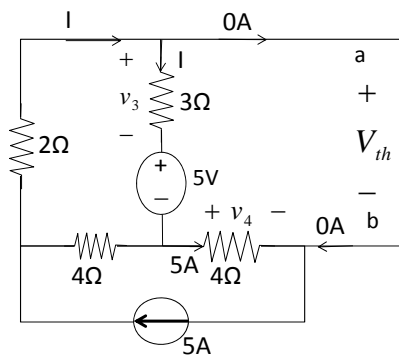


Practice 1: Find  $R_{th}$ ,  $V_{th}$  for the two terminal circuit



$$R_{th} = 4 + 3 // (2 + 4) = 6\Omega$$

$$V_{th} = v_3 + 5 + v_4 = 3I + 5 + 4 \times 5$$

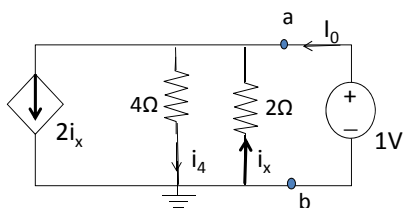
To find  $I$ , use mesh analysis

$$3I + 5 + 4(I - 5) + 2I = 0$$

$$9I = 15, I = 5/3$$

$$V_{th} = 3 \times 5/3 + 25 = 30V$$

Practice 2: Find  $R_{th}$ ,  $V_{th}$  for the two terminal circuit



No independent source.

$$V_{th} = 0.$$

To find  $R_{th}$ , supply 1V.

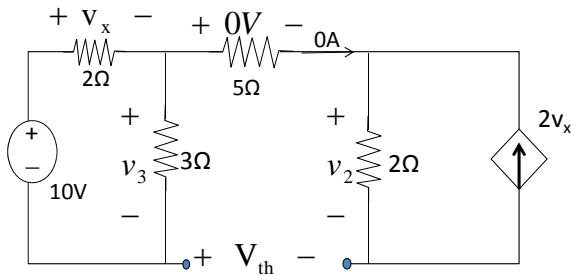
$$i_x = -1/2A, i_4 = 1/4$$

$$I_0 = i_4 + 2i_x - i_x = 1/4 - 1/2 = -1/4A$$

$$R_{th} = 1/I_0 = -4\Omega$$

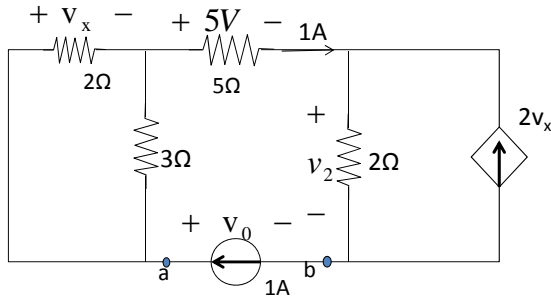
Negative resistance due to dep source.

Practice 3: Find  $R_{th}$ ,  $V_{th}$  for the two terminal circuit



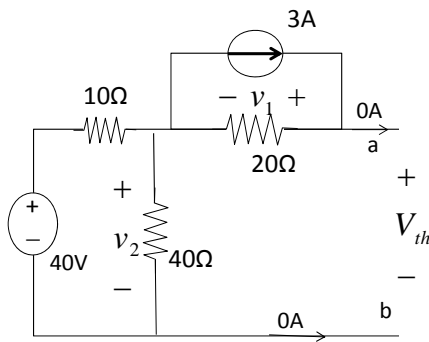
$V_{th} = v_2 - v_3$   
 By voltage division,  
 $v_3 = (3/5) \times 10 = 6V$ ;  
 $v_x = 4V$   
 By Ohm's law,  $v_2 = 2 \times 2v_x = 16V$ ;  
 $V_{th} = 16 - 6 = 10V$

For  $R_{th}$ , supply 1A



$v_x = 1 \times (2/3) = 1.2V$ ,  
 $v_2 = 2(2v_x + 1) = 6.8V$   
 $v_0 = v_x + 5 + v_2 = 13V$ ,  
 $R_{th} = v_0 / 1 = 13\Omega$

Practice 4: Find the Norton's equivalent

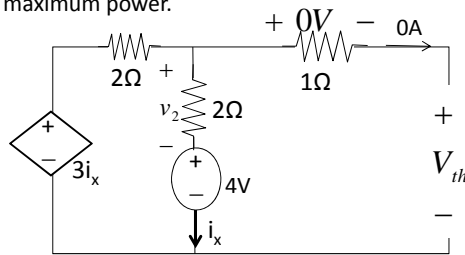


$R_N = 20 + 40 // 10 = 28\Omega$

It is easier to find  $V_{th}$ , then  $I_N = V_{th} / R_N$

$V_{th} = v_1 + v_2$   
 $v_1 = 20 \times 3 = 60V$   
 Same current in 10Ω and 40Ω.  
 By voltage division,  
 $v_2 = (40/50) \times 40 = 32V$   
 $V_{th} = v_1 + v_2 = 92V$ ;  
 $I_N = 92/28 = 23/7\Omega$

Practice 5: Find the value of  $R_L$  so that maximum power is delivered. Also find the maximum power.



