



Structural Engineering Research Group
(SERG)
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Structural Health Monitoring of a Reinforced Concrete Beam Using Finite Element Analysis

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SERG

- Introduction
- Objective
- Literature Review
- Finite Element Modeling
- Materials Properties
- Experimental Work
- Finite Element Model Validation
- Damage Modeling
- Defect Detection Methodology
- Conclusion
- Future Work

- **Structural Health Monitoring (SHM):** The process of implementing a **damage identification strategy** for civil, mechanical, and aerospace engineering infrastructure is referred to as SHM.

Damage:

- Material properties
- Geometric properties
- Boundary conditions
- System connectivity

- **Why SHM?**
 - Public safety
 - Economical benefit

- **SHM system:**

Sensing technology	Power technology	Communication devices	A monitoring station	Signal processing algorithm	Health evaluation algorithm
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- **Sensors** can measure (1) **mechanical quantities** (2) thermal quantities (3) electromagnetic/optical quantities and (4) chemical quantities
- Surface strain measuring sensors are widely use in SHM.

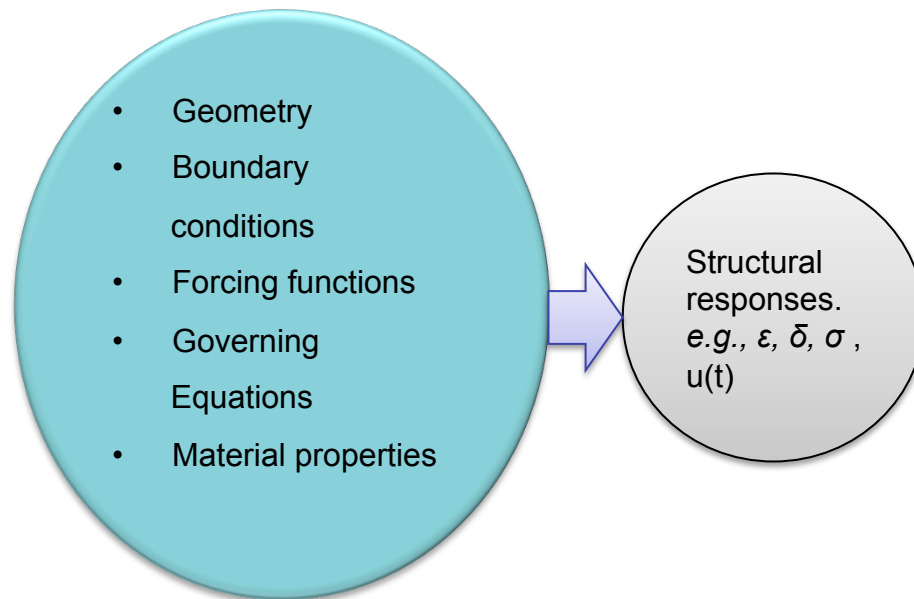
Introduction

- Applicability of fiber optic sensor (FOS) and digital image correlation (DIC) in strain measurements:

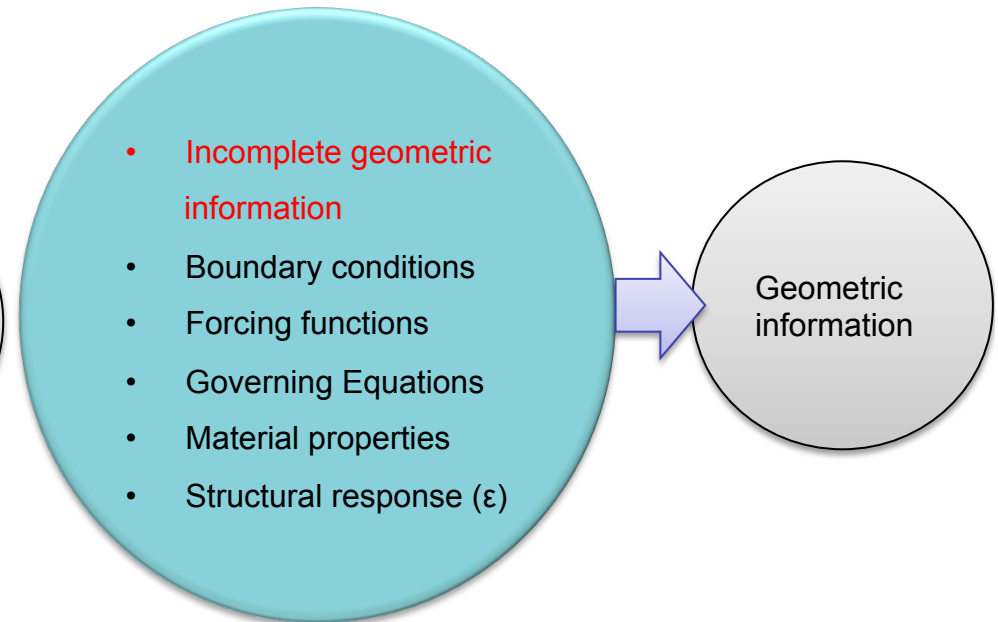
Measurement Technique	Types of surface strain measurement			Subsurface strain measurement
	Points	Lines	Planes	Points / lines
FOS	✓	✓	✗	✗/✓
DIC	✓	✓	✓	✗

- How can surface strain measurement be used to evaluate structural integrity?
- To determine structural health using surface strain measurement is a challenging real-life engineering problem. It is an inverse problem.
- Inverse problem ?

- Forward problem example



- Inverse problem in this research ★



- Knowledge of forward problem solution can be used to solve the inverse problem.

