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Midterm Exam. Astronomy & Astrophysics I

1. Angular Resolution of Telescopes

Calculate the theoretical angular resolution of:

- A. The Gemini optical Telescope (8m aperture, at visible wavelengths)
- B. Global VLBI (Radio, at $\sim 1\text{GHz}$)
- C. Given that atmospheric turbulence (or astronomical “Seeing”) limits resolution to $\geq 0.5''$, what is the primary purpose of large optical telescopes?

2. From the observation that the Sun’s energy output peaks in the yellow part of the spectrum ($\lambda_{\text{Max}}=500\text{ nm}$), estimate its effective surface temperature and luminosity.

3. Luminosity and Distance

The bright star Omicron Eridani ($m_V=4.4$, $T=5,300\text{ K}$) has an annual parallax motion of $0.2''$.

- A. Find the distance to Omicron Eridani (in pc)
- B. Absolute magnitude of Omicron Eridani
- C. Hence calculate the luminosity (in solar units) of Omicron Eridani.

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4. Luminosity, Radius, Temperature, Relationship

Omicron Eridani has a binary companion (actually it's a triple system).

Star B is much fainter, despite being hotter ($m_V=9.5$, $T=16,500$ K)

A. Find the stellar radii of R_A & R_B in solar units. (hint: find the ratio first)

B. Comment on what types of stars these are.

5. Spectral Types

A. State the three most important spectral characteristic of stars of spectral types: O, A M, and briefly note the physical condition responsible.

O:

A:

M:

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6. Orbital Dynamics of Binary Stars

The stars β Aurigae A and β Aurigae B, constitute a dual-lined eclipsing spectroscopic binary with an orbital period of 3.96 days. The observed radial velocity curves have amplitudes $v_A = 108$ km/s and $v_B = 111$ km/s.

Calculate the masses of the two stars.

7. Sketch the Hertzsprung Russell Diagram.

Label the key features, and indicate order-of-magnitude values for Temperature, Luminosity, and Radius.



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8. Stellar Physics.

Apply the Virial Theorem, (plus any other relevant stellar physics) to estimate the temperature deep inside the Sun.

9. Nuclear Reactions

Write out the steps of the Proton-Proton chain

10. Nuclear Reaction Conditions.

Estimate the interaction energy required for protons to get close enough together to have a reasonable probability of undergoing quantum tunneling, and compare this to the typical kinetic energy of solar protons.

C. What is likely the dominant energy production process (and why) in:

A. The Sun

B. Sirius

C. Brown Dwarfs

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Formulae:

Wien's Law	$\lambda_{\max} = \frac{T}{2.9 \times 10^{-3} \text{ m K}}$
Hydrostatic Equilibrium	$\frac{dP_r}{dr} = -\frac{GM_r \rho_r}{r^2}$
Mass Distribution	$\frac{dM_r}{dr} = 4\pi r^2 \rho_r$
Gravitational Potential Energy	$U_G = -\frac{3}{5} \frac{GM^2}{R}$
Magnitudes	$m_1 - m_2 = -2.5 \log_{10} \frac{f_1}{f_2}$
Distance modulus and absolute magnitude	$\mu = m - M = 5 \log_{10} D_{pc} - 5$ $(M_A + M_B) \sin^3 i = \frac{P(v_A^{obs} + v_B^{obs})^3}{2\pi G}$
Kepler's Law	$(M_A + M_B) \sin^3 i = \frac{4\pi^2}{GP^2} (a_A \sin i + a_B \sin i)^3$
Proton Mass:	1.67 x10 ⁻²⁷ kg
Electron Mass:	9.11 x10 ⁻³¹ kg
Electron Charge:	-1.9x10 ⁻¹⁹ C
Sun: Mass:	1.99 x10 ³⁰ kg
Mean Radius:	6.38 x10 ⁵ km
Absolute Magnitude:	+4.83
Apparent magnitude:	-26.74
Flux at Earth:	1.4 x10 ³ W/m ²
Earth: Mass:	5.98 x10 ²⁴ kg
Mean Radius:	6.38 x10 ³ km
Earth-Sun Distance:	1AU = 150 x10 ⁶ km
Plank's Constant:	6.63 x10 ⁻³⁴ J.s
Stefan-Boltzmann Constant:	5.67 x10 ⁻⁸ W/m ² .K ⁴
Boltzmann's Constant:	1.38 x10 ⁻²³ J/K
Coulomb Constant:	9 x10 ⁹ N/C
Gravitational Constant:	6.67 x10 ⁻¹¹ N.m ² /kg