

## Section 5.2

After viewing the lecture videos and reading the textbook, you should be able to answer the following questions:

1. What is sigma notation?
2. Suppose a sum can be written in sigma notation as  $\sum_{k=1}^n a_k$ .
  - a. What is  $\Sigma$ ? What does it stand for?
  - b. What is the index of summation?
  - c. What is the lower limit of summation?
  - d. What is the upper limit of summation?
  - e. What is the  $k$ -th term of the sum?
  - f. Write the sum without sigma notation.
3. The algebra rules for finite sums are:

$$\sum_{k=1}^n (a_k + b_k) = \sum_{k=1}^n a_k + \sum_{k=1}^n b_k$$

$$\sum_{k=1}^n (a_k - b_k) = \sum_{k=1}^n a_k - \sum_{k=1}^n b_k$$

$$\sum_{k=1}^n c a_k = c \cdot \sum_{k=1}^n a_k$$

$$\sum_{k=1}^n c = n \cdot c$$

Suppose  $\sum_{k=1}^{13} a_k = 3$  and  $\sum_{k=1}^{13} b_k = 5$ . Find the values of:

- a.  $\sum_{k=1}^{13} (a_k + b_k)$
- b.  $\sum_{k=1}^{13} (a_k - b_k)$
- c.  $\sum_{k=1}^{13} 7a_k$
- d.  $\sum_{k=1}^{13} 11$
- e.  $\sum_{k=1}^{13} (7a_k - b_k + 11)$

4. Which of the following is not true (select one):

- a.  $\sum_{k=1}^n (a_k - 1) = \sum_{k=1}^n a_k - n$
- b.  $\sum_{k=1}^n (a_k - 1) = \sum_{k=1}^n a_k - 1$
- c.  $\sum_{k=1}^n (a_k - 1) = \sum_{k=1}^n a_k - \sum_{k=1}^n 1$

5. A Riemann sum for a bounded function  $f$  on a closed interval  $[a, b]$  is the sum

$$S_P = \sum_{k=1}^n f(c_k) \cdot \Delta x_k.$$

- a. What does  $n$  represent?
  - b. The set  $P$  is called a **partition** of  $[a, b]$ . What is  $P$ ? (Answer:  $P$  is any set such that  $P = \{x_0, x_1, x_2, \dots, x_{n-1}, x_n\}$  where  $a = x_0 < x_1 < x_2 < \dots < x_{n-1} < x_n = b$ )
  - c. What is the  $k$ -th subinterval of  $[a, b]$ ?
  - d. What does  $\Delta x_k$  represent? How can we calculate  $\Delta x_k$ ?
  - e. What does  $c_k$  represent?
  - f. Other than "the value of  $f(x)$  at  $x = c_k$ ", what does  $f(c_k)$  represent?
6. If  $P$  is a partition of  $[a, b]$ , what is  $\|P\|$  (the **norm** of  $P$ )?
7. The Riemann sum for a continuous function  $f$  on a closed interval  $[a, b]$  approximates (choose one):
- a. The total area of the region bounded by the curve  $y = f(x)$  and the  $x$ -axis over the interval  $[a, b]$ .
  - b. The area above the  $x$ -axis of the region bounded by the curve  $y = f(x)$  and the  $x$ -axis minus the area below the  $x$ -axis of the region bounded by the curve  $y = f(x)$  and the  $x$ -axis over the interval  $[a, b]$ .
  - c. It is just a random sum that we defined.