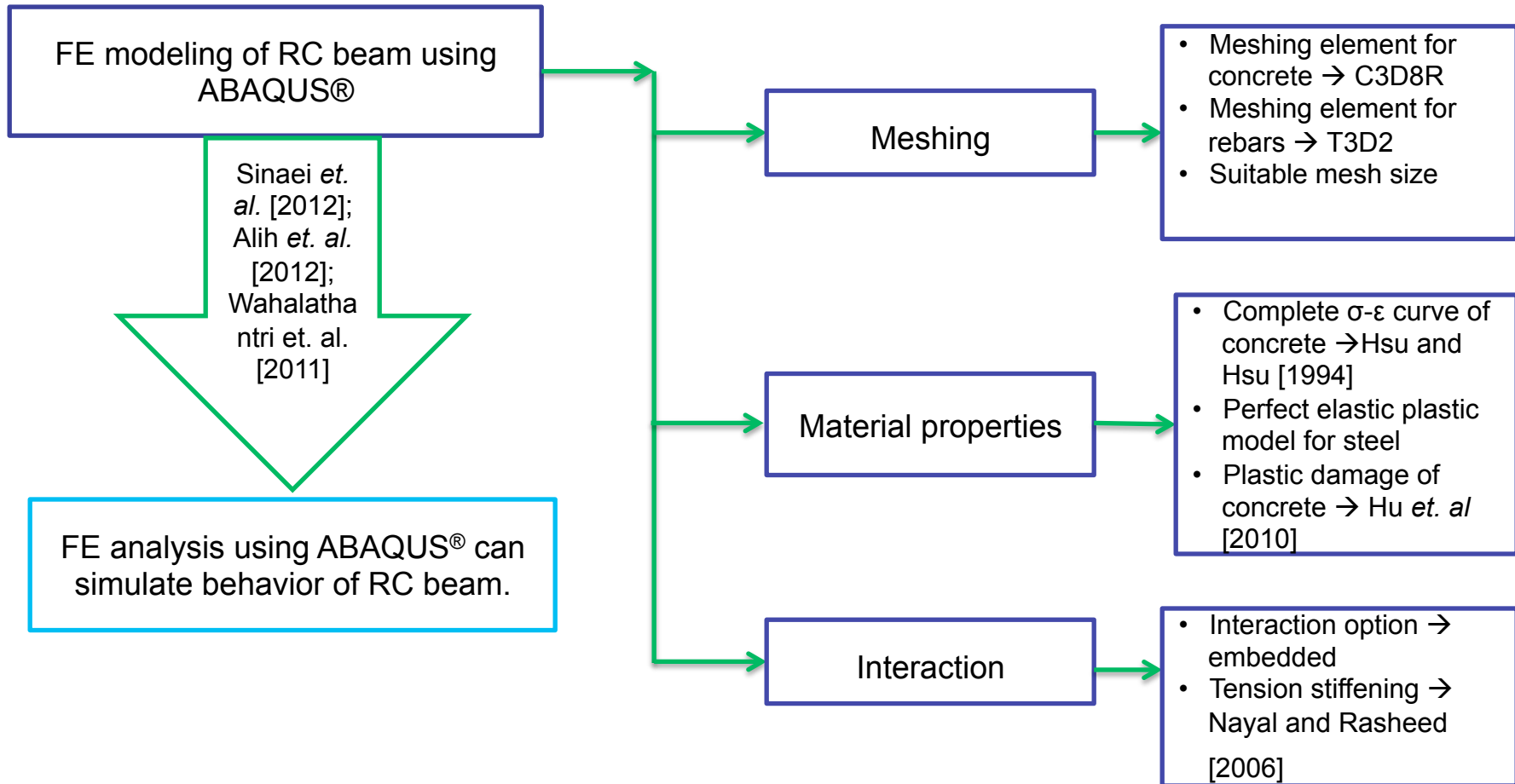
Objective

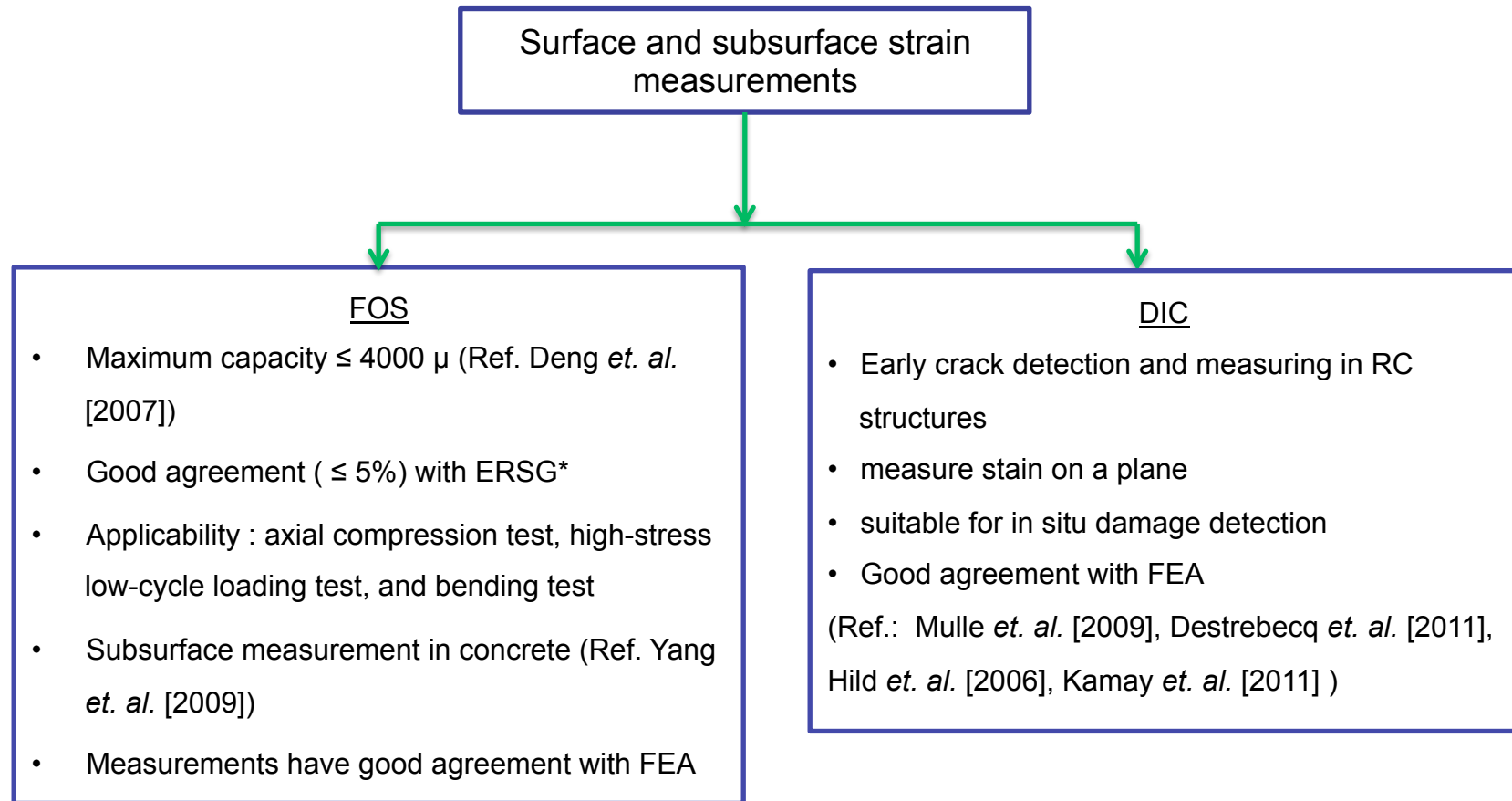
- The research objective of this study is to develop a damage detection methodology to relate surface strain measurement to internal conditions (e.g., healthy or damaged) using a singly-reinforced concrete beam as an example.

Internal condition assessment
using surface measurements/
inverse problem solution
techniques for civil infrastructures

Wang *et. al.*
[2010];
Nazmul *et.*
al. [2004,
2007]; Cox
et. al. [1991]

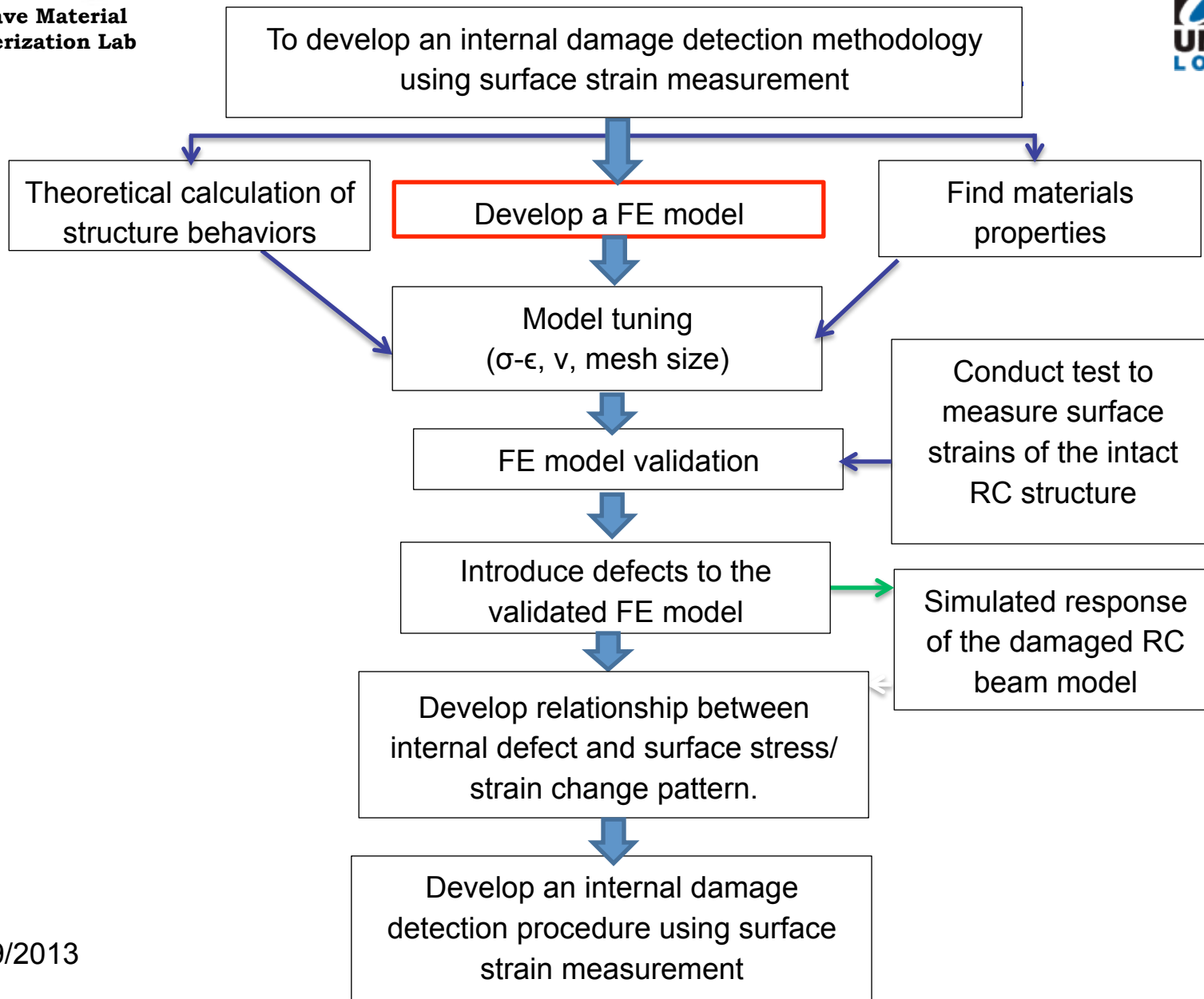
Theoretical approach	<ul style="list-style-type: none">• Applicable for solving inverse problem using precise local measurements.
Numerical approach	<ul style="list-style-type: none">• Can be used in global damage detection• Sensitive-based FE model updating is frequently used in damage detection

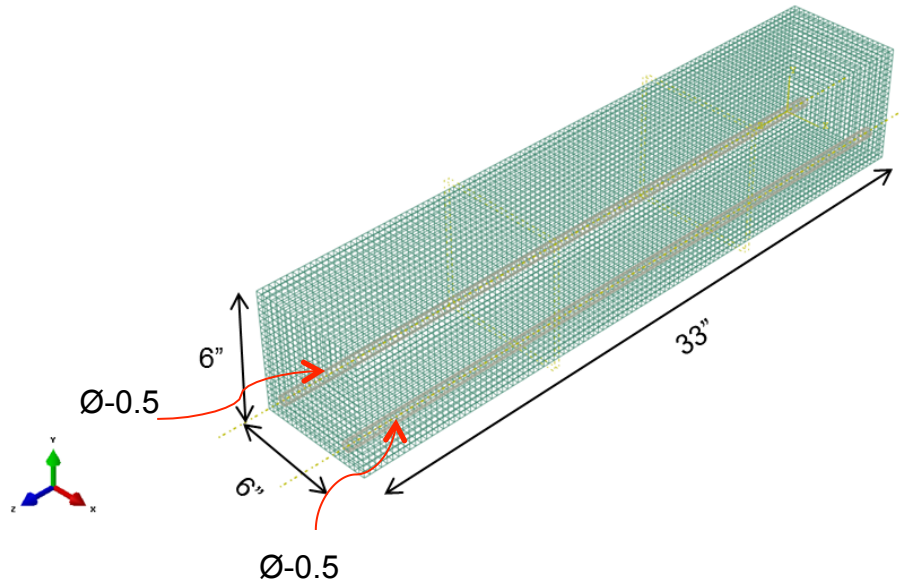




* Electrical Resistance Strain Gauge

Research Roadmap



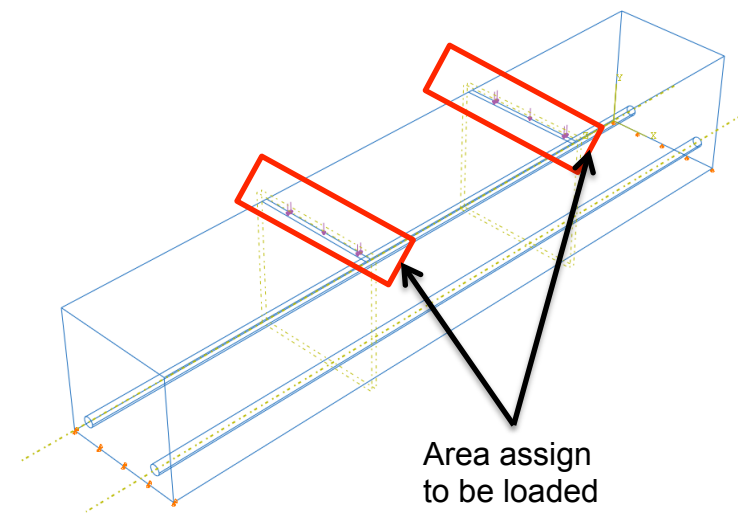


▪ Loading and B.C.:

- Simply supported
- Loaded area $\rightarrow 0.125'' \times 6''$
- Loading level \rightarrow from 0 to 2.2 kips at four steps

▪ Meshing and interaction:

- Element to model concrete \rightarrow C3D20
- Element to model rebar \rightarrow C3D8
- Mesh edge size for concrete $\rightarrow 0.3''$
- Mesh edge size for rebar $\rightarrow 0.25''$
- Total elements in the model $\rightarrow 45,056$
- Total variables $\rightarrow 579,285$
- Interaction between concrete and rebar \rightarrow embedded



