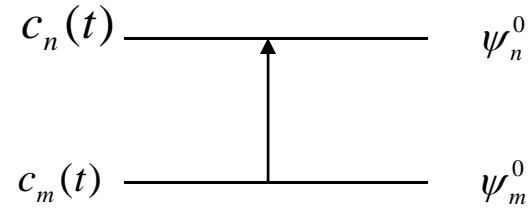


Discussion of Fermi golden rule

$$w_{nm} = \frac{2\pi}{\hbar} |W_{nm}|^2 \delta(E_n^0 - E_m^0 - \hbar\omega)$$

$$|W_{n,m}|^2 = A_0^2 |\langle n | D | m \rangle|^2 = A_0^2 |\langle n | -er | m \rangle|^2$$

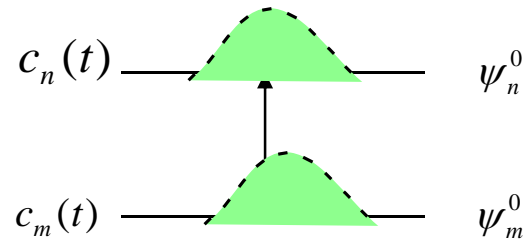


Energy conservation

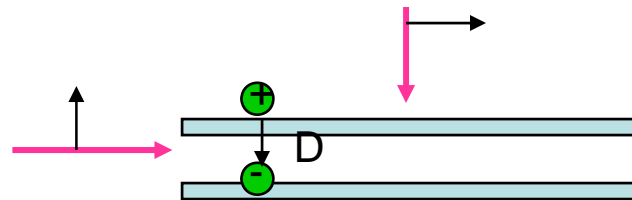
$$\delta(E_n^0 - E_m^0 - \hbar\omega)$$

Selection rules

Wavefunction overlap



Polarization selection rule



$$W = \frac{2\pi}{\hbar} \left| \langle \psi_m^0 | V_0 | \psi_n^0 \rangle \right|^2 \rho(\hbar\omega)$$

Fermi-Golden rule

$$W_{nm} = \frac{2\pi}{\hbar} \left| \langle \psi_m^0 | V_0 | \psi_n^0 \rangle \right|^2 \delta(E_m - E_n - \hbar\omega)$$

Fermi-Golden rule

Absorption coefficient

$$\alpha = -\frac{dI}{I dx}$$

$$\alpha = -\frac{1}{I} \frac{dI}{dt} \frac{dx}{dt} = \frac{1}{I_0} W c_r$$

Small absorption approximation

In semiconductors

$$W_{c \leftarrow v} = \frac{2\pi}{\hbar} \left| \langle \psi_c^0 | H' | \psi_v^0 \rangle \right|^2 \rho(\hbar\omega) (1 - f_c) f_v$$

$$\alpha_{c \leftarrow v} = \frac{c_r}{I_0} W_{c \leftarrow v} = \frac{c_r}{I_0} \frac{2\pi}{\hbar} \left| \langle \psi_c^0 | H' | \psi_v^0 \rangle \right|^2 \rho_{red}(\hbar\omega) (1 - f_c) f_v$$

$$f_c = \frac{1}{e^{(E_c - E_{Fc})/kT} + 1} \quad f_v = \frac{1}{e^{(E_v - E_{Fv})/kT} + 1}$$

$$\rho_{red}(\hbar\omega) = \left( \frac{2m_r}{\hbar^2} \right)^{3/2} (\hbar\omega - E_g)$$

$$\frac{dI_V}{dx} = \frac{n}{c} \Delta x h\nu \cdot B_{21} \rho_{ph}(h\nu) \text{Pred} [f_n(E_2) - f_p(E_2 - h\nu)]$$

$$= \frac{n}{c} h\nu B_{21} \cdot \frac{dI_V}{dx} \cdot \text{Pred} [f_n(E) - f_p(E - h\nu)]$$

$$\Rightarrow g = B_{21} \cdot \frac{n}{c} h\nu \cdot \text{Pred}(h\nu) [f_n(E) - f_p(E - h\nu)]$$

• injection current level to reach threshold.

$$\rightarrow n = n_0 e^{qV/kT}, \quad V = E_{FA} - E_{FP}$$

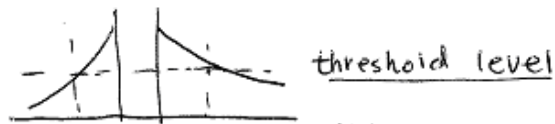
•  $\Rightarrow$  minority carrier concentration.

$$n_p \geq n_{p0} e^{qE_g/kT}, \quad \text{build-in-potential } V_0 = E_g + \frac{kT}{q} \ln \frac{N_A N_D}{N_C N_V}$$

injection current

$$J = J_n + J_p$$

$$= q \left( \frac{D_n n_p}{L_n} + \frac{D_p p_n}{L_p} \right) [e^{qV/kT} - 1]$$



$$J_n(x) = J_n(0) e^{-x/L_n}$$

$$J_p(x) = J_p(0) e^{-x/L_p}$$

hw: 4.4, 4.5, 4.6, 4.8, 4.9

Considering stimulated emission, the net emission rate:

$$W_{c \rightarrow v} - W_{c \leftarrow v} = \frac{2\pi}{\hbar} \left| \langle \psi_c^0 | H' | \psi_v^0 \rangle \right|^2 \rho_{red}(\hbar\omega) [f_v(1 - f_v) - (1 - f_c)]$$

Gain coefficient

$$G = \frac{c_r}{I_0} (W_{c \rightarrow v} - W_{c \leftarrow v}) = \frac{c_r}{I_0} \frac{2\pi}{\hbar} \left| \langle \psi_c^0 | H' | \psi_v^0 \rangle \right|^2 \rho_{red}(\hbar\omega) [f_c - f_v]$$

$$G \geq 0 \quad E_{fc} - E_{fv} > E_c - E_v$$

Gain

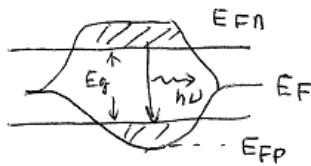
$$R_{st}^{21} > G_{12} \Rightarrow f_n(E_2) \cdot (1 - f_p(E_1)) > [f_n(E_1)] \cdot f_p(E_2)$$

$$\Rightarrow \left[ \frac{1}{e^{(E_2 - E_{Fn})/kT} + 1} \right] \left[ 1 - \frac{1}{e^{(E_1 - E_{Fp})/kT} + 1} \right]$$

$$> \frac{1}{e^{(E_1 - E_{Fp})/kT} + 1} \cdot \left[ 1 - \frac{1}{e^{(E_2 - E_{Fn})/kT} + 1} \right]$$

$$\Rightarrow e^{-(E_2 - E_{Fn})/kT} \cdot e^{-(E_{Fp} - E_1)/kT}$$

$$E_{Fn} - E_{Fp} > E_2 - E_1 \cong E_g$$

Gain coefficient in semiconductor

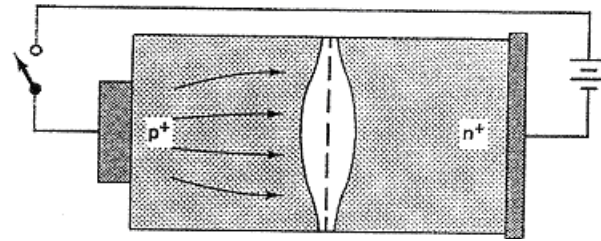
$$\frac{dN_{ph}}{dt} = B_{12} (N_2 - N_1) P_{ph}(h\nu) \leftarrow \text{two level system}$$

in semiconductor:

