*. For an  $O_3$ self-broadened half-width *larger* than the air-broadened half-width the decrease in partial pressure 21 of  $O_3$  (and subsequent overestimate of buffer gas pressure) would cause an apparent *decrease* in the half-width determined for the data run. For each data point in concern the O<sub>3</sub> self-broadened 23 half-width was measured under the same conditions for estimation of the systematic error introduced by the partial pressure changes. The values for ozone self-broadened half-width fall into the range, 25  $\gamma_o(296) = 4.04 - 4.71 \text{ MHz/Torr}$  and n = 0.74 - 1.24, with the average values,  $\gamma_o(296) = 4.44 \text{ MHz/Torr}$ 27 and n = 0.98. Using the individual O<sub>3</sub> self-broadened half-width parameters and partial pressure

deviations the *narrowed* half-width for a suspect run was checked vs. the *normal* value. Normally the value did not change more than 0.5%, a surprising result that rectifies the use of all N(N-1)

values available in a comparison of N scans. When the values were more than 1% different, the run 31 was not used in the parametric fit.

- Temperature gradients within the flow of the gas due to slow equilibration and/or contact with warmer windows would increase as the bath temperature is moved further from room temperature, therefore increasing the error of the temperature measurement proportionately to the difference be-
- 35 tween the cell temperature and room temperature. Furthermore, the directionality of this potential systematic error source would always cause n to be underestimated. Such an error would scale to
- 37 the cell dimensions, and if large enough to be a problem, would be noticeable with the use of a variety of different length and/or diameter cells. For the 625.4 GHz  $(15_{6,10} \leftarrow 16_{5,11})$  transition in this
- 39 study, two different cells (L = 0.5 and 1.0 m) were used during experimentation and measurements overlapped within the uncertainties, in fact the shorter cell showed a slightly larger temperature

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Fig. 6. Comparisons of measured and calculated values for the temperature dependence of the pressure induced half-width for the various  $K_a=1$  transitions.  $\square$  Measured rotational (this study),  $\square$  measured rotational (CNRS) [15] (left) Connor [50] (right),  $\triangle$ —measured vibrational  $v_1$  branch (Langley) [14] and  $\Box$ —calculated rotational (this study).

- 1 exponent. If such a systematic error exists it must be significantly smaller than the random error. Furthermore, the magnitudes of the measured exponents are consistent with comparisons to other
- temperature dependent studies such as Smith [14] where very similar values are determined for the 3  $K_a = 1$  transitions (see Fig. 6).

5

Theoretical values for the temperature exponents are all higher than measured values, with the values coming into closer agreement when the calculated values are limited to a similar temperature range compared to the measured values. Ideally, the pressure and temperature dependencies 7

determined by theory and experiment would randomly disperse. The theoretical values are all larger

9 as the temperature decreases as shown in the analogous plot for the exponents. Interestingly, the crossing point is at higher temperatures for the two largest J transitions.

#### 11 5.2. Comparisons of results

Measurements have been reported for O<sub>3</sub> in the 240 and 640 GHz bands of EOS-MLS, and cal-13 culations for transitions for these as well as the transitions located in 2.5 THz band. Experimental measurements of these transitions are planned using a different spectrometer. In addition to the

fourteen transitions of interest to EOS-MLS, eight additional transitions were investigated to pro-15 vide further comparison of the present work to existing infrared and previous FIR and mm-wave

17 results.

Plots of the J-dependence of the half-width are shown in Fig. 7 for the  $J_{2,J-2} \leftarrow J_{1,J-1}$  and  $J_{1,J-1} \leftarrow J_{0,J}$  Q branches that are predominant features in the rotational bands. The agreement 19 between the present experiments and CRB calculations is quite good at J < 15 for the Q branch and at all comparable values for  $K_a = 0$ . The monotonic decrease in half-width with increase in 21 J is readily extended to show agreement with measurements of Smith et al. [14] for the  $v_1$  branch

23 and the single measurement in the submillimeter by Priem et al. [15].

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Fig. 7. Comparisons of measured and calculated values for pressure induced half-width values at 296 K for the  $J_{2,J-2} \leftarrow J_{1,J-1}$  transitions (left) and various  $K_a = 0$  transitions (right).  $\Diamond$ —Measured rotational (this study),  $\bigcirc$ —measured rotational (CNRS) [15] (left) Connor [50] (right),  $\triangle$ —measured vibrational  $v_1$  branch (Langley) [14] and  $\square$ —calculated rotational (this study).

- 1 Comparisons to other branches in the  $v_1$  data [14] show very good agreement among similar  $J, K_a$  transitions. Unlike the Q branches, the R branches reported in Ref. [14] are for many of the same J
- values as measured for Q branches in this work. Not shown in Fig. 7 is the J + 1<sub>2,J</sub> ← J<sub>1,J-1</sub> and J + 1<sub>1,J</sub> ← J<sub>0,J</sub> R type branches reported by Smith et al. these values all overlap the measurements
   of this study. As theory has suggested, there seems to be very little vibrational dependence of the
- b) b) this study. This theory has suggested, there seems to be very hitse violational appendix half-width parameters.
  7 The EID study of Lorgen [1() superty on extension number of helf width for higher such.
  - 7 The FIR study of Larsen [16] reports an extensive number of half-widths for higher values of  $K_a$ . A few of the transitions in the present work can be compared by extrapolation of the *J*-dependence
- 9 to lower values. Comparison of the  $15_{6,10} \leftarrow 16_{5,11}$  branch transition to similar  $K_a$  values in [16] shows an agreeable trend of increasing half-width for decreasing J, as observed for the lower values 11 of  $K_a$ .

The absence of measurable shifts in the rotational spectra is not unexpected since the theoretical results give a maximum  $\delta_o$  of 0.009 MHz/Torr. Line shifts in air have been measured in the  $v_1$ band that range from -0.288 to 0.180 MHz/Torr. This result is expected since the theory has shown

- that the dominant part of the intermolecular potential responsible for the line shift is the vibrational dephasing term,  $S_1$ . Whenever there is a change in vibrational state for the transition the  $S_1$  term
- 17 is non zero and tends to be greater than the imaginary parts of the  $S_2$  terms. The contribution of the  $S_1$  term is independent of the rotational states. As the number of vibrational quanta exchanged

19 in a transition increases the  $S_1$  contribution increases and the line is approximately given by the  $S_1$  contribution plus small fluctuations about this value given by the rotational contributions to the shift.

- Comparisons of the temperature exponent, n, show a generic agreement throughout experiments, with values typically falling in the range 0.6–0.8 without any obvious  $J, K_a$  dependence. The CRB
- results do not show nearly as much randomness and are often larger than the measured values. Any trends suggested by the CRB calculations cannot be verified due to the present accuracy limits in
  - the measured values.

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#### 1 6. Conclusion

This paper has presented a comprehensive analysis of the air-broadened  $O_3$  millimeter and submillimeter rotational transitions that will facilitate the study of  $O_3$  in the Earth's stratosphere and upper troposphere. The work produces several broadening parameters precise to 2% at the  $2\sigma$  level, and indicates clear trends in the *J* and  $K_a$  dependence of the half-width parameters in showing

agreement between rotational, vibrational and theoretical studies.

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