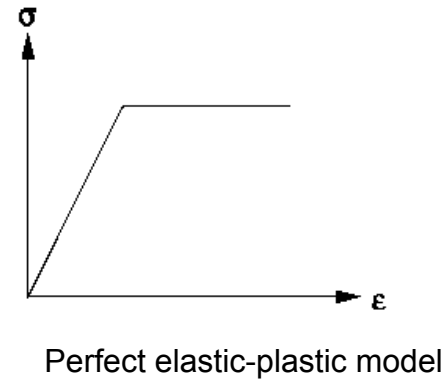
- Materials properties

- Elastic properties:

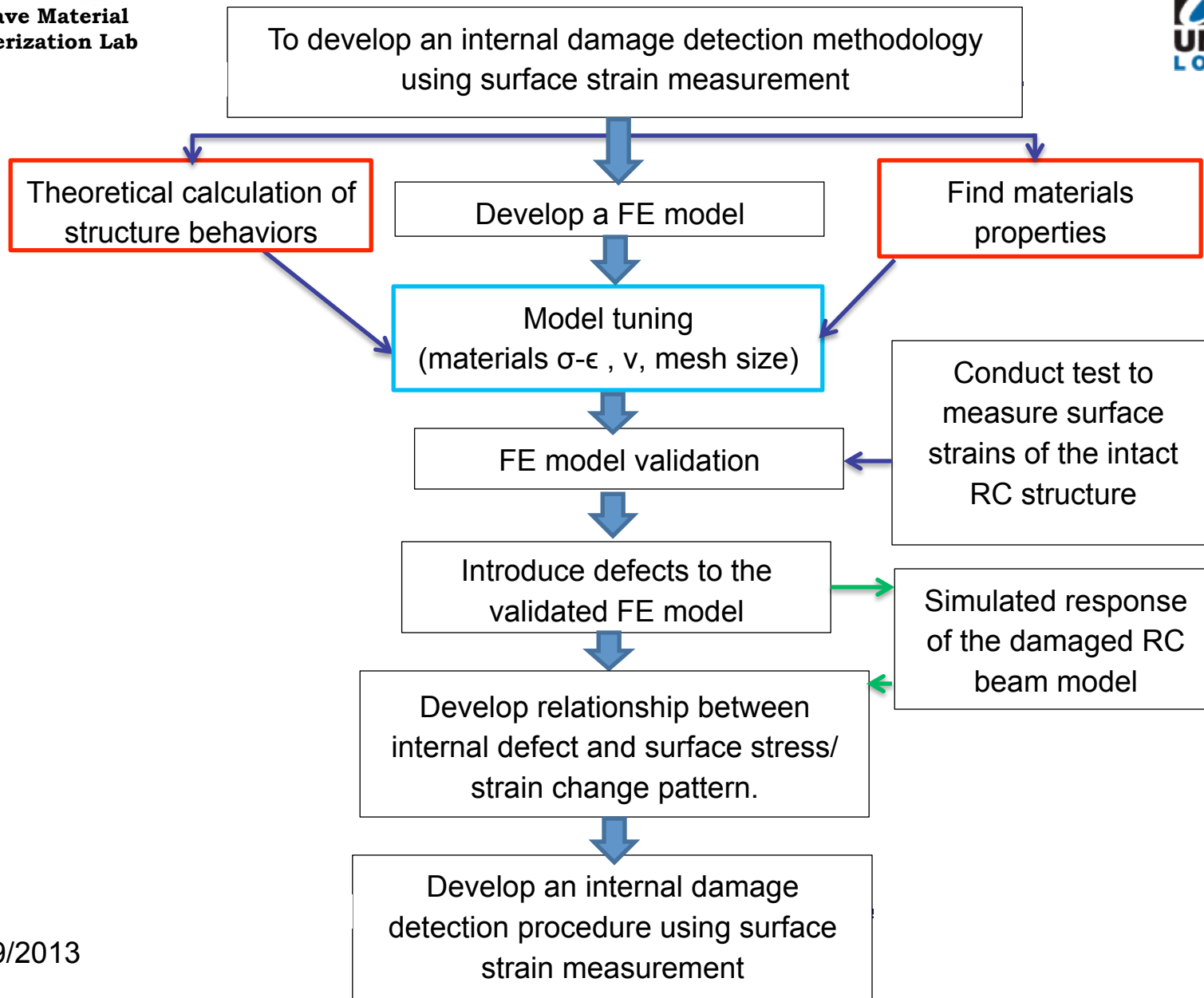
- $E_c = 57,000 \sqrt{f_c}$ (ACI 318, units in psi)
- $\nu_c = 0.16$ (Ref. Bonfiglioli *et. al.* [2003])
- $E_s \rightarrow$ Experimentally obtained $\rightarrow 30 \times 10^6$ psi
- $\nu_s = 0.3$

- Plastic properties and interaction:

Model	Purpose
Hsu and Hsu [1994]	To obtain complete σ - ϵ
Perfect elastic-plastic material property	σ - ϵ behavior of steel
Nayal and Rasheed model [2006] (Modified by Walhalathantri <i>et. al.</i> [2011])	Simulate interaction between concrete and rebars



Research Roadmap



☐ Materials Testing

- Steel → tension test of rebar
- Concrete → ASTM standard compression test (C39/C39M)

▪ Tension Test of rebar

➤ Specimen:

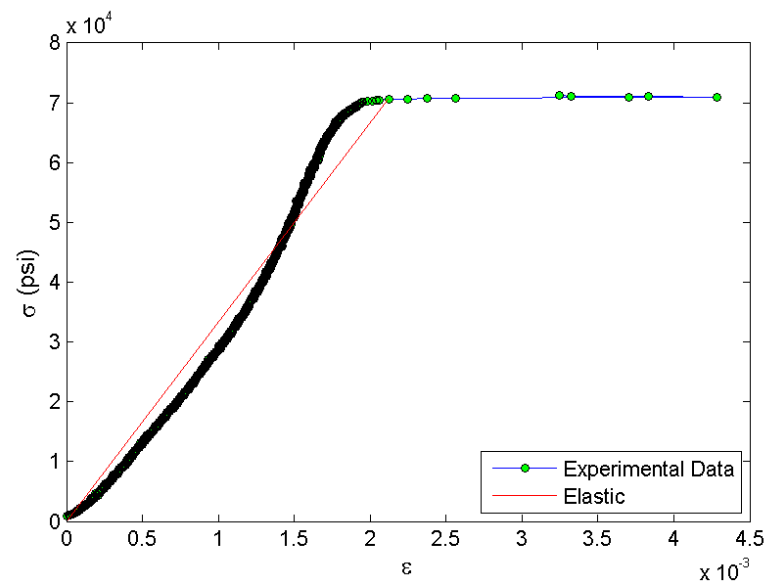
- #4 steel rebar
- Length → 14"

➤ Test result: $f_y \rightarrow 70$ ksi,

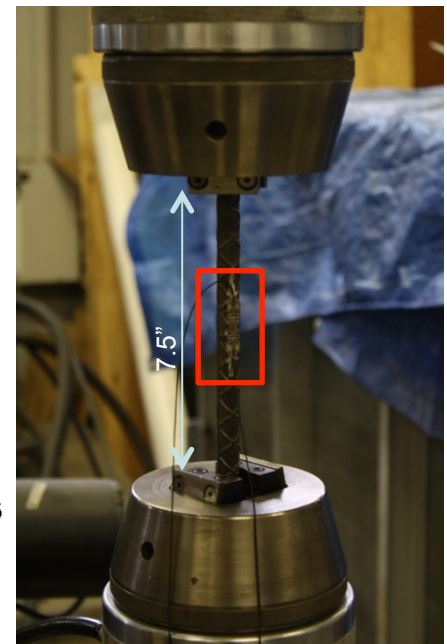
$$E_s = 30 \times 10^6 \text{ psi}$$

▪ Compression test of concrete

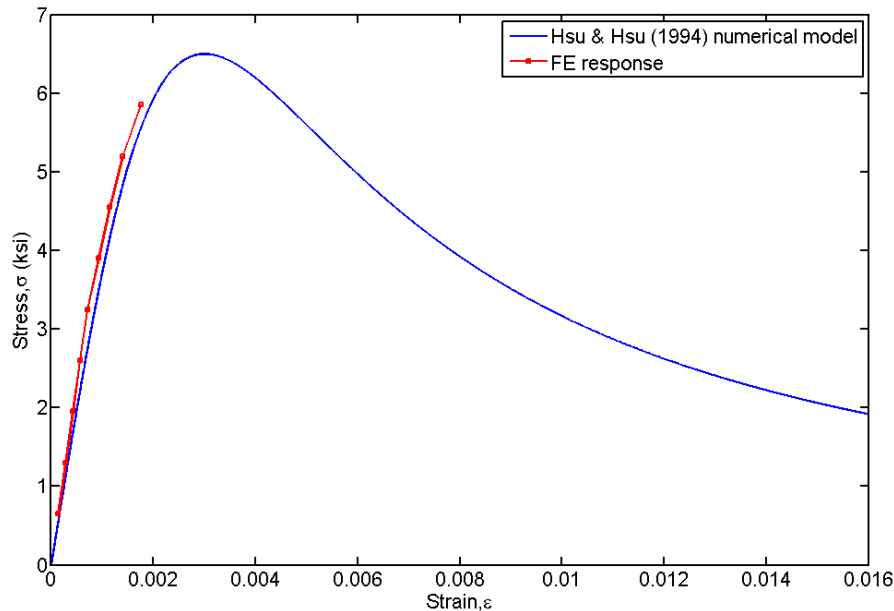
- ASTM C39/C39M
- Specimen: Two 4" x 8" cylinders
- Test result: $\sigma_{cu} = 6,500$ psi



Experimental σ - ϵ of steel rebar



▪ Hsu and Hsu model [1994]



Complete σ - ϵ curve of concrete obtained from Hsu & Hsu model

$$\sigma_c = \beta \epsilon_c / \epsilon_{oc} / \beta - 1 + (\epsilon_c / \epsilon_{oc})^\beta * \sigma_{cu}$$

- A dependent parameter, $\beta = 1 / (1 + (\sigma_{cu} / \epsilon_{oc} E_0))$
- Strain at peak stress, $\epsilon_o = 8.9 \times 10^{-5} \sigma_{cu} + 3.28312 \times 10^{-3}$
- Peak tangential modulus, $E_o = 1.2431 \times 10^2 \sigma_{cu} + 3.28312 \times 10^3$

Where,

- σ_c = compressive stress values
- σ_{cu} = Ultimate compression stress (obtained from standard compression test ASTM C39/C39M)
- ϵ_c = compressive strain (domain)

