

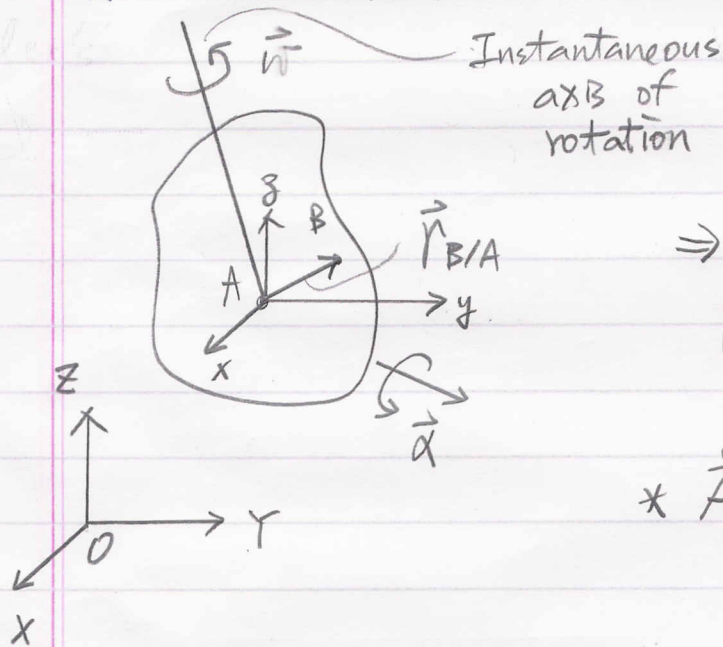
* Angular acceleration:

$$\vec{\alpha} = \frac{d\vec{\omega}}{dt} = \dot{\vec{\omega}} = \ddot{\theta}$$

* Linear velocity: $\vec{v} = \vec{\omega} \times \vec{r}$

* Linear acceleration: $\vec{a} = \vec{\alpha} \times \vec{r} + \vec{\omega} \times (\vec{\omega} \times \vec{r})$

General motion



$$\vec{v}_B = \vec{v}_A + \vec{\omega} \times \vec{r}_{B/A}$$

$$\Rightarrow \vec{a}_B = \vec{a}_A + \vec{\alpha} \times \vec{r}_{B/A} + \vec{\omega} \times (\vec{\omega} \times \vec{r}_{B/A})$$

$$* \dot{\vec{A}} = (\dot{\vec{A}})_{xyz} + \vec{\Omega} \times \vec{A}$$

* $\vec{\omega} = \vec{\omega}_s + \vec{\omega}_p \Rightarrow$ measured from the absolute coord. sys. (X, Y, Z)

$\vec{\omega}_p \Rightarrow$ measured from the relative coord. sys. $\Rightarrow \vec{\Omega} = \vec{\omega}_p$

$$\dot{\vec{\omega}}_s = (\dot{\vec{\omega}}_s)_{xyz} + \vec{\omega}_p \times \vec{\omega}_s$$

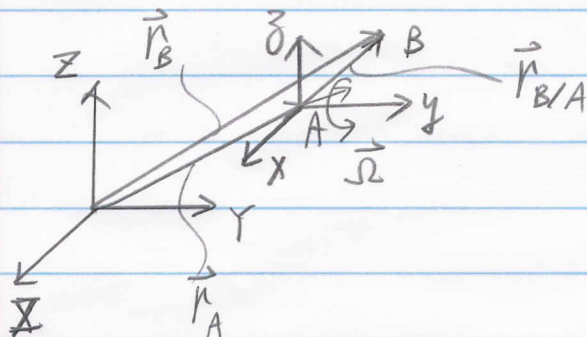
$$\dot{\vec{\omega}}_p = (\dot{\vec{\omega}}_p)_{xyz} + \vec{\omega}_p \times \vec{\omega}_p$$

$$\Rightarrow \vec{\alpha} = \dot{\vec{\omega}} = \dot{\vec{\omega}}_s + \dot{\vec{\omega}}_p$$

Relative-Motion Analysis Using Translating and Rotating Axes

* Position =

$$\vec{r}_B = \vec{r}_A + \vec{r}_{B/A}$$



* Velocity =

$$\vec{v}_B = \vec{v}_A + \vec{\Omega} \times \vec{r}_{B/A} + (\vec{v}_{B/A})_{xyz}$$

* Acceleration =

$$\begin{aligned} \vec{a}_B = \vec{a}_A + \dot{\vec{\Omega}} \times \vec{r}_{B/A} + \vec{\Omega} \times (\vec{\Omega} \times \vec{r}_{B/A}) \\ + 2\vec{\Omega} \times (\vec{v}_{B/A})_{xyz} + (\vec{a}_{B/A})_{xyz} \end{aligned}$$