

Image Processing using Matlab

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Outline

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- What is Matlab?
- Matlab Basics
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Introduction

- Image Processing generally involves extraction of useful information (qualitative and/or quantitative) from an image.
- This useful information may be the dimensions of an engineering component, size of diagnosed tumor, a three-dimensional rendering of an unborn baby, spatial distribution (e.g., length, shape) of a surface crack, area of a corroded steel rebar, or volume of a crumbled concrete.

What is Matlab?

- Matlab is an abbreviation of Matrix Laboratory by MathWork®.
- Scientific and engineering standard for mathematical processing and programming → Large user group around the world
- In Matlab, everything is represented in the form of arrays or matrices. → Linear Algebra
- Code developed in Matlab can be converted into C, C++ or Visual C++. → Portability, flexibility
- Matlab codes may be called as ActiveX Object from higher level languages like Visual Basic. → Expendability

Matlab Basics

- Matrix Declaration:
 - Null Matrix → *null*
 - Matrix with Ones → *ones(m, n)*
 - Identity Matrix → *eye(n)*
 - Random Matrix → *randn(n)*
- Matrix Arithmetic:
 - Addition
 - Subtraction
 - Multiplication
 - Division

Matlab Basics

- Matrix manipulation:
 - Addressing of individual element $\rightarrow A(i, j)$
 - Complete row addressing $\rightarrow A(:, n)$
 - Complete column addressing $\rightarrow A(n, :)$
 - Transpose $\rightarrow A = B'$
 - Flip matrices \rightarrow *fliplr* and *flipud*
- Saving and loading data \rightarrow *save* and *load*
- Concept of function and m-files
- Concept of path \rightarrow *cd*, *pwd*

Matlab Basics

- Useful commands:
 - *whos*
 - *help* → *Learn how to use help to teach yourself Matlab commands.*
 - *clear*
 - *path*
 - *cd*
 - *dir*
 - *lookfor*

Image Processing in Matlab

- Images can be conveniently represented as matrices in Matlab.
- Images can be conveniently represented as matrices (2D or 3D) in Matlab.
- The matrix may simply be $m \times n$ form or it may be 3D array or it may be an indexed matrix, depending upon image type.
- Image processing is carried out by matrix calculation or matrix manipulation.
- Image can be read by using *imread* command, displayed with *imshow* command, and saved with *imwrite* command.

Image Processing in Matlab

- Generally speaking, images can be of three types; black & white (BW), grey scale, and colored (Red-Green-Blue or RGB).
- In Matlab, there are the following types:
 - Black & White images are called binary images, containing 1 for white and 0 for black.
 - Grey scale images are called intensity images, containing numbers in the range of 0 to 255 or 0 to 1.
 - Colored images may be represented as RGB Image or Indexed Image.

Image Processing in Matlab

- In **RGB** images there exist three indexed images.
- First image contains all the red portion of the image, second green and third contains the blue portion. → *Therefore for a 640 x 480 sized image the matrix will be 640 x 480 x 3.*
- An alternate method of colored image representation is Indexed Image. → *Each color in the image is given an index number and in image matrix each color is represented as an index number.*
- Map matrix contains the database of which index number belongs to which color.

Image Processing in Matlab

- Read in an image.
- Validates the graphic format.
(bmp, hdf, jpeg, pcx, png, tiff, xwd)
- Store it in an array.
clear, close all
I = imread('pout.tif');
[X, map] = imread('pout.tif');

Image Processing in Matlab

- RGB Image to Intensity Image (*rgb2gray*)
- RGB Image to Indexed Image (*rgb2ind*)
- RGB Image to Binary Image (*im2bw*)
- Indexed Image to RGB Image (*ind2rgb*)
- Indexed Image to Intensity Image (*ind2gray*)
- Indexed Image to Binary Image (*im2bw*)
- Intensity Image to Indexed Image (*gray2ind*)
- Intensity Image to Binary Image (*im2bw*)
- Intensity Image to RGB Image (*gray2ind*, *ind2rgb*)

Image Processing in Matlab

- There are a number of ways to get statistical information about data in the image. → Image histogram is on such way.
- An image histogram is a chart that shows the distribution of intensities in an image.
- Each color level is represented as a point on x-axis and on y-axis is the number instances a color level repeats in the image.
- Histogram may be view with *imhist* command.
- Sometimes all the important information in an image lies only in a small region of colors, hence it usually is difficult to extract information out of that image.
- To balance the brightness level, one can perform histogram equalization.