• Inelastic strain, $\epsilon_c^{in} = \epsilon_c - \epsilon_{oc}^{el}$

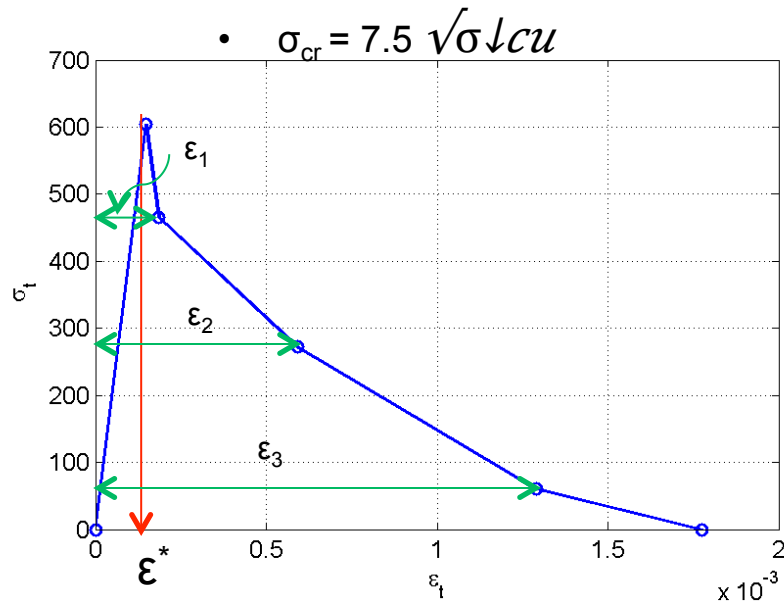
$$\epsilon_{oc}^{el} = \sigma_c / E_o$$

• Damage parameter, $d_t = \epsilon_c^{in} / \epsilon_c$

• Plastic strain, $\epsilon_c^{pl} = \epsilon_c^{in} - \frac{d_t \sigma_c}{(1-d_t)E_o}$

Stress, σ_c	Damage parameter, d_t	Inelastic strain, ϵ_c^{in}
3.25E+03	0.00E+00	0.00E+00
3.56E+03	8.69E-03	6.20E-05
3.72E+03	1.01E-02	7.24E-05
3.88E+03	1.17E-02	8.38E-05
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- Nayal and Rasheed tension stiffening model [2006] (Modified by Walhalathantri *et. al.* [2011])

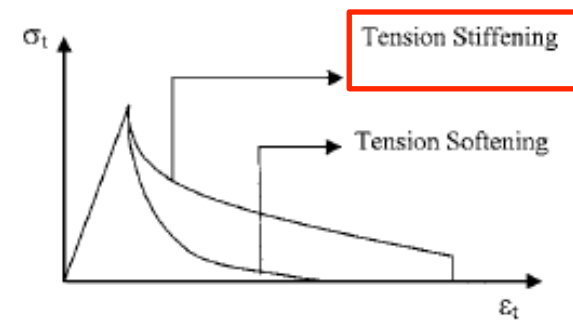


• Cracking strain, $\epsilon_t^{ck} = \epsilon_c - \epsilon_t^{el}$

$\epsilon_t^{el} = \sigma_t / E_0$

• Plastic strain, $\epsilon_t^{pl} = \epsilon_c^{in} - \frac{d_t \sigma_c}{(1-d_t)E_0}$

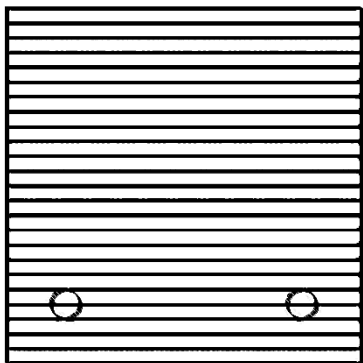
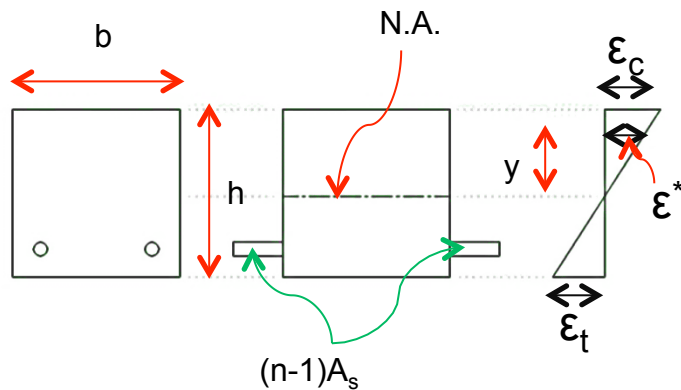
• Damage parameter, $d_t = \epsilon_t^{in} / \epsilon_c$



Tension stiffening (Ref. Nayal *et. al.* [2006])

Stress, σ_c	Strain, ϵ_t	Elastic strain, ϵ_t^{el}	Cracking strain, ϵ_t^{ck}	Damage parameter, d_t	Plastic strain, ϵ_t^{pl}
604.66	1.48E-04	1.48E-04	0.00E+00	0.00E+00	0.00E+00
465.59	1.85E-04	1.14E-04	7.10E-05	3.84E-01	7.09E-05
272.10	5.91E-04	6.65E-05	5.25E-04	8.88E-01	5.17E-04
60.46	1.29E-03	1.48E-05	1.27E-03	9.89E-01	-7.48E+02

Theoretical Calculations



- Effective flexural rigidity,

$$EI = \sum_{i=1}^{n-1} N_i I_i + E_c I_c$$

In an uncracked section,

$$EI = E_c (bh^3/12 + bh \cdot e_1^2 I_3 +$$

$$(n-1)A_s \cdot e_2^2 I_3)$$

where,

- e_1 = distance from concrete section c.g. to section c.g.
- e_2 = distance from equivalent concrete section c.g. to section c.g.

□ From Euler–Bernoulli beam theory,

$$\triangleright M_{int} = EI\phi$$

Where,

$$\phi = \epsilon \downarrow t + \epsilon \downarrow c / h$$

E = Elastic modulus

I = Moment of inertia

$$\phi = \epsilon \downarrow t + \epsilon \downarrow c / h = \epsilon \uparrow * / y$$

$$\therefore M_{int} = EI \epsilon \uparrow * / y$$

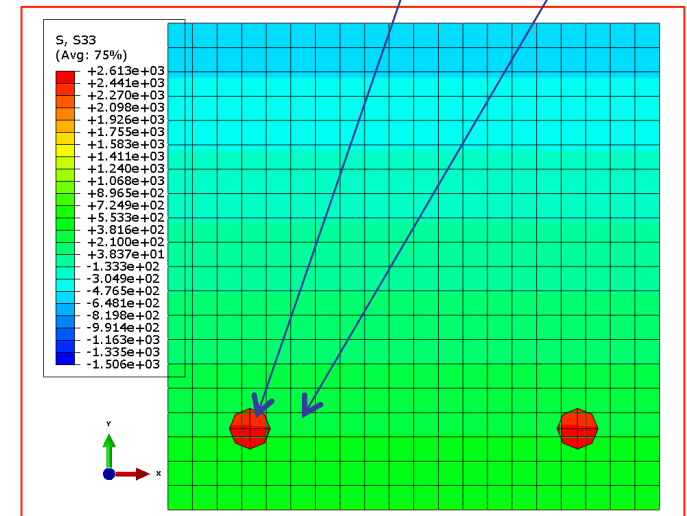
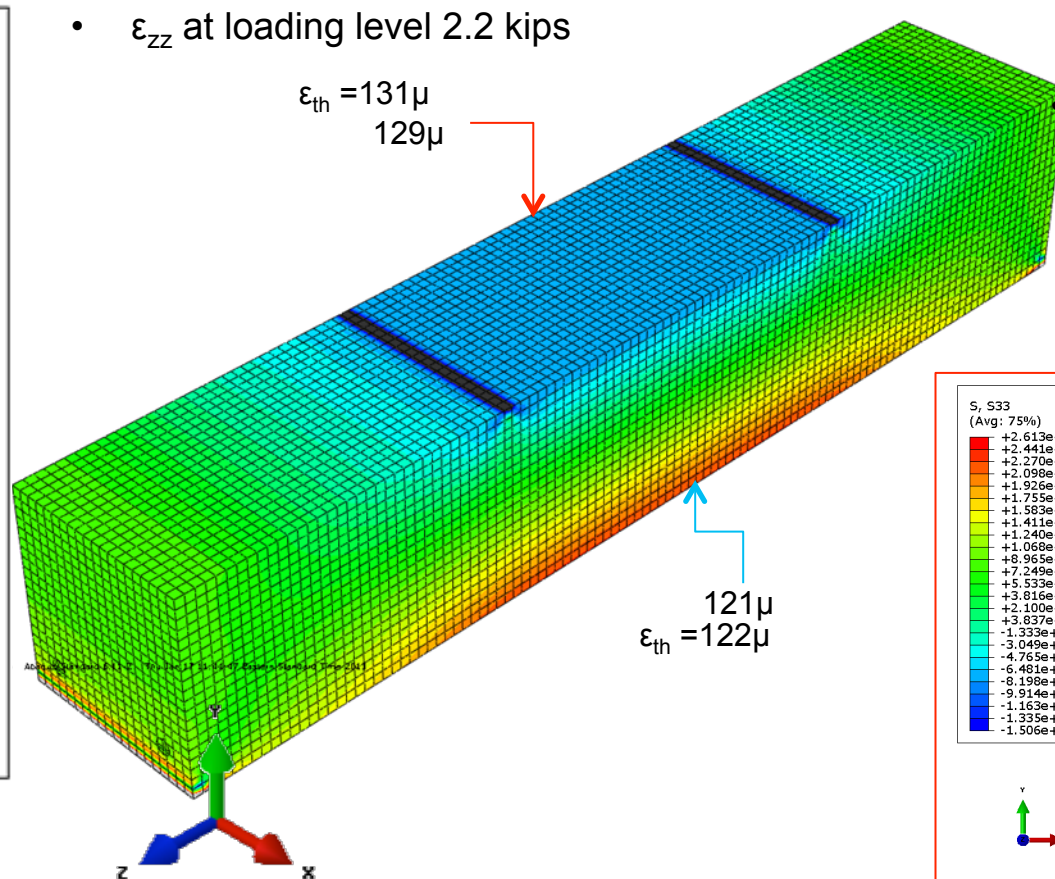
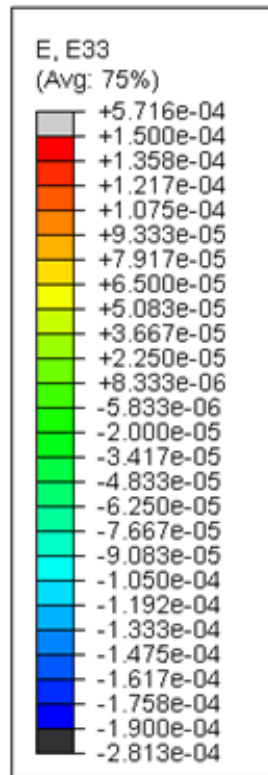
$$\epsilon \uparrow * = M_{int} \cdot y / EI$$

