

1.(a) (15%) For a wave with frequency $f = 1\text{MHz}$, the amplitude phasor at different position z can be written as: $\tilde{A}(z) = 5e^{-j100z}$, what is the instantaneous value of the amplitude $A(z,t)$ at different position z ? What's the ^{direction} direct the wave travels?

$$A(z,t) = \text{Re} \left[\hat{A}(z) e^{j\omega t} \right] = \text{Re} \left[5e^{-j100z} \cdot e^{j2\pi f t} \right]$$

$$= \text{Re} \left[e^{j(2\pi f t - 100z)} \right]$$

$$= \cos(2\pi f t - 100z)$$

it Travels along ^{the} z direction.

1.(b) (30%) A 10GHz voltage source is connected to a lossless transmission line is terminated with $Z_L = j25\text{-}\Omega$. The characteristic impedance of the transmission line is $50\text{-}\Omega$. Assuming the phase velocity of the transmission line is $0.8c$, where c is the speed of light. (1) Find out the location of the first $|V|_{\max}$ from the load, (2) What's the standing wave ratio S ? (3) how long the transmission line will make it equivalent to a short circuit?

$$(1) \quad 0.8c = f \cdot \lambda \quad \Rightarrow \quad \lambda = \frac{0.8c}{f} = \frac{0.8 \times 3 \times 10^8}{10 \times 10^9}$$

$$\lambda = 2.4 \text{ cm}$$

$$\text{normalized load } Z_L = \frac{Z_L}{Z_0} = 0.5j$$

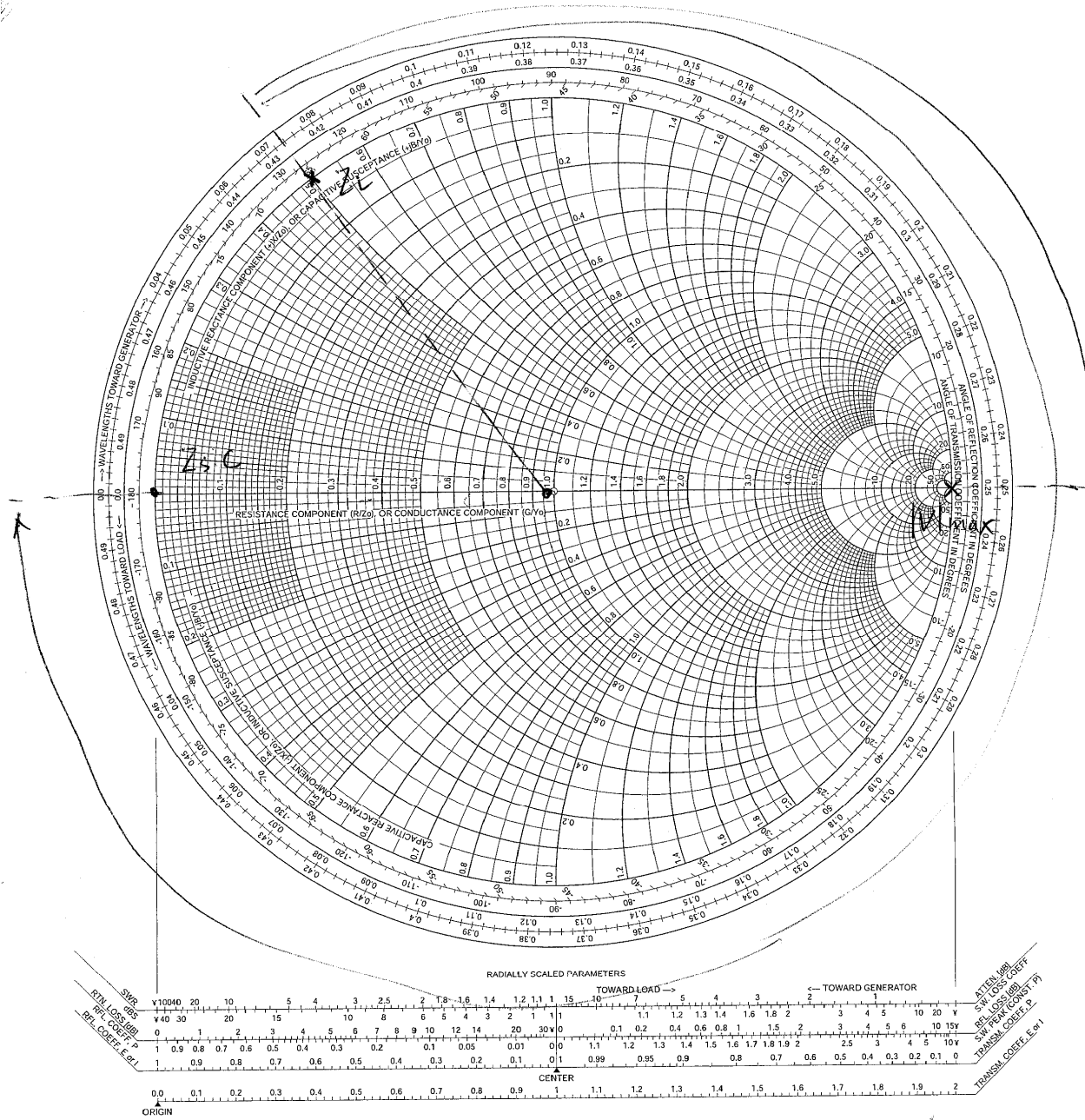
distance between $|V|_{\max}$ and the Z_L is :