Image Processing in Matlab

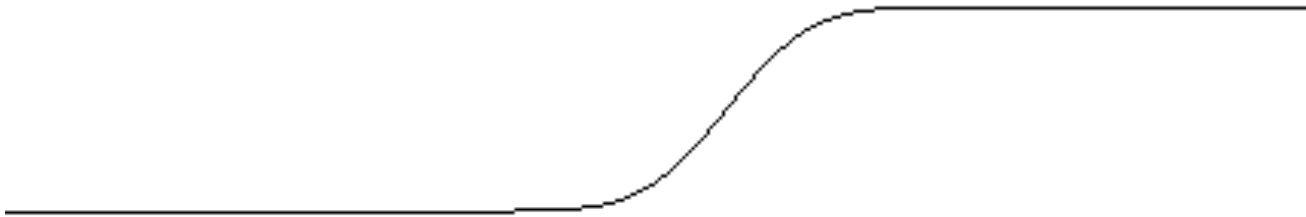
- In image processing useful pixels in the image are separated from the rest by image segmentation.
- *Brightness threshold* and *edge detection* are the two most common image segregation techniques.
- In brightness threshold, all the pixels brighter than a specified brightness level are taken as 1 and rest are left 0.
→ *This leads to a binary image with useful image as 1 and unwanted as 0.*
- In edge detection special algorithms are used to detect edges of objects in the image. → *edge*

Edge Detection

- Edge detection extract edges of objects from an image.
- There are a number of algorithms for this, but these may be classified as derivative based or gradient based.
- In derivative based edge detection the algorithm takes first or second derivative on each pixel in the image. → *In case of first derivative at the edge of the image there is a rapid change of intensity.*
- While in case of second derivative there is a zero pixel value, termed zero crossing.
- In gradient based edge detection a gradient of consecutive pixels is taken in x and y direction.

Edge Detection

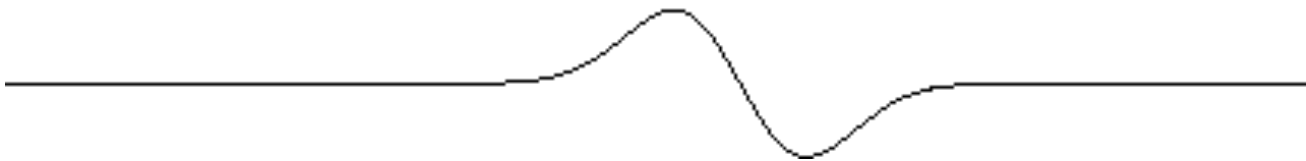
Function $f(x)$



1st derivative



2nd derivative



Edge Detection

- Taking derivative on each and every pixel of the image consumes a lot of computer resources and is not practical.
→ *Typically an operation called kernel operation is carried out.*
- A kernel is a small matrix sliding over the image matrix containing coefficients which are multiplied to corresponding image matrix elements and their sum is put at the target pixel.

Sobel Edge Detection

- In *sobel* following formulas are applied on each pixel (i,j) in the image and two matrices S_x and S_y are obtained:

$$S_x = (a_2 + ca_3 + a_4) - (a_0 + ca_7 + a_6)$$
$$S_y = (a_0 + ca_1 + a_2) - (a_6 + ca_5 + a_4)$$
$$C = 2$$

- Alternatively this can be done by applying following two kernels:

$S_x =$	-1	0	1
	-2	0	2
	-1	0	1

$S_y =$	1	2	1
	0	0	0
	-1	-2	-1

- The resultant matrix is then obtained by taking the square root of the sum of the squares of S_x and S_y , as follows:

$$M(i,j) = (S_x^2 + S_y^2)^{1/2}$$

Prewitt Edge Detection

- In *Prewitt* everything is same but $C=1$:

$$S_x = (a_2 + ca_3 + a_4) - (a_0 + ca_7 + a_6)$$
$$S_y = (a_0 + ca_1 + a_2) - (a_6 + ca_5 + a_4)$$
$$C = 1$$

- Alternatively this can be done by applying following two kernels:

$$s_x = \begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix} \quad s_y = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ -1 & -1 & -1 \end{bmatrix}$$

- The resultant matrix is then obtained by taking the square root of the sum of the squares of S_x and S_y , as follows:

$$M(i,j) = (S_x^2 + S_y^2)^{1/2}$$

Morphological Operations

- These are image processing operations done on binary images based on certain morphologies or shapes.
- The value of each pixel in the output is based on the corresponding input pixel and its neighbors.
- By choosing appropriately shaped neighbors one can construct an operation that is sensitive to a certain shape in the input image.

Morphological Operation Skeletonize

- It creates skeleton of an object, by removing pixels on the boundaries but does not allow objects to break apart.
- It is an extremely important operation in image processing as it removes complexities from an image without losing details.