FE Model Response

▪ FEA results

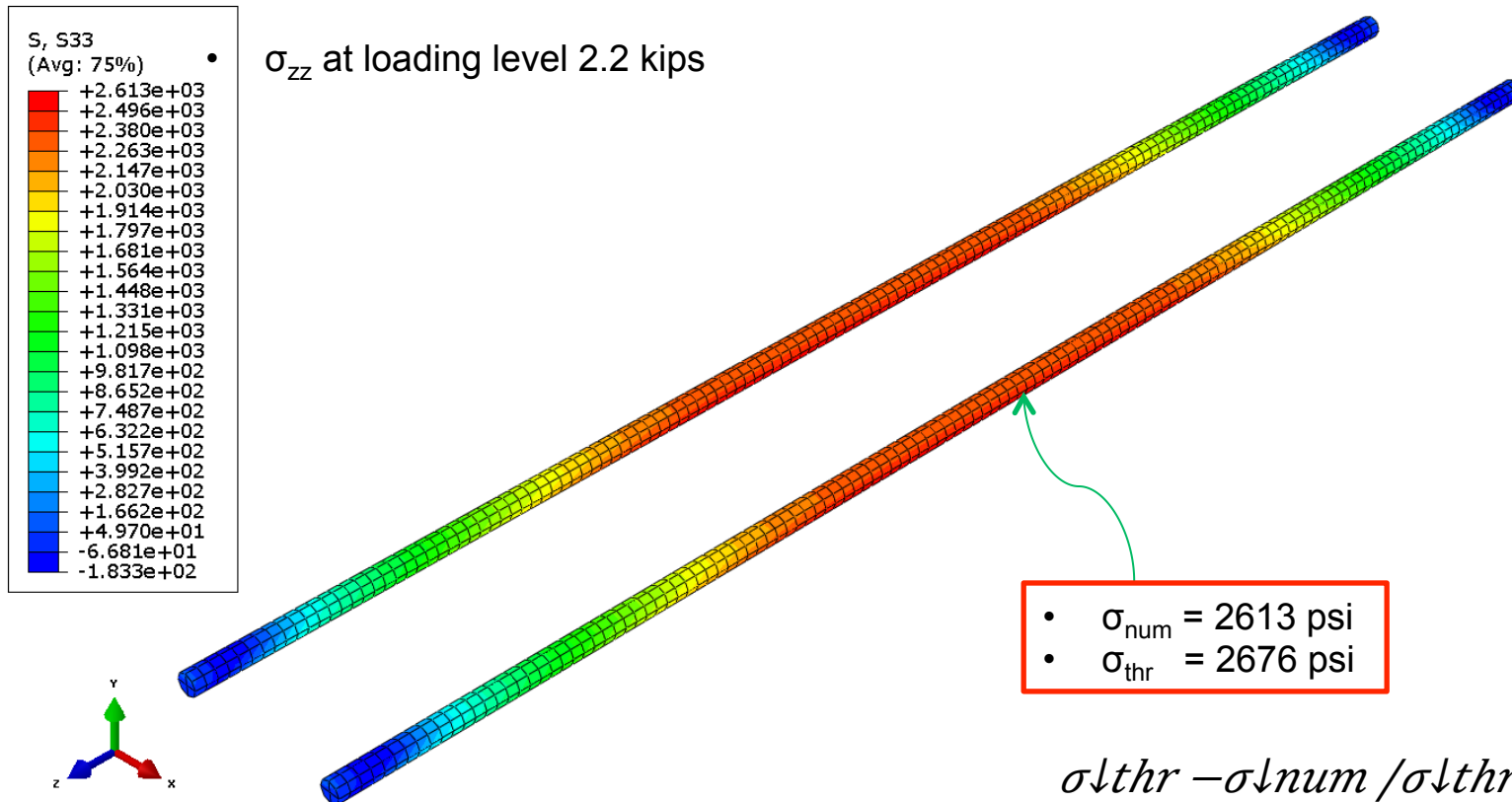
$$n = E \downarrow s / E \downarrow c = 30 / 4.59 = 6.53$$

$$n = E \downarrow s \varepsilon / E \downarrow c \varepsilon = \sigma \downarrow s / \sigma \downarrow c = 2330 / 357 = 6.53$$



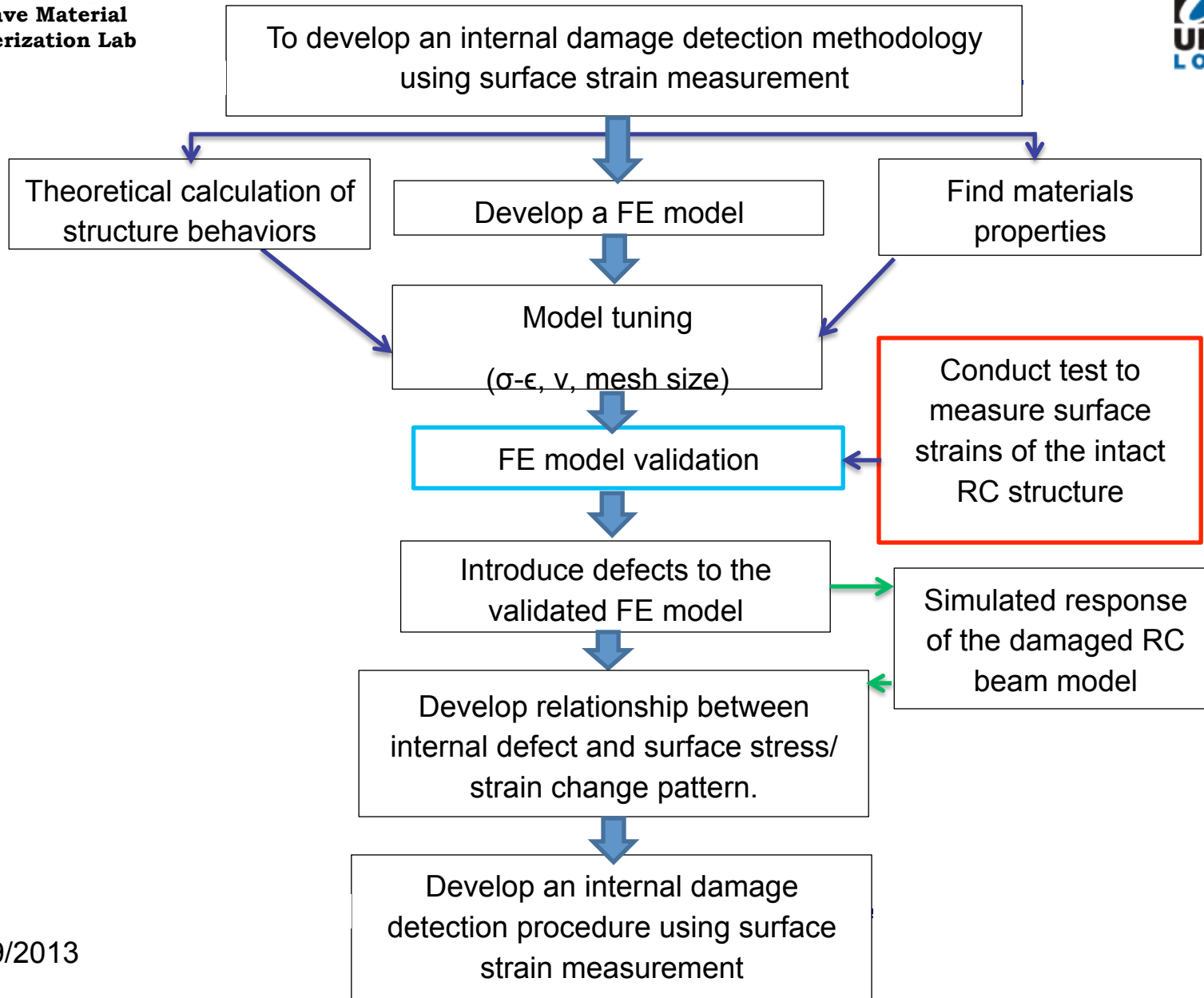
FE Model Response

- Rebar stress from FEA results:



$$\frac{\sigma_{thr} - \sigma_{num}}{\sigma_{thr}} \cdot 100 = 2.35 \%$$

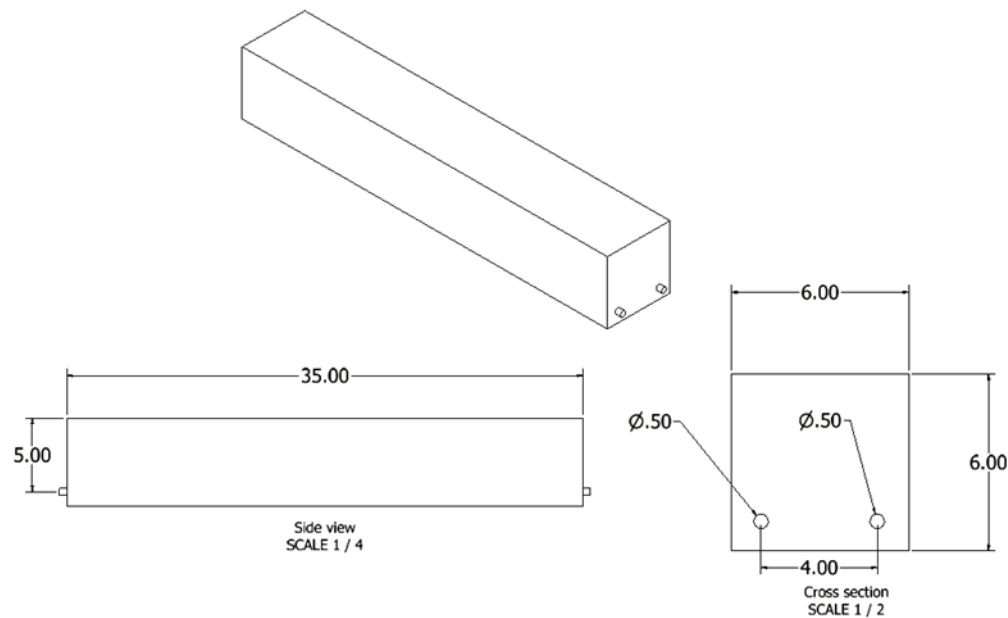
Research Roadmap



Experimental Work

▪ Specimen :