$$0.25\lambda - 0.072\lambda = 0.178\lambda = 0.427 \text{ cm}$$

$$(2) \quad S = \infty$$

(3) length of the transmission line is :

$$0.5\lambda - 0.072\lambda = \overset{0.428\lambda}{\cancel{0.428\lambda}} = 1.027 \text{ cm}$$



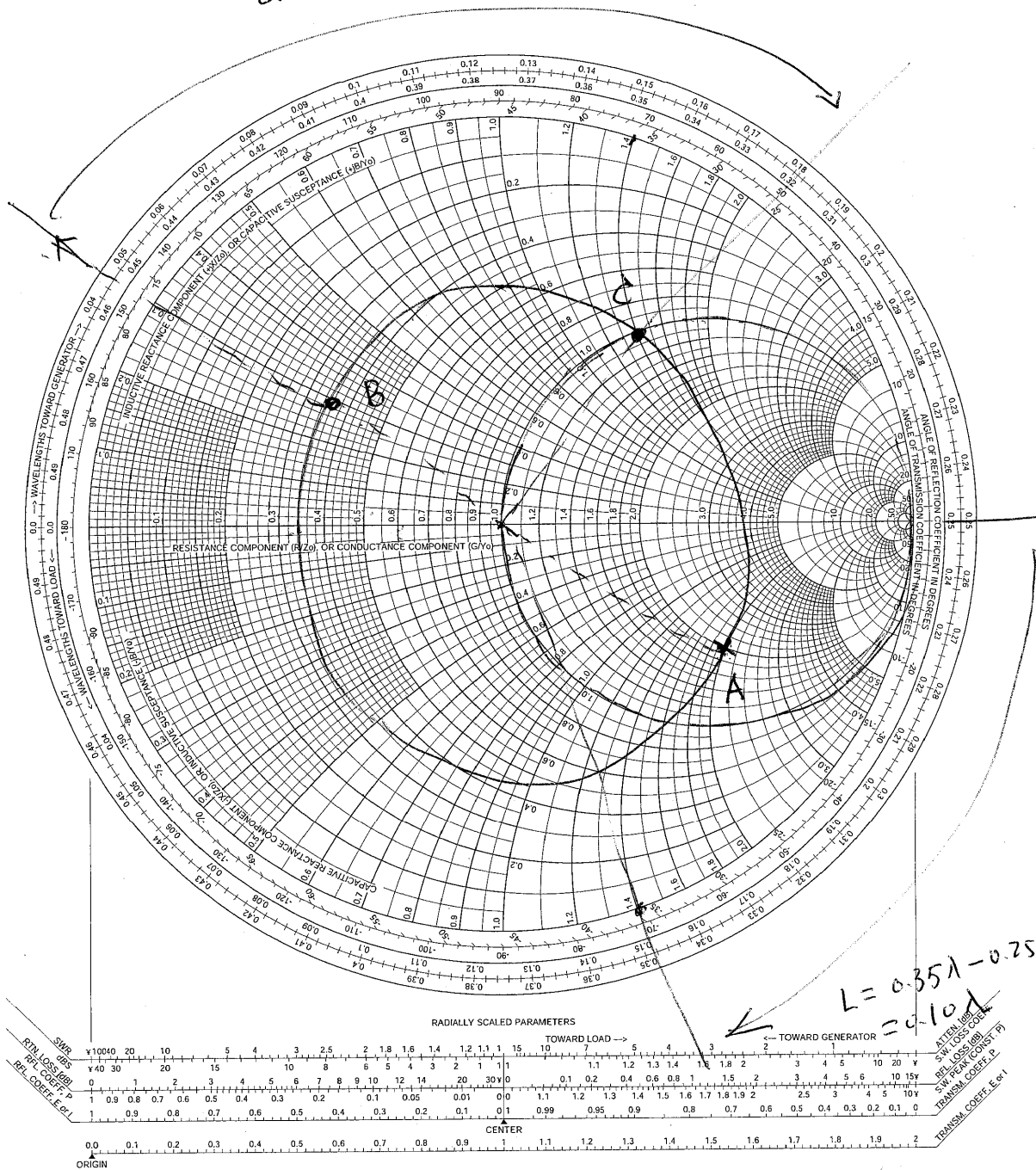
2. (30%) On a lossless $50\text{-}\Omega$ transmission line terminated with a $Z_L = 100 - j100\ \Omega$. If this transmission line is to be matched to the load using a shorted load stub. Determine the stub length and distance between the load and stub. Two possible answers. You only need to show one of them.