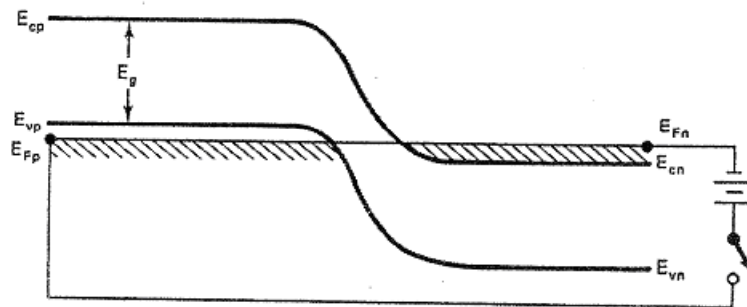
$$I_{\nu} \leftarrow \text{optical power, } \frac{\text{energy}}{\text{unit area} \cdot \text{sec}}$$

$$\frac{dI_{\nu}}{dt} = \frac{h\nu}{\cancel{dt}} \frac{dN_{ph}}{dt} (dx)$$

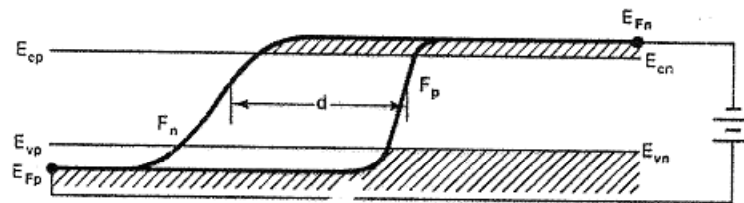
$$\frac{dI_{\nu}}{dx} = \frac{dI_{\nu}}{dt} \cdot \frac{dt}{dx} = \frac{nc}{c} \cdot \frac{h\nu}{\cancel{dt}} \frac{dN_{ph}}{dt} \cdot \Delta x$$



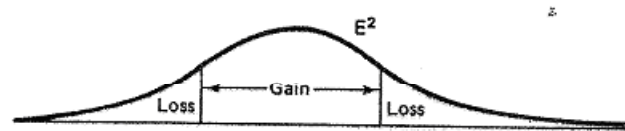
(a)



(b)



(c)



(d)

if  $r_1 = r_2 = R^{1/2}$

$$I = I_0 \frac{1}{(1-R)^2 + 4R \sin^2 \beta L}$$

Maximum:  $\beta L = m\pi$ ,  $I = \frac{I_0}{(1-R)^2}$  ↗ resonant condition

Minimum:  $\beta L = m\pi + \frac{\pi}{2}$ ,  $I = \frac{I_0}{(1+R)^2}$

$$I = \frac{I_0}{(1-R)^2 + 4R \sin^2 \beta L}$$

$$= \frac{I_0 / (1-R)^2}{1 + \frac{4R}{(1-R)^2} \sin^2 \beta L}$$

$$F \equiv \frac{\pi R^{1/2}}{1-R} \quad \Rightarrow \quad I = \frac{I_0 / (1-R)^2}{1 + \frac{4F^2}{\pi^2} \sin^2 \beta L \cdot n} = \frac{I_0 / (1-R)^2}{1 + \left(\frac{2F}{\pi} \sin \beta L n\right)^2}$$

When  $\frac{2F}{\pi} \sin \beta L = 1$ ,  $I = I_{\max} \cdot \left(\frac{1}{2}\right)$

$$\Delta \beta n L = \left(\frac{\pi}{2}\right) \cdot (F)^{-1} = \frac{\pi}{2F}$$

$$\Delta \left(\frac{2\pi}{\lambda}\right) \cdot n L = \frac{\pi}{2F}$$

$$\Delta \left(\frac{1}{\lambda}\right) = \frac{1}{4F} \cdot \frac{1}{nL} = \frac{1}{2F} - \frac{1}{2nL}$$

$$\Rightarrow \Delta \omega = \frac{1}{2F} \cdot \left(\frac{c}{2nL}\right), \quad \Delta \lambda = \frac{1}{2F} \cdot \left(\frac{\lambda^2}{2nL}\right)$$

↑  
spectrum width.



Example : For a cavity of 1mm long, calculate the R needed for a spectral width of 30 kHz

Longitude mode separation  $\Delta\nu_m = 150\text{GHz}$

$$\Rightarrow 2F = \frac{150\text{GHz}}{30\text{kHz}} = 5 \times 10^6 = \frac{2\pi \cdot R^2}{L \cdot R}$$

$$\Rightarrow R = 99.9999\%$$

## 4. Quantum Well Lasers

1). density of states



Quantum effect.

$$k_z = \frac{2\pi}{a} n$$

$$E = \frac{\hbar^2(k_x^2 + k_y^2)}{2m} + \frac{\hbar^2}{2m} k_z^2$$

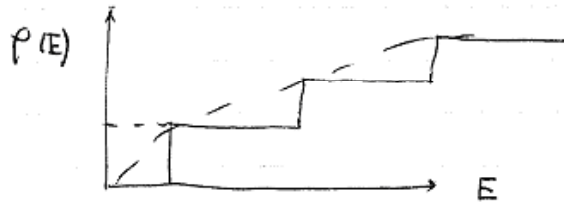
$$= \frac{\hbar^2}{2m} \left( k_x^2 + k_y^2 + \left(\frac{2\pi}{a}\right)^2 n^2 \right)$$

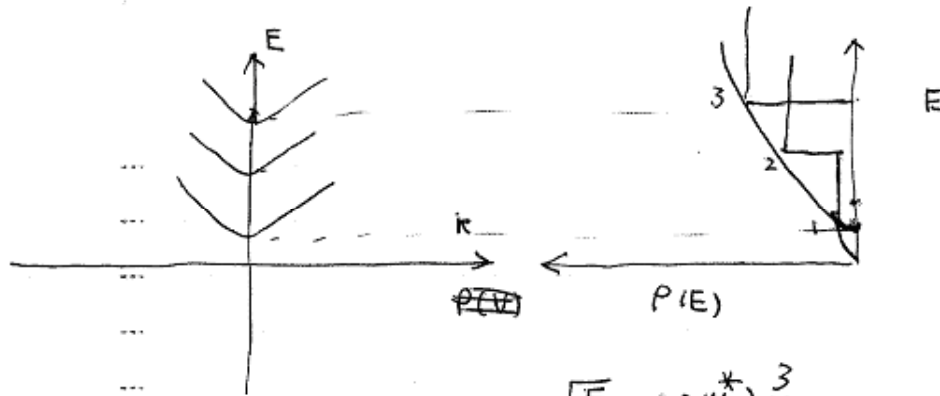
# of states available  $k \rightarrow k + dk$  $k_x, k_y + dk_x, dk_y, k_z$ 

$$\# \text{ of states available } N = \frac{\left(\frac{2\pi}{a}\right) 2\pi k_x k_y \cdot dk_x dk_y}{\left(\frac{2\pi}{a}\right) \cdot \left(\frac{2\pi}{L_x}\right) \left(\frac{2\pi}{L_y}\right) S} = P(E) dE$$