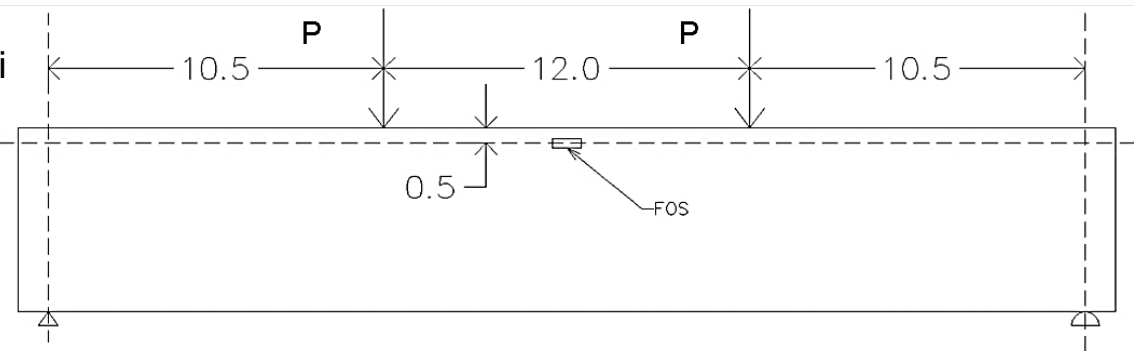
- 6" x 6" x 35" RC beam
- 2-#4 steel rebars in the tension zone
- Mix proportion of concrete (by volume) = 1:1.5: 3 (cement: sand : gravel)
- Water to cement ratio = 0.5 (by weight)



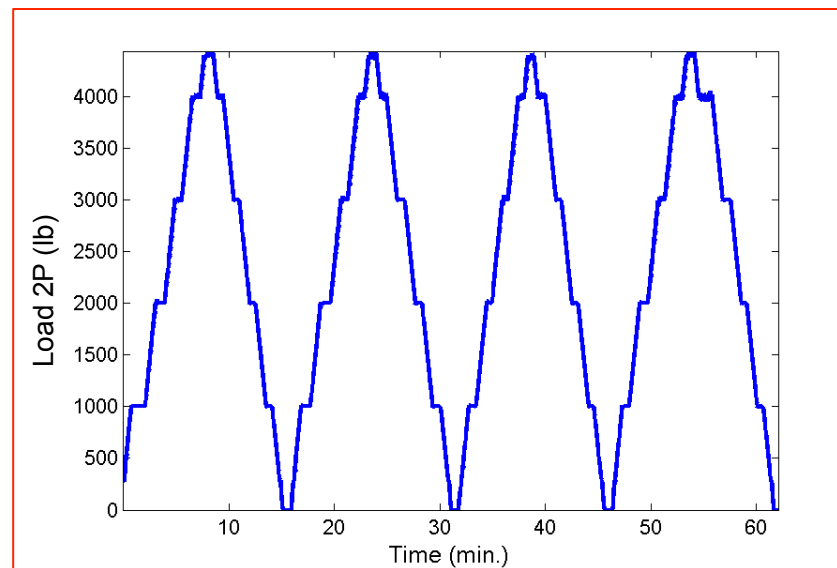
Experimental Work

Maximum load and loading levels:

- $\sigma_{cr} = 7.5 \sqrt{\sigma_{cu}} = 604.66 \text{ psi}$
- $M_{cr} = \sigma_{cr} I_g / y_t = 24.11 \text{ k-in}$
- $P_{max} = M_{cr} / l = 2.29 \text{ kips}$



- Loading level steps: 2.2 kips, 2.0 kips, 1.5 kips, 1.0 kip, and 0.5 kip



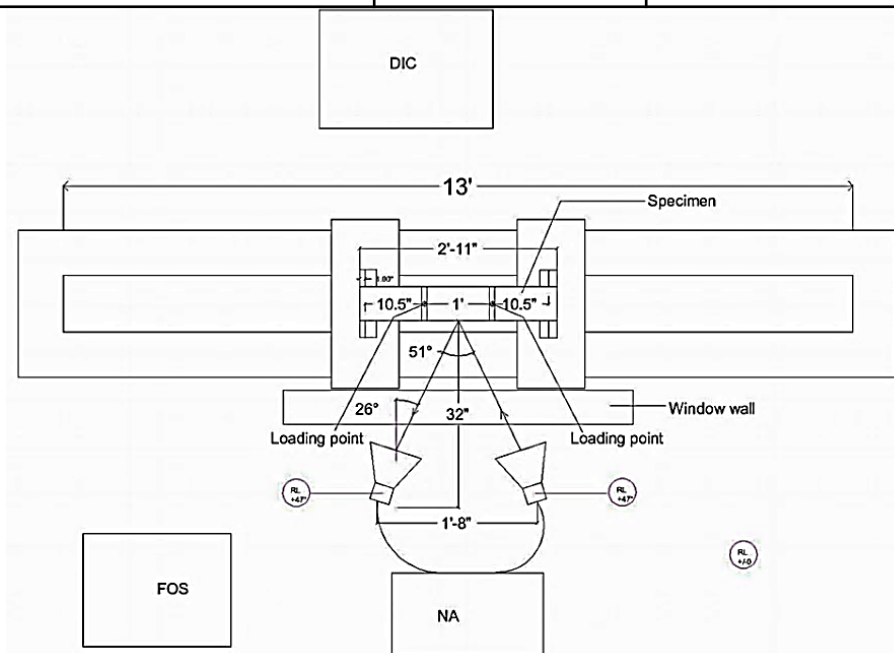
Experimental Work

▪ Test schedule

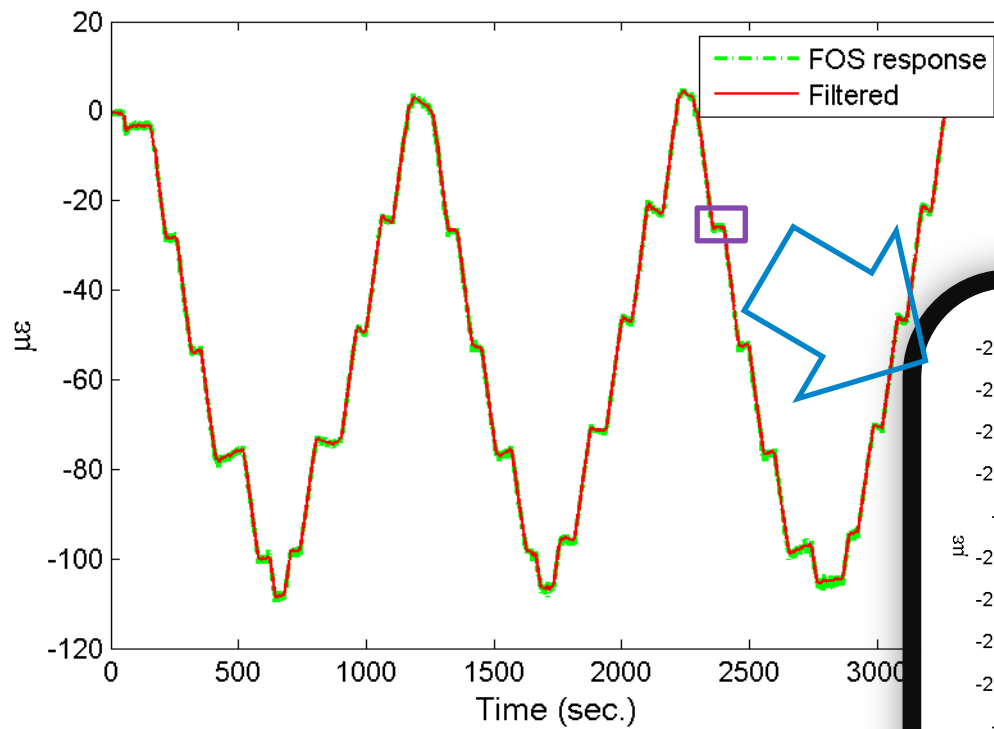
Experiment no.	Loading levels and cycles	Date	Sensors
Experiment 1	4 cycles, Loading levels → 0.5 k, 1.0 k, 1.5 k, 2.0 k, and 2.2 k	Aug. 1, 2012	DIC, FOS, and radar
Experiment 2	4 cycles, Loading levels → 0.5 k, 1.0 k, 1.5 k, 2.0 k, and 2.2 k	Sep. 27, 2012	FOS and radar
Experiment 3	4 cycles, Loading levels → 0.5 k, 1.0 k, 1.5 k, 2.0 k, and 2.2 k	Oct. 05, 2012	FOS and radar
Experiment 4	3 cycles, Loading levels → 0.5 k, 1.0 k, 1.5 k, 2.0 k, and 2.2 k	Jan. 25, 2013	FOS and radar

▪ Equipment:

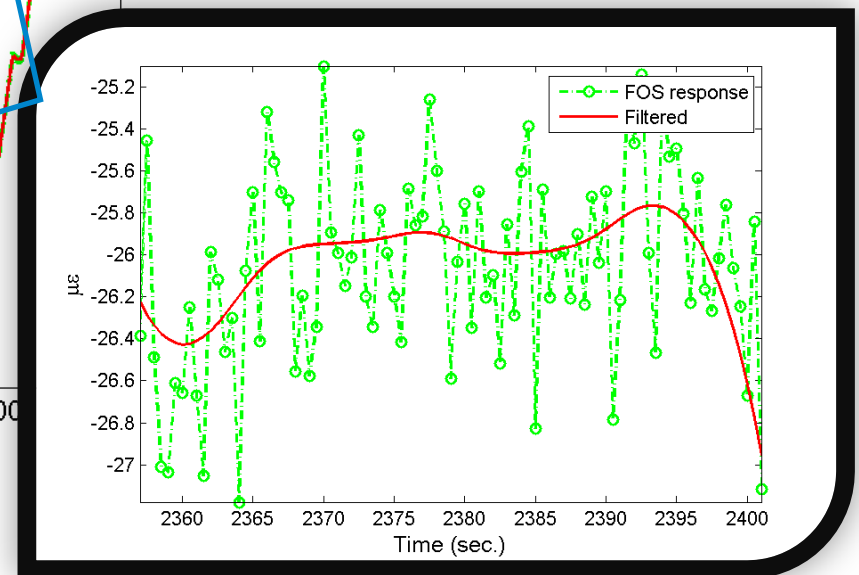
- Load cell:
 - ✓ Model Name: Lebow 3175
 - ✓ Maximum capacity → 50,000 lb.
- FOS:
 - ✓ Model name: os3110
 - ✓ Maximum capacity → +/- 2500 $\mu\epsilon$
- DIC:
 - ✓ Resolution → 4096 x 3072



- FOS measurement:

