

1. (30%) A lossless  $100\text{-}\Omega$  line  $\lambda/8$  is terminated in an unknown impedance. If the input impedance is  $Z_{in} = -j25\text{-}\Omega$ . Find the load  $Z_L$ .

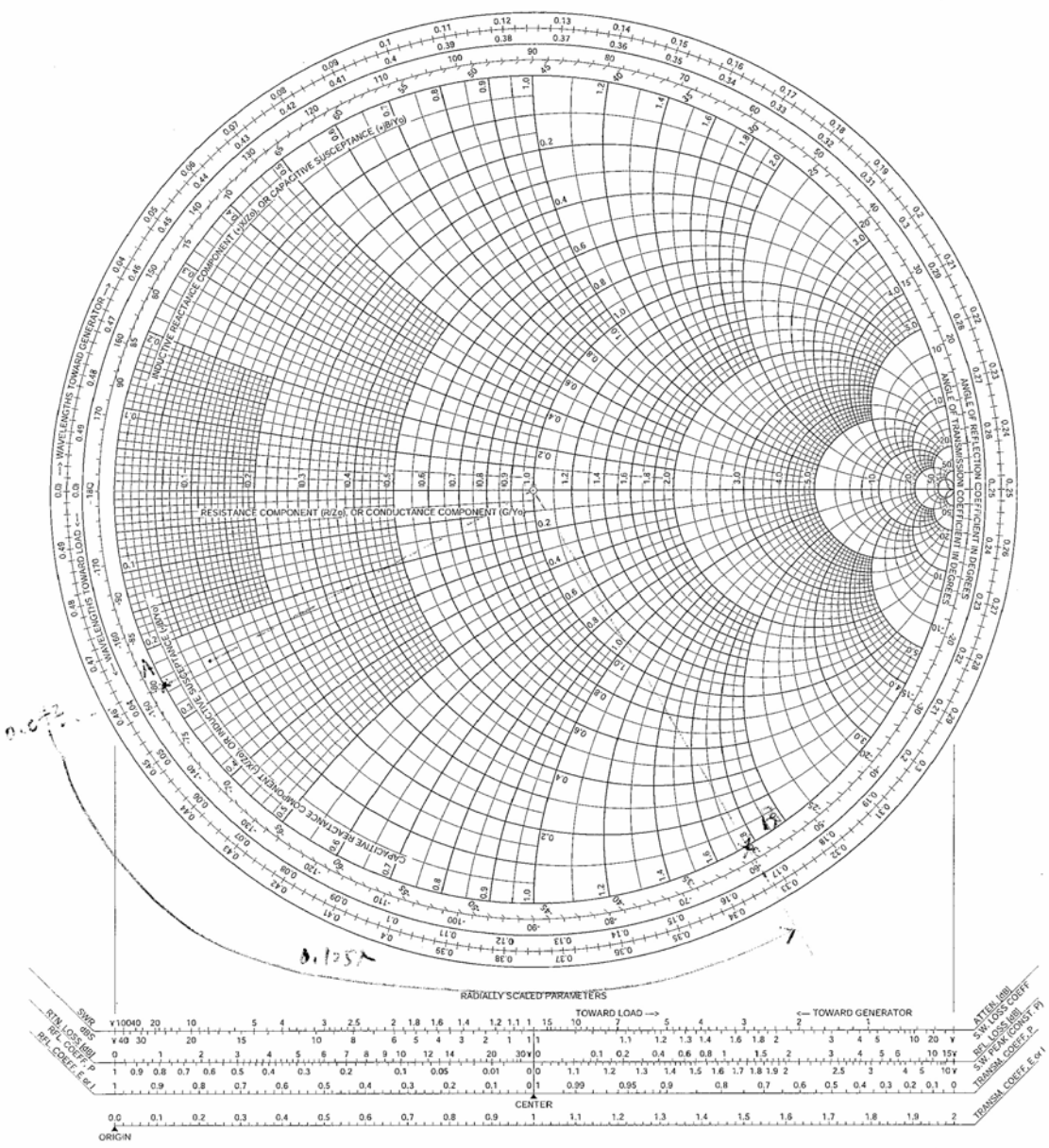
$$Z_{in} = \frac{Z_{in}}{Z_0} = -j0.25 \quad \text{point A}$$

0.042 on WTL scale:

$Z_L$  should be  $0.042\lambda + 0.125\lambda = 0.167\lambda$   
on WTL scale, point B.

$$Z_L = -j1.75$$

$$Z_L = Z_0 \cdot Z_L = -j175\Omega$$



2. (35%) On a lossless  $50\text{-}\Omega$  transmission line terminated with a  $Z_L = 120 + j100\ \Omega$ . If this transmission line is to be matched to the load using a shorted load stub. Determine the stub length and distance between the load and stub. Two possible answers. You only need to show one of them.