 $\Rightarrow$   $N$  of states available per unit ~~volume~~ <sup>area</sup>
@ a specific  $E \rightarrow \Delta E + E$ 

$$P(E) dE = \left(\frac{2\pi}{a}\right) \cdot \frac{2M^*}{\hbar^2 a} dE = \frac{M^*}{2\hbar^2 \pi a} dE$$





$$P(E)|_{\text{bulk}} = \frac{\sqrt{E}}{4\pi^2} \left( \frac{2m^*}{\hbar^2} \right)^{\frac{3}{2}} = P(E)|_{\text{well}} \frac{a}{2\pi} \sqrt{k_x^2 + k_y^2 + \frac{2\pi^2}{a^2}}$$

$$P(E)|_{\text{well}} = \frac{m^*}{2\pi\hbar^2} \left( \frac{1}{a} \right)$$

... Reduced density of states for optical transition.

$$P_{\text{red}}(E)|_{\text{Q.W.}} = \frac{m^*}{2\pi\hbar^2} \left( \frac{1}{a} \right) (h\nu - E_g)$$

... Note: 1) in Q.W. Less injection current needed to reach a energy level  $\leftarrow$  Low threshold.

... 2)  $P_{\text{red}}(h\nu)|_{\text{Q.W.}}$  depends on well thickness

2). density of states & reduced density of states in Quantum Dots.



discrete energy level.

$$E = \left(\frac{2\pi}{L_x} n_x\right)^2 + \left(\frac{2\pi}{L_y} n_y\right)^2 + \left(\frac{2\pi}{L_z} n_z\right)^2$$

$$f(E) dE = \delta(E - E_{\text{level}}) N / V_0$$

$\frac{N}{V_0}$  ← Numbers of QDs per unit volume.

Example: calculate reduced density of state in a 100 Å GaAs Quantum Well

$$f_{\text{red}}(E) = \frac{m_r^*}{\pi^2 L_z} = 2 \times 10^{19} \text{ (eV)}^{-1} \cdot \text{cm}^{-3}$$

3). Multi-Quantum Well (MQW).

$\Gamma$  ← confinement factor.



optical field

$$\Gamma = \frac{a}{d}$$

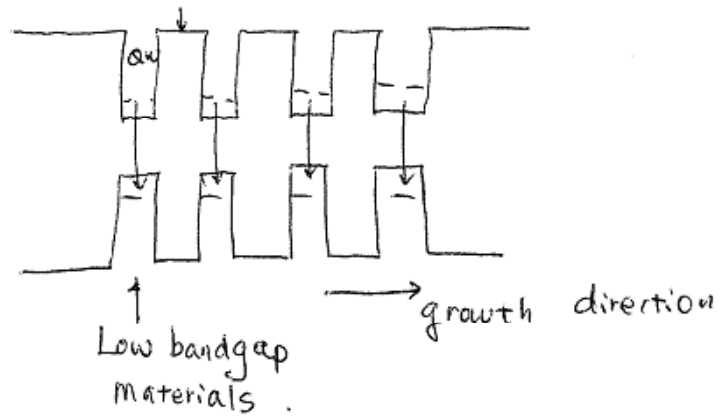
$a$  ← QW width  
 $d$  ← optical beam width.  
 ↑  
 waveguide size.

For single QW,  $\Gamma$  is small  $\sim \frac{100 \text{ \AA}}{1 \mu\text{m}} = 10^{-2}$ .

⇒ optical beam not effectively amplified.

MQW,  $\Gamma_{\text{MQW}} = n \Gamma_{\text{single}}$

4). Band diagram of MQW  
wide bandgap materials



Example

- ... consider GaAs QW.  $m_e^* = 0.07m_e$ .  
 ... Calculate 1). first two electron energy levels for  
 ... QW thickness = 10nm, 2). hole energy below  $E_v$   
 ...  $m_h^* = 0.50m_e$ . 3). Change of emission wavelength  
 ... ~~for~~ compared with bulk GaAs  $E_g = 1.42\text{ eV}$

... solution: 1). 
$$\epsilon_n = \frac{(\pi \hbar)^2}{2m_e^*} = \frac{\hbar^2}{2m_e^*} \left(\frac{2\pi n}{d}\right)^2$$

$$= \frac{\hbar^2 \cdot n^2}{8m_e^* d^2} = \begin{cases} 0.0537\text{ eV}, & n=1 \\ 0.215\text{ eV}, & n=2 \end{cases}$$

2). 
$$\epsilon_v = \frac{\hbar^2 n^2}{8m_h^* d^2} = 0.0075\text{ eV}.$$

... much smaller than conduction band

... 3). QW. emission wavelength

$$\lambda_{\text{QW}} = \frac{hc}{E_g + \epsilon_1 + \epsilon_1'} = 839\text{ nm}$$

... bulk emission wavelength

$$\lambda_{\text{bulk}} = \frac{hc}{E_g} = 874\text{ nm}.$$

Example

- ... Consider GaAs QW.  $m_e^* = 0.07m_e$ .  
 ... Calculate 1) first two electron energy levels for  
 ... QW thickness = 10nm, 2) hole energy below  $E_v$   
 ...  $m_h^* = 0.50m_e$ . 3) Change of emission wavelength  
 ... ~~for~~ compared with bulk GaAs  $E_g = 1.42\text{ eV}$   
 ...

... Solution:

$$1). \quad \epsilon_n = \frac{(\hbar k)^2}{2m_e^*} = \frac{\hbar^2}{2m_e^*} \left(\frac{2\pi n}{d}\right)^2$$

$$= \frac{\hbar^2 \cdot n^2}{8m_e^* d^2} = \begin{cases} 0.0537 \text{ eV}, & n=1 \\ 0.215 \text{ eV}, & n=2 \end{cases}$$

$$2). \quad \epsilon_v = \frac{\hbar^2 n^2}{8m_h^* d^2} = 0.0075 \text{ eV}.$$

... much smaller than conduction band  
 ...