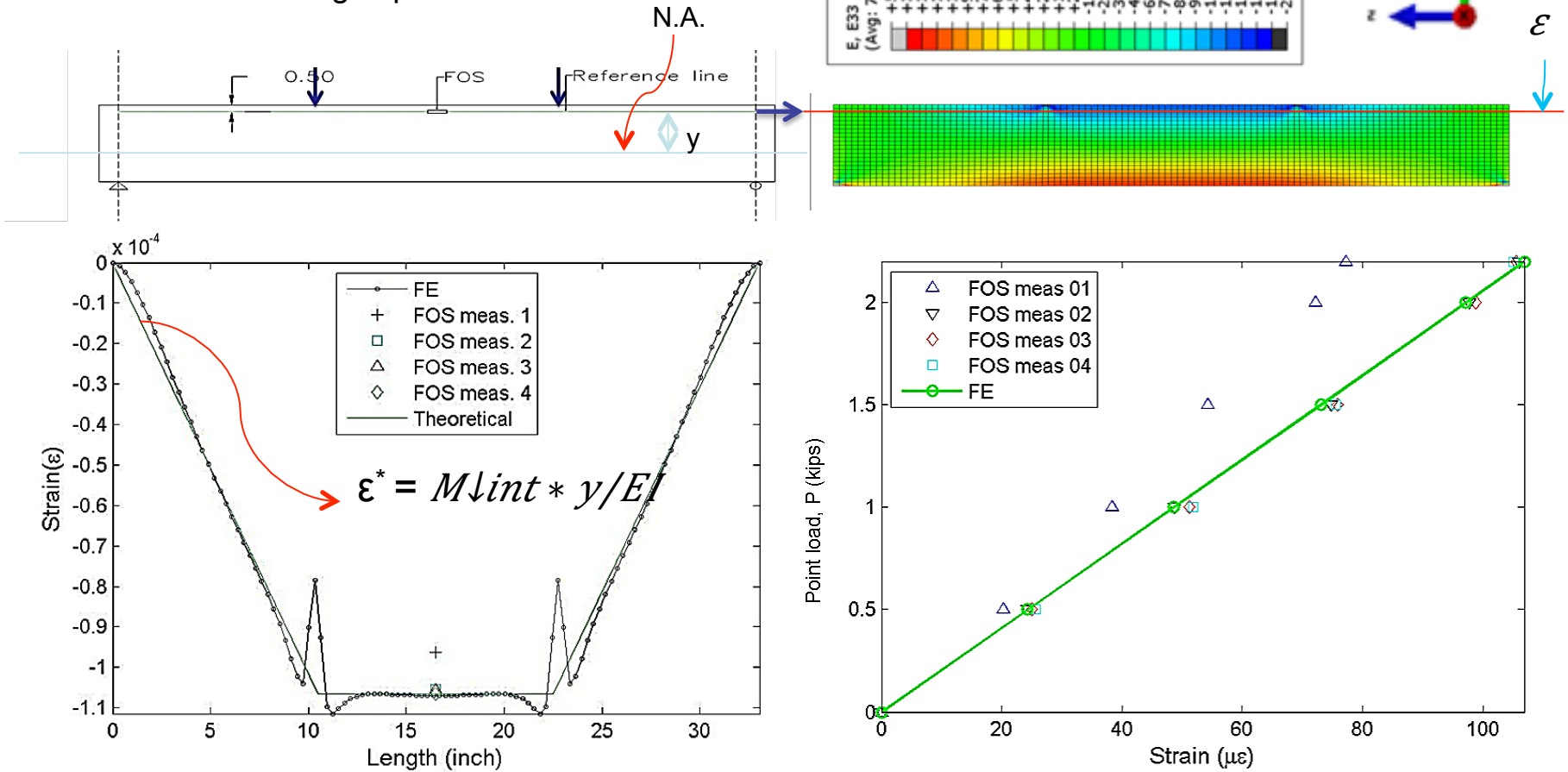


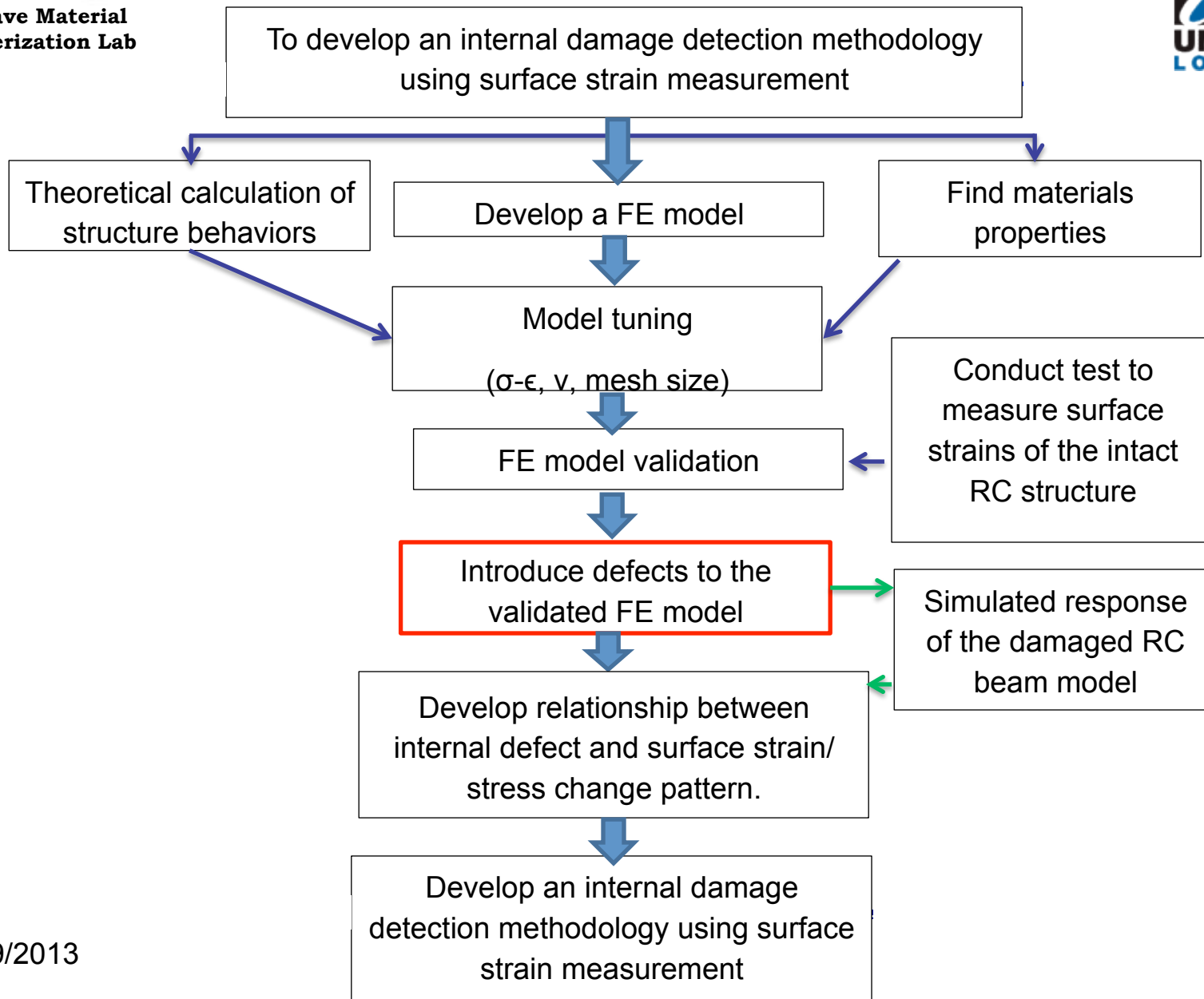
Experiment 4, FOS measurement



FE Model Validation

- Theoretical and FEA comparison
- Validation using experimental measurements

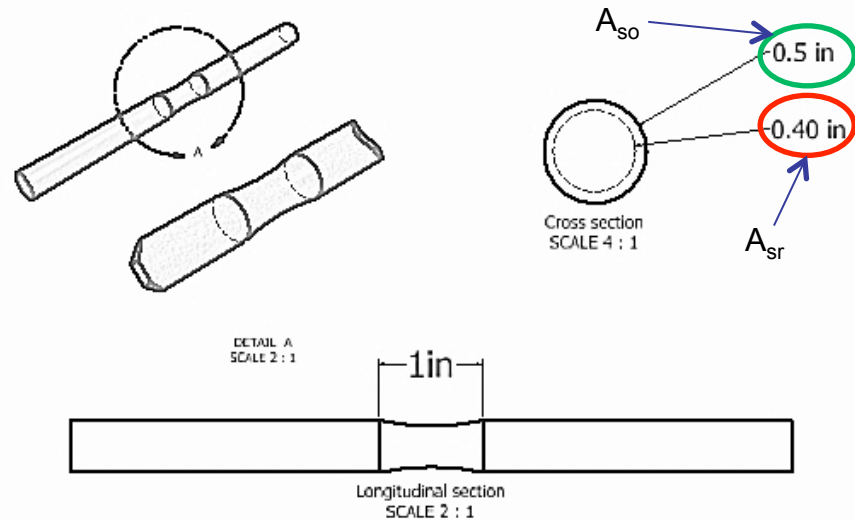




Damage Modeling

■ Definition of damage:

- Reduction of steel rebar cross section/volume
- To simulate rebar corrosion
- Cross sectional reduction, $\Delta A_s = A_{\downarrow so} - A_{\downarrow sr}$
 $A_{\downarrow so} * 100$
- Volume reduction, $\Delta V_s = V_{\downarrow so} - V_{\downarrow sr} / V_{\downarrow sc}$
 $* 100$



$\Delta A_s(\%)$	$V_{so} - V_{sr}(in^3)$	ΔV_s (1-in defect)	ΔV_s (5-in defect)
10	0.013	6.633	5.736
15	0.020	10.204	8.768
20	0.026	13.265	11.402
25	0.033	16.837	14.419
30	0.040	20.408	17.836
36	0.048	24.48	21.635

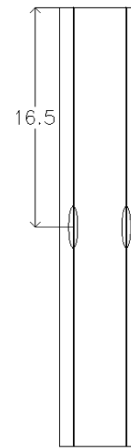


Damage Modeling

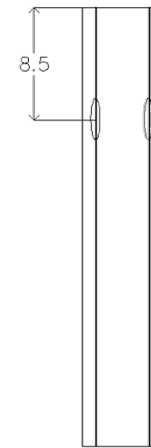
■ Artificial damage scenarios:

- (i) Type I
- (ii) Type II
- (iii) Type III
- (iv) Type IV

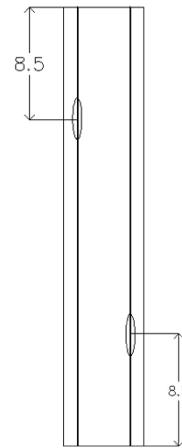
- Damage intensity, $\Delta A_s \rightarrow$ 36%, 30%, 25%, 20%, 15%, and 10%