1. normalized load $Z_L = \frac{Z_L}{Z_0} = 2 - j2$

point A on the Smith chart.

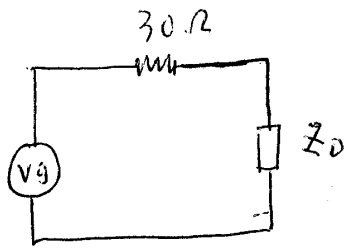
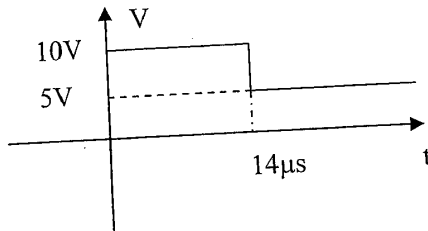
the admittance is at point B

$$d = 0.18\lambda - 0.043\lambda = 0.136\lambda$$



$$L = 0.35\lambda - 0.25\lambda = 0.10\lambda$$

3. (25%) A time domain reflector is an instrument to locate faults on a transmission line. A voltage meter is connected to beginning of a $50\text{-}\Omega$ lossless matched transmission line, and the measured voltage waveform is shown in following figure. The line insulating material is Teflon with $\epsilon_r = 2.0$. If we know that the resistance of the generator is $30\text{-}\Omega$, determine: (a) the magnitude of the generator voltage, and (b) the location of the fault.



$$(a) \quad 10 \text{ V} = V_g \frac{Z_0}{30 + Z_0}$$

$$\Rightarrow V_g = 16 \text{ (V)}$$

$$(b) \quad \frac{2L}{v} = 14 \mu\text{s}$$

$$\Rightarrow L = 7 \mu\text{s} \cdot v = 7 \times 10^{-6} \times \frac{c}{\sqrt{\epsilon_r}}$$

$$= 1.5 \times 10^3 \text{ (m)}$$