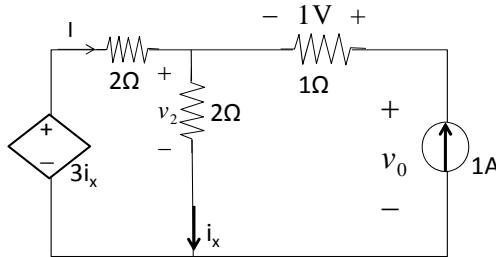
$$V_{th} = v_2 + 4$$

To find  $v_2$ , use mesh analysis.

$$2i_x + 2i_x + 4 - 3i_x = 0$$

$$i_x = -4A$$

$$V_{th} = 2i_x + 4 = -4V$$

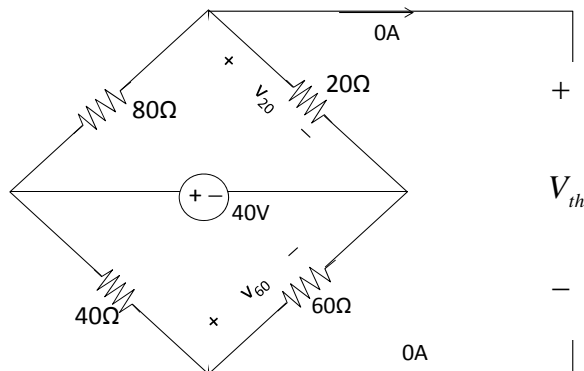


To find  $R_{th}$ , turn off 4V,  
Supply 1A,  $R_{th} = v_0/1$   
 $v_0 = 1 + v_2$   
Use mesh analysis to find  $v_2$

Assign current  $I$ . Then  $i_x = I + 1$   
By KVL along left mesh:  
 $2I + 2(I + 1) - 3(I + 1) = 0$ ;  
 $I = 1A$ ;  $i_x = 2A$   
 $v_2 = 2i_x = 4V$ ,  $v_0 = 1 + 4 = 5V$   
 $R_{th} = 5\Omega$ ;

The maximum power is delivered when  $R = 5\Omega$ . The maximum power is  
 $p_{max} = V_{th}^2 / (4R_{th}) = 16/20 = 0.8W$

Practice 6: Find the unknown  $R_L$  so that maximum power is delivered. Also find the maximum power.



$$V_{th} = v_{20} - v_{60}$$

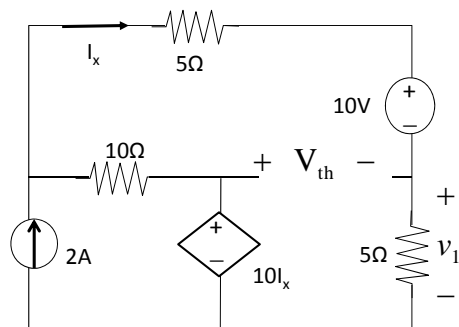
By voltage division,  $v_{20} = (20/100) \times 40 = 8V$ ,  $v_{60} = (60/100) \times 40 = 24V$   
 $V_{th} = 8 - 24 = -16V$

For  $R_{th}$ , turn off 40V with short circuit. Then  $R_{th} = 20 // 80 + 40 // 60 = 16 + 24 = 40\Omega$

The maximum power is delivered when  $R_L = R_{th} = 40\Omega$ ,

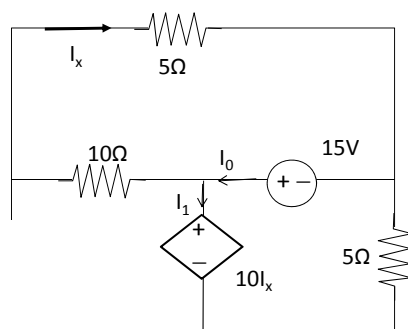
$$p_{max} = \frac{(-16)(-16)}{4 \times 40} = 1.6W$$

Practice 7: Find the unknown  $R$  so that maximum power is delivered. Also find the maximum power.



$V_{th} = 10I_x - v_1 = 10I_x - 5I_x = 5I_x$ . Use mesh analysis to find  $I_x$ .  
 By KVL,  $5I_x + 10 + 5I_x - 10I_x + 10(I_x - 2) = 0$ ,  $I_x = 1A$ ;  
 $V_{th} = 5I_x = 5V$ .

To find  $R_{th}$ , turn off 2A, 10V and supply  $v_0 = 15V$ . Then  $R_{th} = 15/I_0$



$$I_x = 15 / (10 + 5) = 1A;$$

$$I_1 = (15 - 10I_x) / 5 = 1A$$

$$I_0 = I_1 + I_x = 2A$$

$$R_{th} = 15 / 2 = 7.5\Omega$$

The maximum power is delivered when  
 $R = 7.5\Omega$ ;  
 $P_{max} = 5^2 / (4 \times 7.5) = 5/6W$