

Math 491, Problem Set #9  
(due 10/9/03; postponed to 10/14/03)

1. (a) How many different polygonal paths of length  $n$  are there that start at the point  $(0, 0)$  and then take  $n$  steps of length 1, such that each step is either rightward, leftward, or upward, and such that no point gets visited more than once? Give an explicit formula.
- (b) If one chooses at random one of the paths of length  $n$  described in part (a) (so that each of the length- $n$  paths has an equal chance of being chosen), what is the expected value of the  $y$ -coordinate of the last point on the path? Find a constant  $c$  so that this expected value is asymptotic to  $cn$ .