Erosion & Dilation

- These are the most fundamental of binary morphological operations.
- In dilation if any pixel in the input pixel's neighborhood is on, the output pixel is on otherwise off.
- In actual dilation grows the area of the object. Small holes in the object are removed.
- In erosion if every pixel in the input pixel's neighborhood is on the output pixel is on otherwise off
- This in actual works as shrinking the object's area, thus small isolated regions disappear.

Simple Morphological Operations

- *imerode* – Erode image.
- *imclose* – Morphologically close image.
- *imopen* – Morphologically open image.
- *imdilate* – Dilate image.
- *strel* – Create morphological structuring element (STREL).

- *imread* – Read image from graphics file.
- *imwrite* – Write image to graphics file.
- *imshow* – Display image.
- *imsubtract* – Subtract one image from another or subtract constant from image.
- *imadjust* – Adjust image.
- *imcrop* – Crop image.

Erosion & Dilation

- *imdilate*

The term watershed
refers to a ridge that ...

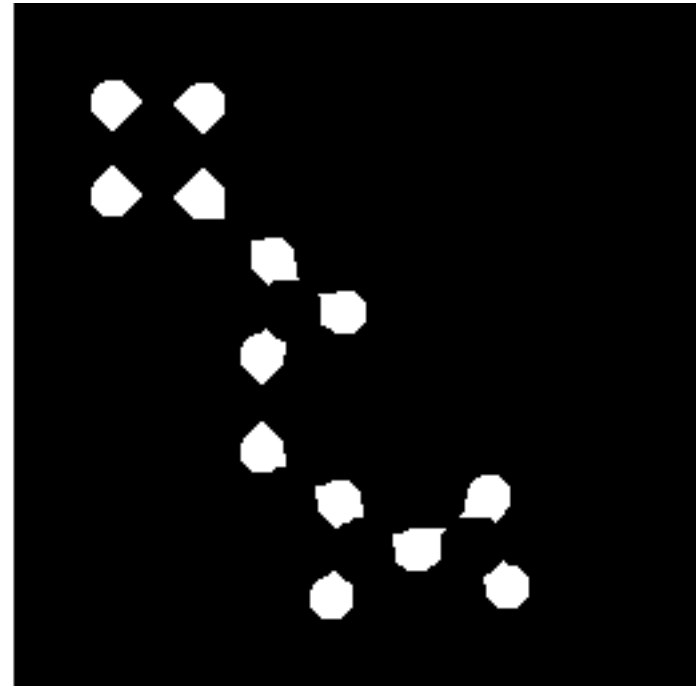
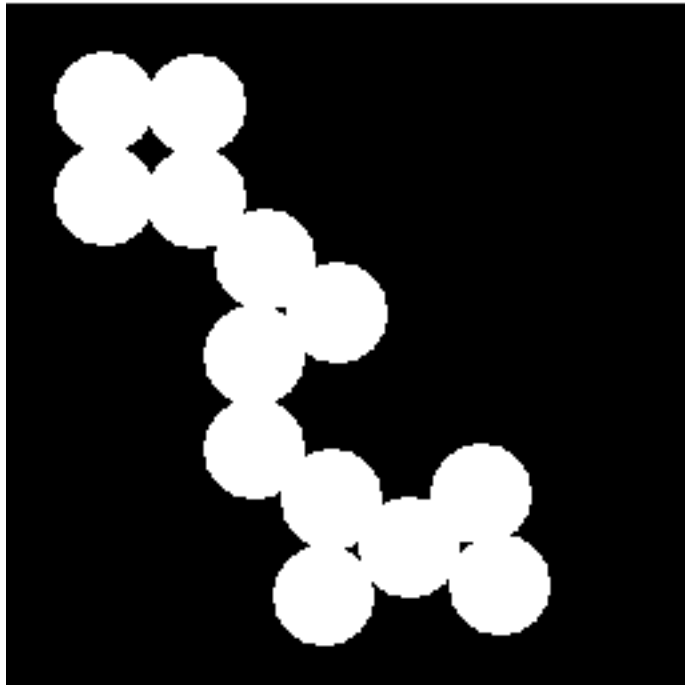
... divides areas
drained by different
river systems.

The term watershed
refers to a ridge that ...



Erosion & Dilation

- *imerode*



Summary

- Imaging (rendering data into image) is an approach in data visualization. Mathematically, an image is a two-dimensional tensor.
- *Linear Algebra* is the mathematical basis in image processing.
- The objective of image processing is ***to reveal the physical pattern in the data, not to play with mathematical skills.***

References

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