

## ***Formula Sheet: Electricity and Magnetism***

### **Coulomb's law**

$$F = k \frac{Q_1 Q_2}{r^2}$$

### **Electric Field**

$$\vec{E} = \frac{\vec{F}}{q}$$

Field of a point charge

$$E = k \frac{Q}{r^2}$$

Principle of superposition

$$\vec{E}_{net} = \sum_{i=1}^N \vec{E}_i$$

### **Electric potential**

$$V = \frac{U}{q}$$

$$V(r) = - \int_{\infty}^r \vec{E} \cdot d\vec{l}$$

$$V_{ba} = V_b - V_a = - \int_a^b \vec{E} \cdot d\vec{l}$$

For a point charge  $V(r) = \frac{1}{4\pi\epsilon_0} \frac{Q}{r}$

### **Potential Energy**

q moving through  $V_{ba}$

$$\Delta U = qV_{ba}$$

### **Capacitors**

$$C = \frac{Q}{V}$$

Parallel-plate  $C = \epsilon_0 \frac{A}{d}$

***Capacitors connected in parallel***

$$C_{eq} = C_1 + C_2 + \dots$$

***Capacitors connected in series***

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$$

***Energy stored in a capacitor***  $U = \frac{Q^2}{2C}$

### **Ohm's law**

$$V = IR$$

$$R = \rho \frac{l}{A}$$

***Power***

$$P = IV$$

***Resistors connected in series***

$$R_{eq} = R_1 + R_2 + R_3 + \dots$$

***Resistors connected in parallel***

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$$

***The potential difference across a charging capacitor in RC circuit***

$$V(t) = \epsilon(1 - e^{-t/RC})$$

**A magnetic field exerts a force**

$$d\vec{F} = I d\vec{l} \times \vec{B}$$

$$\vec{F} = I \vec{l} \times \vec{B}$$

$$\vec{F} = q\vec{v} \times \vec{B}$$

***The torque on a current loop***

$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

$$\vec{\mu} = NI\vec{A}$$

### The Biot-Savart Law

$$d\vec{B} = \frac{\mu_0 I d\vec{l} \times \hat{r}}{4\pi r^2}$$

### The magnetic field of:

A straight line wire

$$B = \frac{\mu_0 I}{2\pi r}$$

A solenoid

$$B = \mu_0 n I$$

### Magnetic flux

$$\Phi_B = \int \vec{B} \cdot d\vec{A}$$

### Mutual inductance

$$M = \frac{N_2 \Phi_{21}}{I_1}$$

$$\varepsilon = -M \frac{dI_1}{dt}$$

### Self-inductance

$$L = N \frac{\Phi_B}{I}$$

$$\varepsilon = -L \frac{dI}{dt}$$

### Energy stored in an inductor

$$U = L \frac{I^2}{2}$$

### Charged LR circuit

$$I = \frac{V_0}{R} (1 - e^{-t/\tau}); \tau = L/R$$

### Maxwell's equations

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q}{\varepsilon_0}$$

$$\oint \vec{B} \cdot d\vec{A} = 0$$

$$\oint \vec{E} \cdot d\vec{l} = -\frac{d\Phi_B}{dt}$$

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 I + \mu_0 \varepsilon_0 \frac{d\Phi_E}{dt}$$

### Constants

Charge on electron

$$e = 1.60 \cdot 10^{-19} \text{ C}$$

Electron mass  $m = 9.11 \cdot 10^{-31} \text{ kg}$

Permittivity of free space

$$\varepsilon_0 = 8.85 \cdot 10^{-12} \text{ C}^2/\text{Nm}^2$$

Permeability of free space

$$\mu_0 = 4\pi \cdot 10^{-7} \text{ Tm/A}$$

$$k = \frac{1}{4\pi\varepsilon_0} = 8.99 \cdot 10^9 \text{ Nm}^2/\text{C}^2$$

### Kinematic eq-ns with const. Acc.:

$$v(t) = v_{0x} + at$$

$$x(t) = x_0 + v_{0x}t + (1/2)at^2$$

$$v^2 = v_{0x}^2 + 2a(x - x_0)$$

Centripetal acceleration  $a_R = v^2/r$