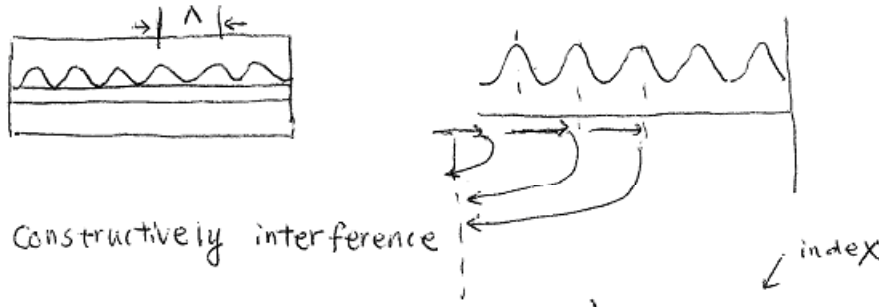
... 3) QW. emission wavelength

$$\lambda_{\text{QW}} = \frac{hc}{E_g + \epsilon_1 + \epsilon_1'} = 839 \text{ nm}$$

... bulk emission wavelength

$$\lambda_{\text{bulk}} = \frac{hc}{E_g} = 874 \text{ nm}.$$

5. distribute feedback Laser (DFB Laser)



$$2\Delta n \neq \pi \Rightarrow 2\Delta n$$

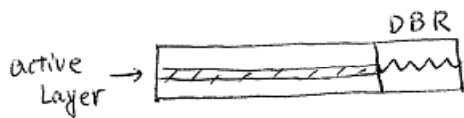
$$m \cdot \lambda = 2\Lambda n$$

$$\Lambda = \frac{m\lambda}{2n} \leftarrow \text{period, } m \text{ is the order of Grating}$$

$$\Rightarrow \Delta \lambda_m = \frac{\lambda_B^2}{2nL}$$

$$\lambda_m = \lambda_B \pm \frac{\lambda_B^2}{2nL} (m+1), \quad m=0, 1, 2, \dots$$

Distribute Bragg reflector ~~mirror~~ (DBR)



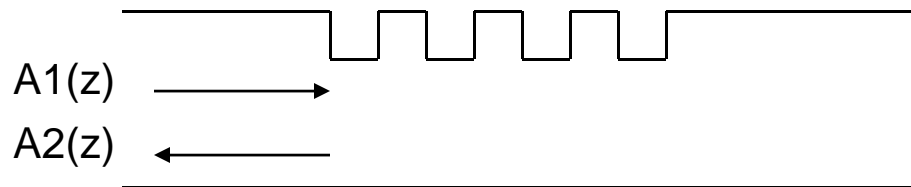
6. Cleaved - coupled - cavity (C<sup>3</sup>).



cavity mode



## Waveguide gratings



$$\frac{dA_1(z)}{dz} = i\kappa A_2(z)$$

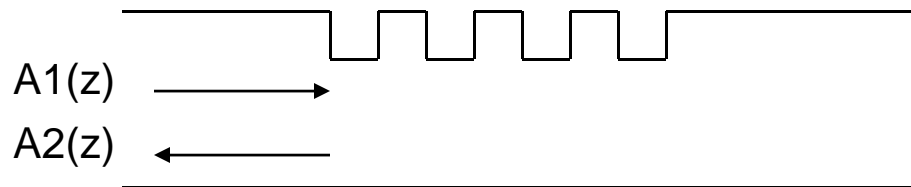
$$\frac{dA_2(z)}{dz} = -i\kappa A_1(z)$$

$$\begin{aligned} \frac{d|A_1(z)|^2}{dz} &= A_1^*(z) \frac{dA_1(z)}{dz} + A_1(z) \frac{dA_1^*(z)}{dz} \\ &= A_1^*(z) i\kappa A_2(z) + A_1(z) (-i\kappa A_2^*(z)) \end{aligned}$$

$$\begin{aligned} \frac{d|A_2(z)|^2}{dz} &= A_2^*(z) \frac{dA_2(z)}{dz} + A_2(z) \frac{dA_2^*(z)}{dz} \\ &= A_2^*(z) (-i\kappa A_1(z)) + A_2(z) (i\kappa A_1^*(z)) \end{aligned}$$

$$\frac{d}{dz} \left( |A_1(z)|^2 - |A_2(z)|^2 \right) = 0$$

## Waveguide gratings



$$\frac{dA_1(z)}{dz} = i\kappa A_2(z)$$

$$\frac{dA_2(z)}{dz} = -i\kappa A_1(z)$$

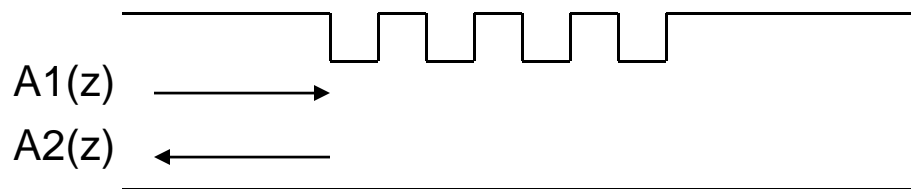
$$\frac{d^2 A_1(z)}{dz^2} = i\kappa \frac{d}{dz} A_2(z) = \kappa^2 A_1(z)$$

$$A_1(z) = A \cosh(\kappa z) + B \sinh(-\kappa z)$$

$$A_2(z) = C \cosh(\kappa z) + D \sinh(-\kappa z)$$

A, B, C, D are determined by the initial conditions

## Waveguide gratings



$$A_1(z)|_{z=0} = A_1(0)$$

$$A_2(z)|_{z=L} = 0$$

$$\frac{dA_1(z)}{dz} = i\kappa A_2(z)$$

$$\frac{dA_2(z)}{dz} = -i\kappa A_1(z)$$

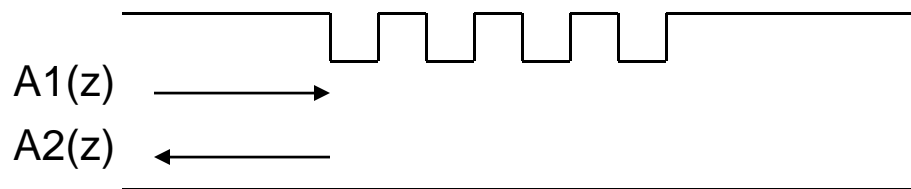
$$A_1(z) = A_1(0) \cosh(\kappa z) + B \sinh(\kappa z)$$

$$A_1(0) \sinh(\kappa L) + B \cosh(\kappa L) = 0$$

$$A_1(z) = A_1(0) \left[ \cosh(\kappa z) - \frac{\sinh(\kappa L)}{\cosh(\kappa L)} \sinh(\kappa z) \right] = A_1(0) \frac{\cosh \kappa(z-L)}{\cosh(\kappa L)}$$