$$Z_L = \frac{Z_L}{Z_0} = 2.4 + j2 \quad \text{point A}$$

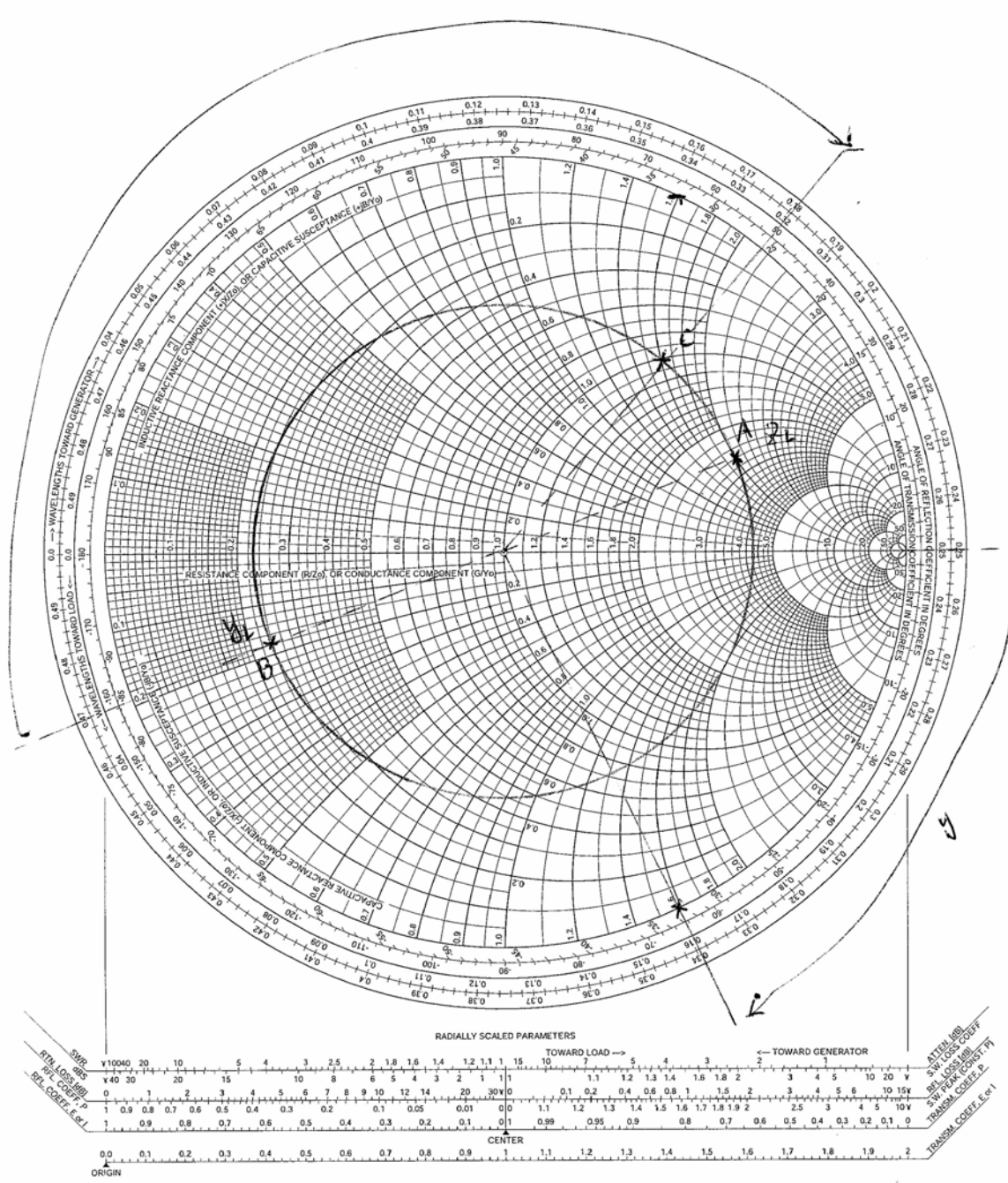
$Y_L$  is at point B.

SWR circle and  $\Gamma_r = 1$  circle, point C

distance between the load & stub

$$d = 0.18\lambda + 0.5\lambda - 0.47\lambda = 0.21\lambda$$

$$L = 0.34 - 0.25\lambda = 0.09\lambda$$



3. (35%) On a lossless transmission line with characteristic impedance  $Z_0 = 50\text{-}\Omega$ , the following observation was noted: (1) distance of the first voltage minimum from the load is 4cm; (2) distance from the first voltage maximum from the load is 9cm; (3)  $S=2$ . Find  $Z_L$ .

$$\frac{\lambda}{4} = 9\text{ cm} - 4\text{ cm} = 5\text{ cm} \quad \Rightarrow \quad \lambda = 20\text{ cm}$$

distance from load to the first  $V_{\max} = 9$

$$= \frac{9}{20} = 0.45\lambda$$

$$Z_L = 1.6 - j0.7$$

$$Z_L = 50 \cdot Z_L = 80 - j35\Omega$$

0.451