$$A_2(z) = A_1(0) \frac{\sinh \kappa(z-L)}{\cosh(\kappa L)}$$

## Waveguide gratings



$$A_1(z)|_{z=0} = A_1(0)$$

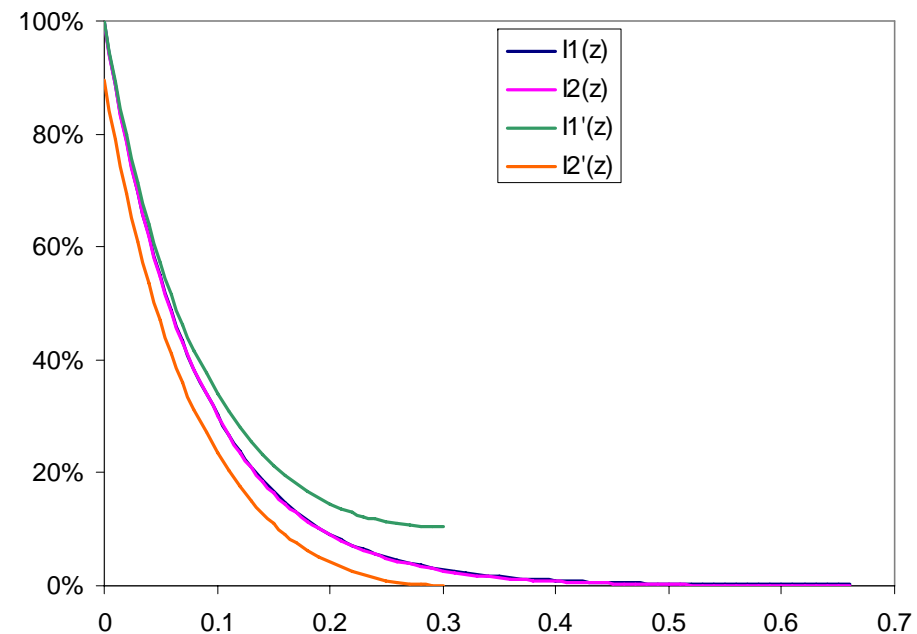
$$A_2(z)|_{z=L} = 0$$

$$\frac{dA_1(z)}{dz} = i\kappa A_2(z)$$

$$\frac{dA_2(z)}{dz} = -i\kappa A_1(z)$$

$$A_1(z) = A_1(0) \frac{\cosh \kappa(z - L)}{\cosh(\kappa L)}$$

$$A_2(z) = A_1(0) \frac{\sinh \kappa(z - L)}{\cosh(\kappa L)}$$



Example:

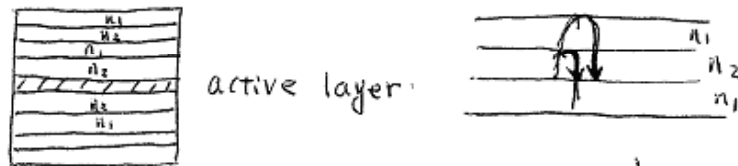
a DFB Laser has grating period  $\Lambda = 0.22 \mu\text{m}$   
and grating length of  $400 \mu\text{m}$ ,  $n = 3.5$ ; first order

Calculate  $\lambda_B$ ,  $\lambda_m$ .

$$\lambda_B = \frac{2\Lambda n}{q} = 2 \cdot 0.22 \cdot 3.5 = 1.54 \mu\text{m}$$

$$\lambda_m = \lambda_B \pm \frac{\lambda_B^2}{2n\Lambda} (m+1) \Rightarrow \lambda = \begin{cases} 1.5392 \mu\text{m} \\ 1.5408 \mu\text{m} \end{cases}$$

### I. Vertical cavity surface emitting Laser (VCSEL)



$$2n_1 d_1 = \frac{\lambda}{2}, \quad 2n_2 d_2 = \frac{\lambda}{2}$$

$$\Rightarrow d_1 = \frac{\lambda}{4n_1}, \quad d_2 = \frac{\lambda}{4n_2} \quad \leftarrow \text{Quarter Wavelength Layer.}$$

Transmission & reflectivity of DBR mirrors.

can be calculated using transmission Matrix.

- Low power output.  $\rightarrow$  short gain.
- design issue,

$$g = \alpha + \frac{1}{2L} \ln \frac{1}{R_1 R_2}$$

since  $L$  is usually very small  $\sim 1 \mu\text{m}$

$R_1$  &  $R_2$  have to be very high.  $\sim 99.99\%$ .

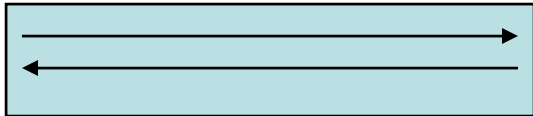
- application of VCSEL.
  - Low threshold, Low power Laser
  - Low cost.

hw # 4.11, 4.13, 4.14, 4.15, 4.16

Rate equations:

$$\left\{ \begin{array}{l} \frac{dN}{dt} = \frac{J}{qd} - \frac{N}{\tau} - \Omega(N - N_0)N_{ph} \\ \frac{dN_{ph}}{dt} = \Omega(N - N_0)N_{ph} + \frac{\theta N}{\tau_r} - \frac{N_{ph}}{\tau_{ph}} \end{array} \right. \quad \begin{array}{l} \theta \text{ Fraction of spontaneous into the specific mode} \\ \tau_{ph} \text{ Photon lifetime} \end{array}$$

$$\tau_{ph} = \frac{2n_r L}{c} \frac{1}{1 - R_1 R_2}$$



$$\frac{dN_{ph}}{dt} = -\frac{N_{ph}}{\tau_{ph}}$$

$$N_{ph}(t = \frac{2Ln_r}{c}) = N_{ph}(t = 0)e^{-\frac{t}{\tau_{ph}}} = N_{ph}(t = 0)R_1 R_2$$

$$\frac{t = \frac{2Ln_r}{c}}{\tau_{ph}} = -\ln(R_1 R_2) \quad \tau_{ph} = \frac{2Ln_r}{c \ln\left(\frac{1}{R_1 R_2}\right)} \quad \ln\left(\frac{1}{R_1 R_2}\right) \approx 1 - R_1 R_2$$

Rate equations:

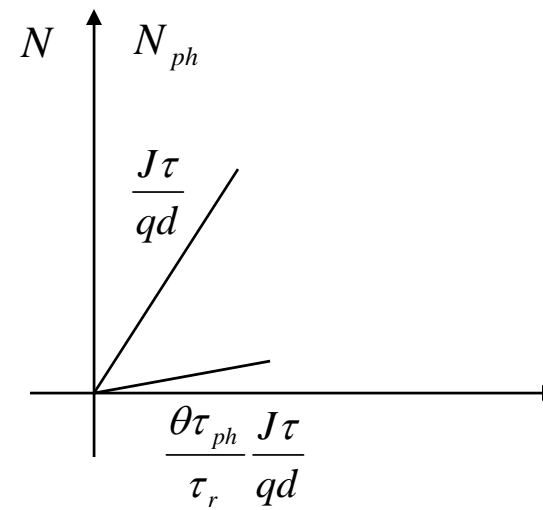
$$\left\{ \begin{array}{l} \frac{dN}{dt} = \frac{J}{qd} - \frac{N}{\tau} - \Omega(N - N_0)N_{ph} \\ \frac{dN_{ph}}{dt} = \Omega(N - N_0)N_{ph} + \frac{\theta N}{\tau_r} - \frac{N_{ph}}{\tau_{ph}} \end{array} \right. \quad \begin{array}{l} \theta \text{ Fraction of spontaneous into the specific mode} \\ \tau_{ph} \text{ Photon lifetime} \end{array}$$

Steady state:

$$\left\{ \begin{array}{l} \frac{J}{qd} = \frac{N}{\tau} + \Omega(N - N_0)N_{ph} \\ \frac{\theta N}{\tau_r} = \frac{N_{ph}}{\tau_{ph}} - \Omega(N - N_0)N_{ph} \end{array} \right.$$

Below threshold:  $N_{ph} \approx 0$

$$\left\{ \begin{array}{l} \frac{J}{qd} \approx \frac{N}{\tau} \\ \frac{N_{ph}}{\tau_{ph}} = \frac{\theta N}{\tau_r} = \frac{\theta J \tau}{\tau_r qd} \end{array} \right. \quad N_{ph} = \frac{\theta J \tau \tau_{ph}}{\tau_r qd}$$





Steady state:

$$\left\{ \begin{array}{l} \frac{J}{qd} = \frac{N}{\tau} + \Omega(N - N_0)N_{ph} \\ \frac{\theta N}{\tau_r} = \frac{N_{ph}}{\tau_{ph}} - \Omega(N - N_0)N_{ph} \end{array} \right.$$

Above threshold:

$$\frac{\theta N}{\tau_r} \ll \Omega(N - N_0)N_{ph}$$

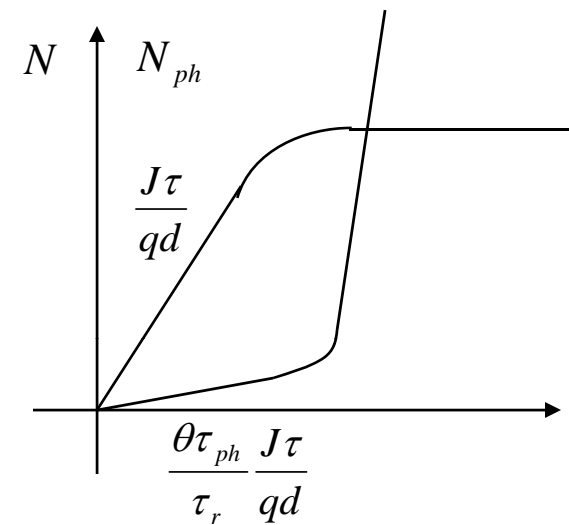
$$\left\{ \begin{array}{l} \frac{J}{qd} = \frac{N}{\tau} + \Omega(N - N_0)N_{ph} \\ \frac{N_{ph}}{\tau_{ph}} = \Omega(N - N_0)N_{ph} \end{array} \right.$$

$$\frac{J}{qd} = \frac{N}{\tau} + \frac{N_{ph}}{\tau_{ph}}$$

$$N = N_0 + \frac{1}{\tau_{ph}\Omega} = \bar{N}$$

$$N_{ph} = \frac{J\tau_{ph}}{qd} - \frac{N\tau_{ph}}{\tau} = \frac{\tau_{ph}}{qd} (J - J_{th})$$

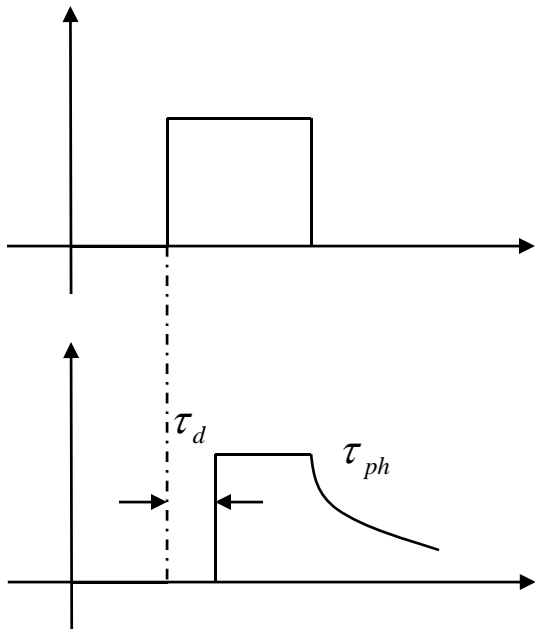
$$J_{th} = \frac{\bar{N}qd}{\tau}$$

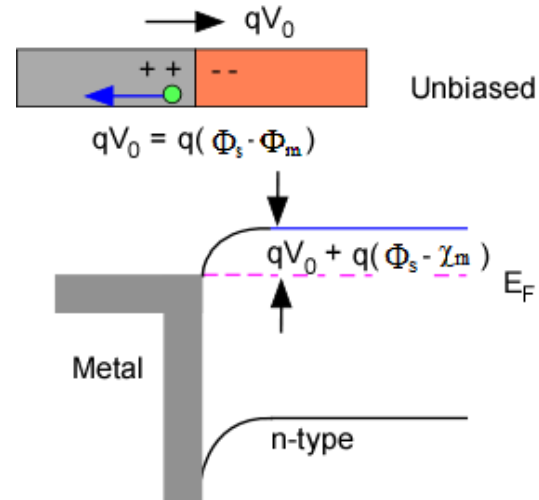
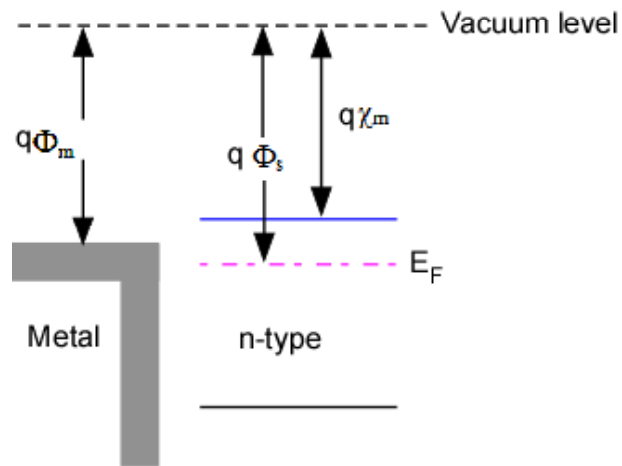


Turn-on delay

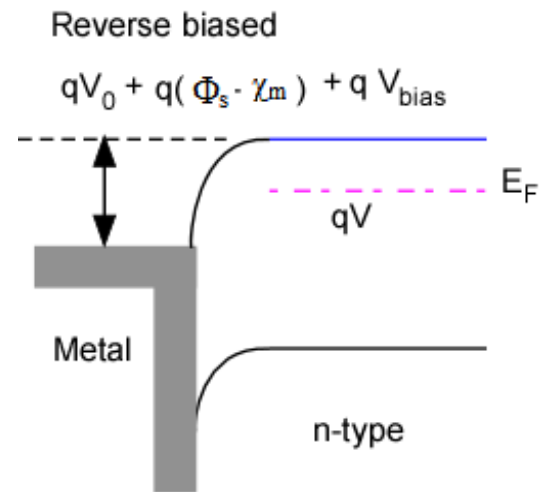
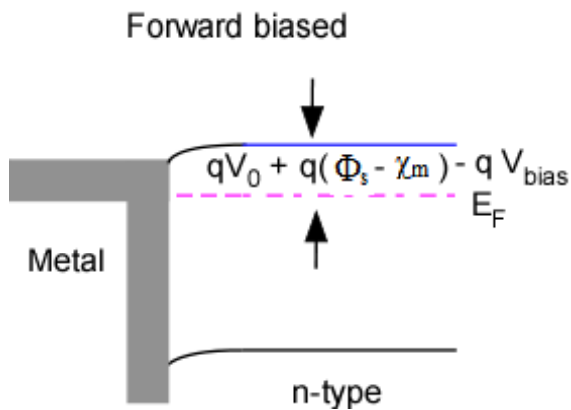
$$\frac{dN}{dt} = \frac{J}{qd} - \frac{N}{\tau} - \Omega(N - N_0)N_{ph}$$

$$\frac{dN}{dt} = \frac{J}{qd} - \frac{N}{\tau} \quad \tau_d = N_{th} / \frac{J}{qd} = \frac{\bar{N}}{J/qd} = \frac{\tau J_{th} / qd}{J/qd} = \tau \frac{J_{th}}{J}$$

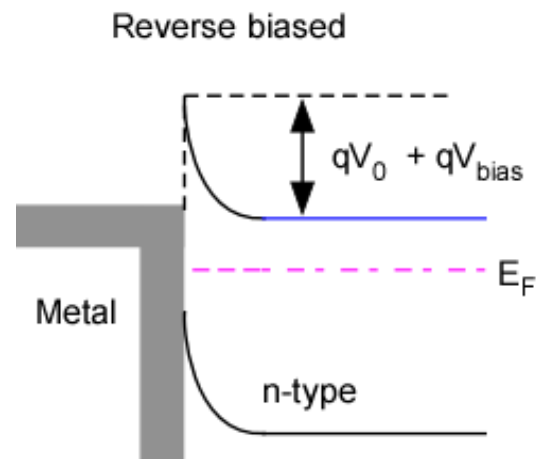
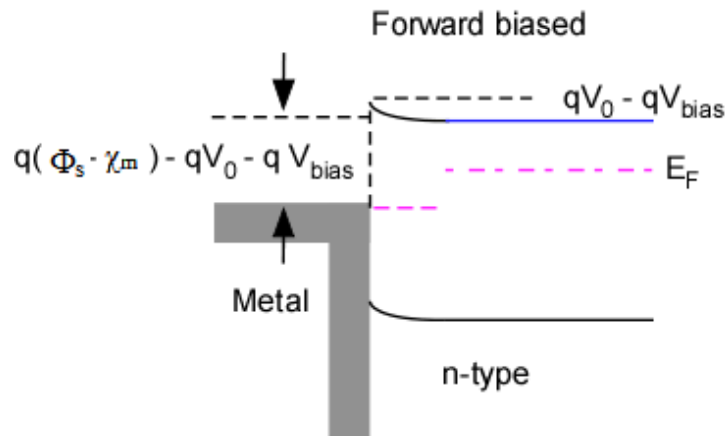
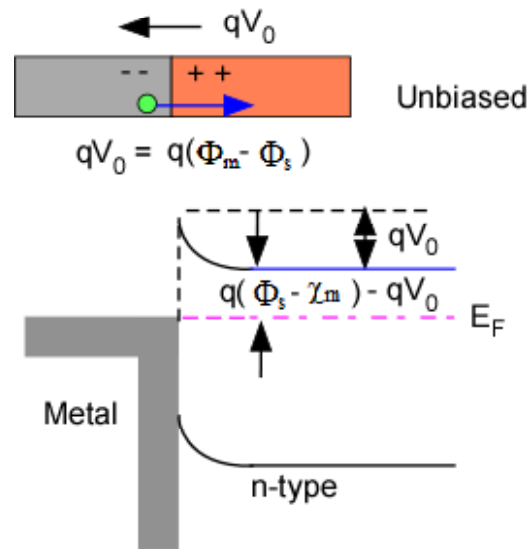
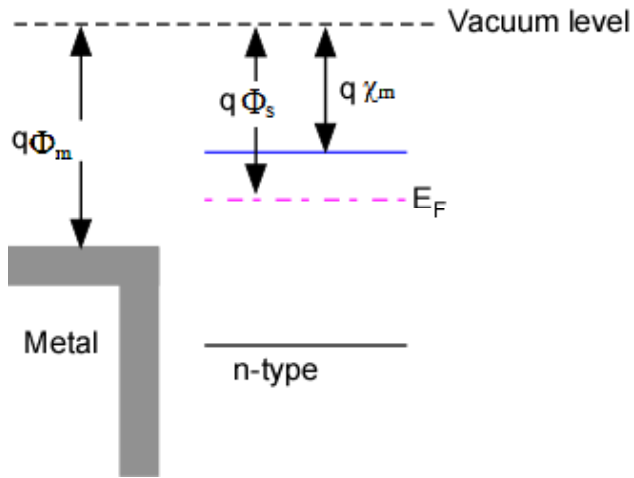




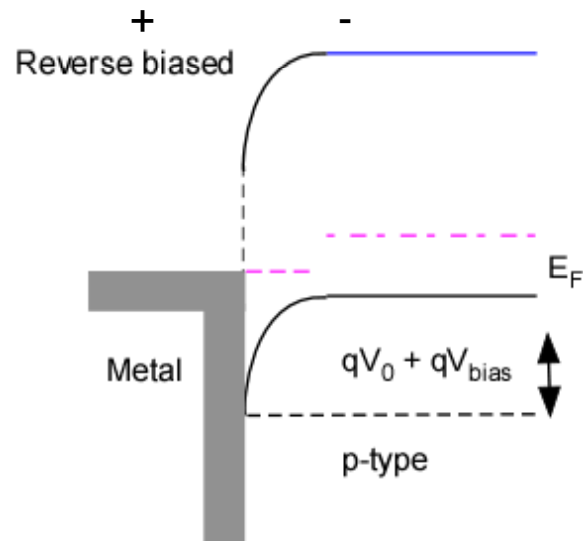
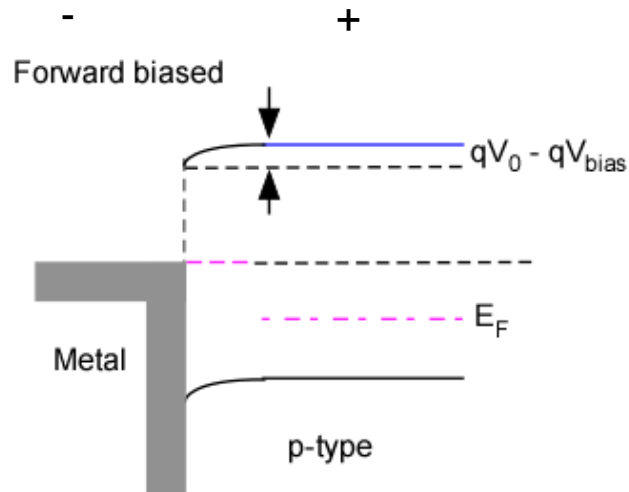
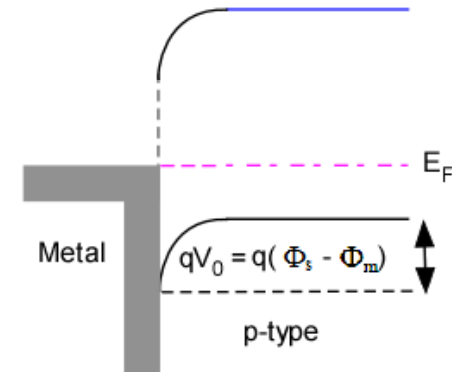
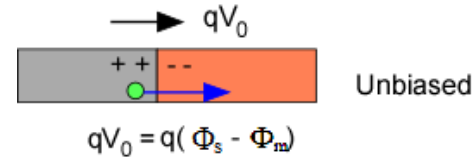
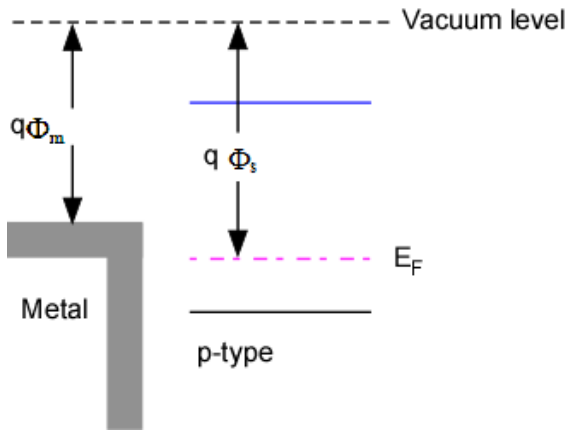
Ohmic contact



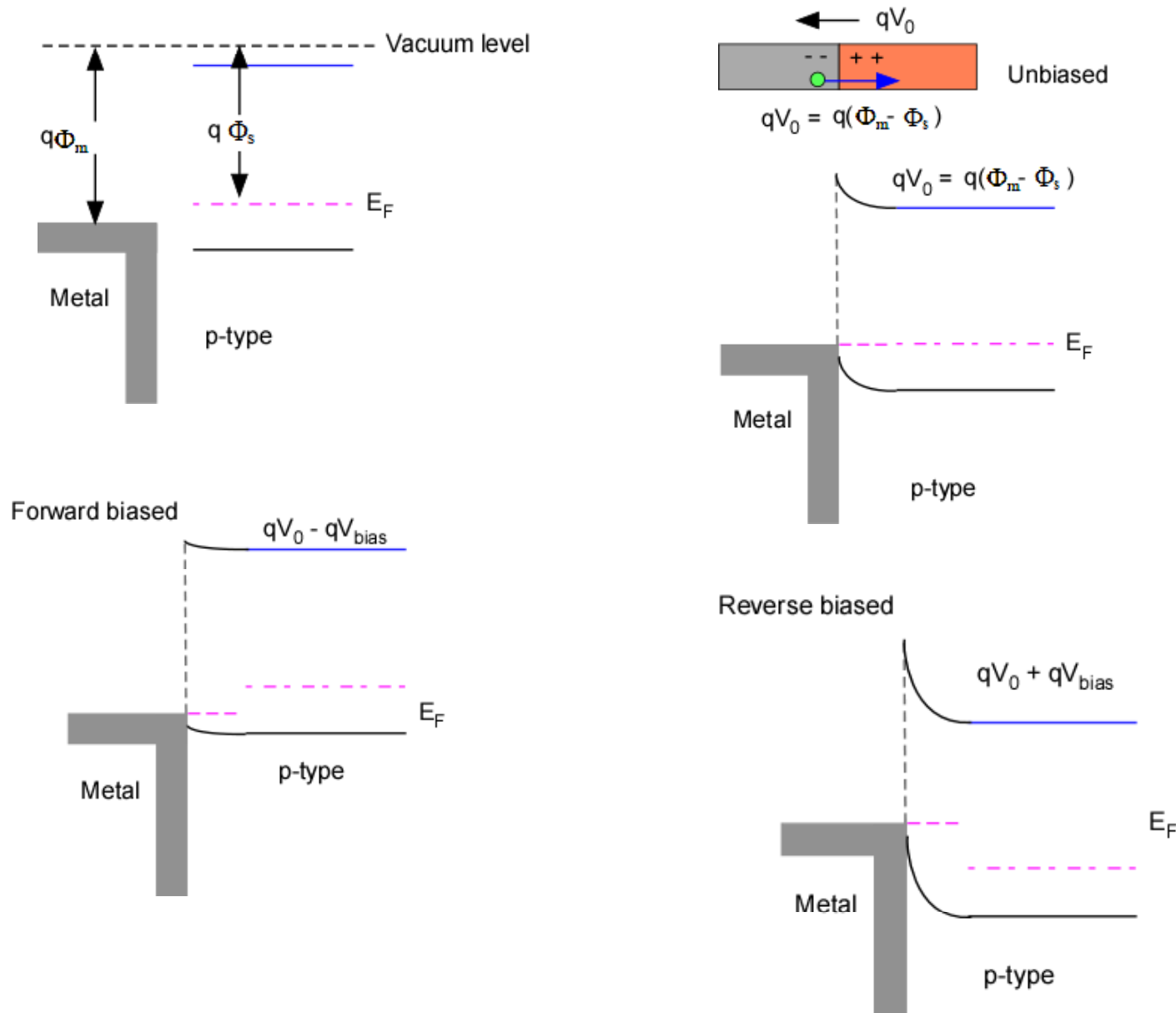
Schottky barrier



Schottky barrier



Ohmic contact



typical method for forming ohmic contacts is by doping the semiconductor heavily in the contact region, which reduces depletion width. When depletion width small enough carriers can be tunneling through the barriers.

- hw: 1. A schottky barrier is formed between a metal having a work function of 4.3 eV and a p-type Si with electron affinity = 4 eV. The acceptor doping in Si is  $10^{17} \text{ cm}^{-3}$
- (a) draw the equilibrium <sup>band</sup> diagram, show a numerical value for  $qV_0$
- (b) draw the band diagram for 0.3V forward bias. Repeat 2V reverse bias.
2. what's the conductivity of a piece of Ge ( $n_i = 2.5 \times 10^{13} \text{ cm}^{-3}$ ) doped with  $5 \times 10^{13} \text{ cm}^{-3}$  donors  $D_n = 100 \text{ cm}^2/\text{s}$ . If the electron affinity of Ge = 4.0 eV and we put down a metal electrode with work function = 4.5 eV. ~~What~~ what's the work function difference. Do you expect this to be a schottky or an ohmic contact?