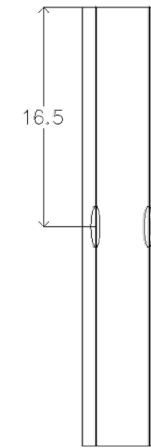
Type I



Type II



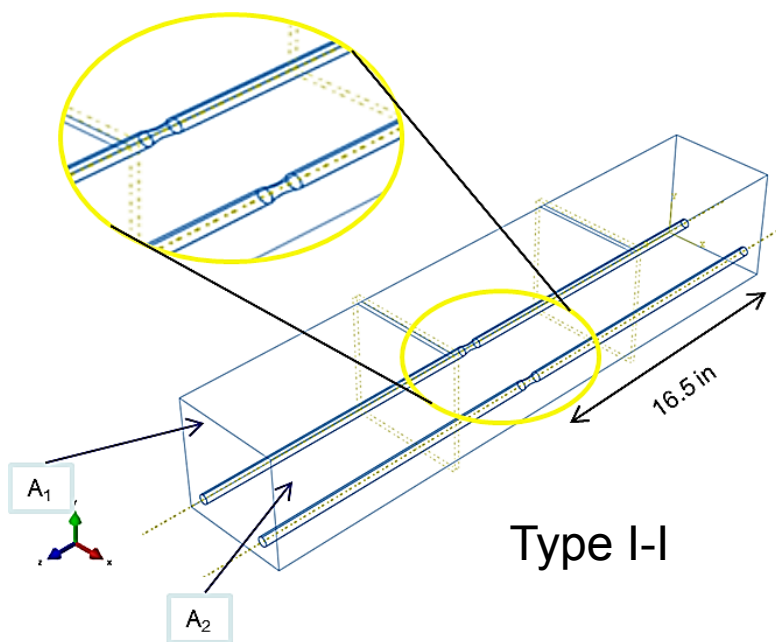
Type III



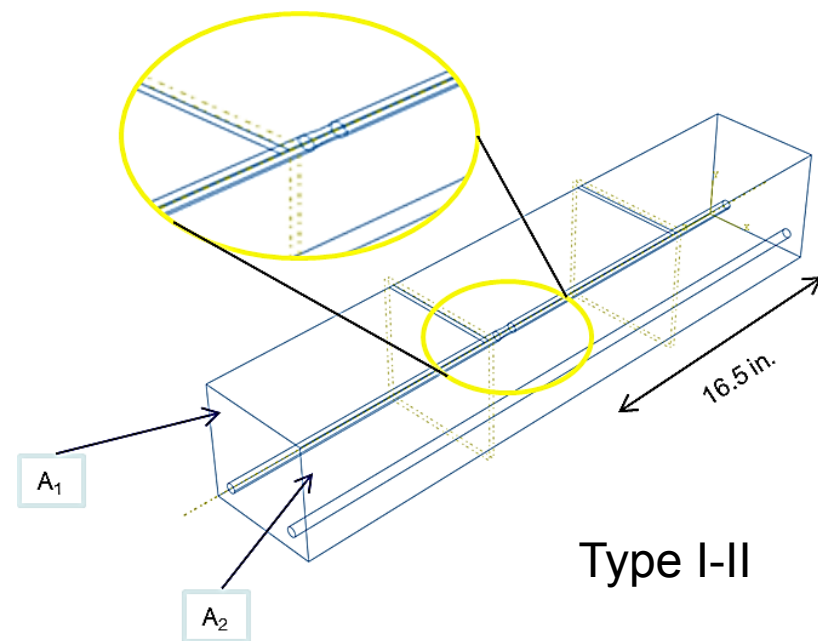
Type IV

Damage Modeling

- Subcategories of Type I are
 - (a) Type I-I (Symmetric) and
 - (b) Type I-II (Nonsymmetrical)
- Damage intensity, $\Delta A_s \rightarrow 36\%$, 30% , 25% , 20% , 15% , and 10%



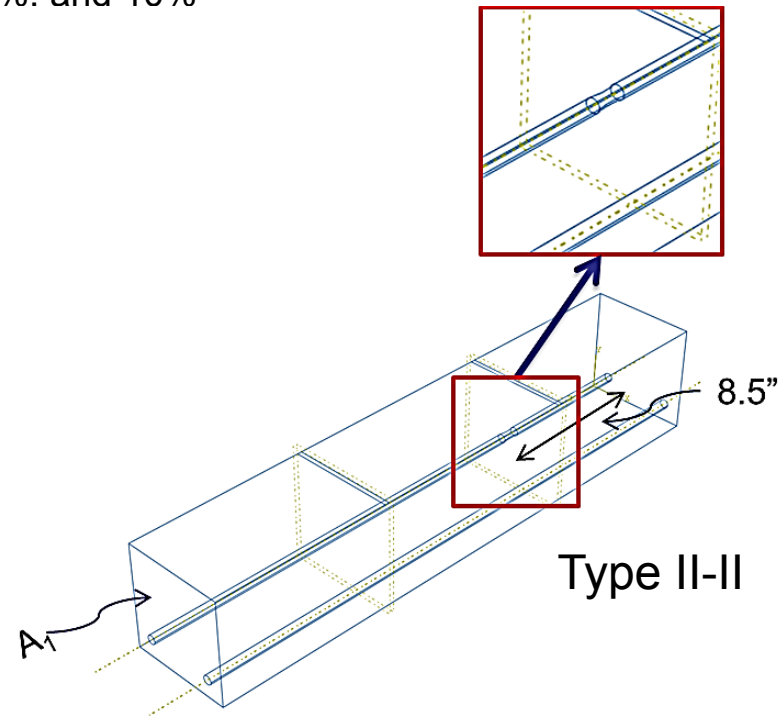
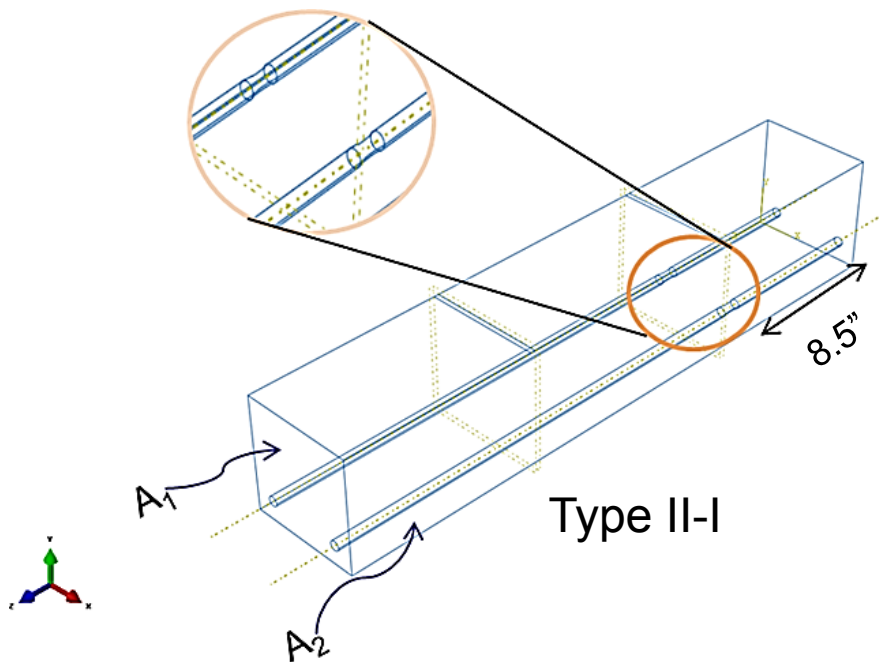
Type I-I



Type I-II

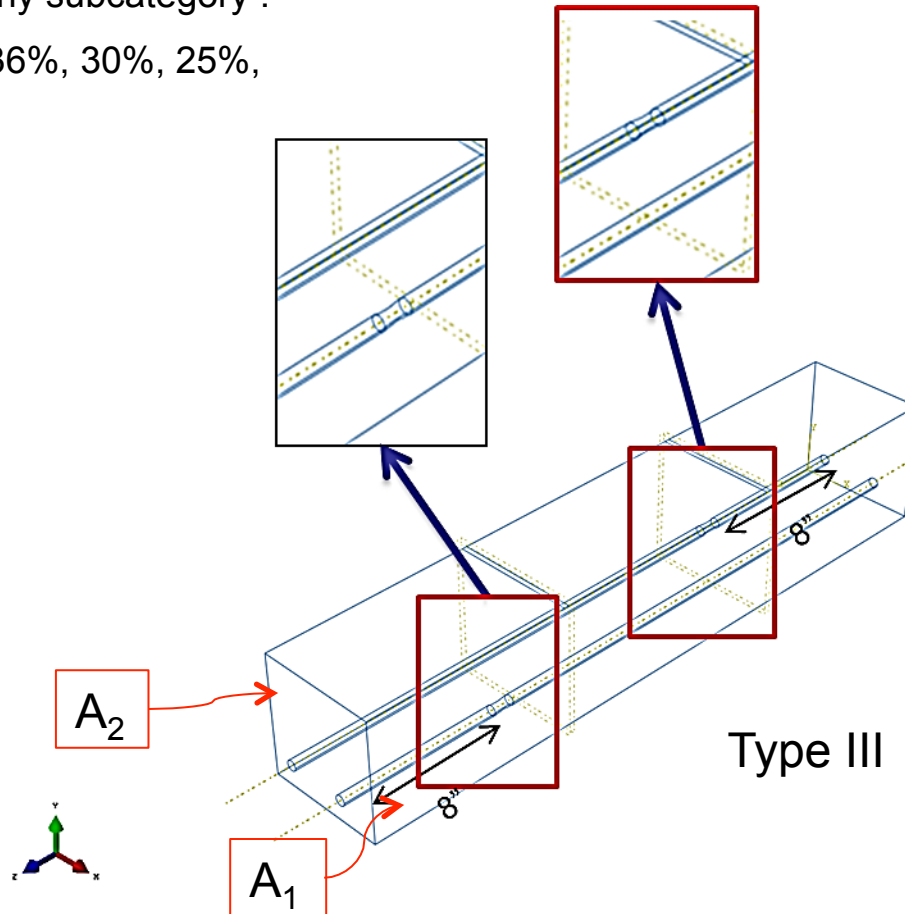
Damage Modeling

- Subcategories of Type II are
 - (a) Type II-I (Symmetric) and
 - (b) Type II-II (Nonsymmetrical)
- Damage intensity, $\Delta A_s \rightarrow 36\%$, 30% , 25% , 20% , 15% , and 10%



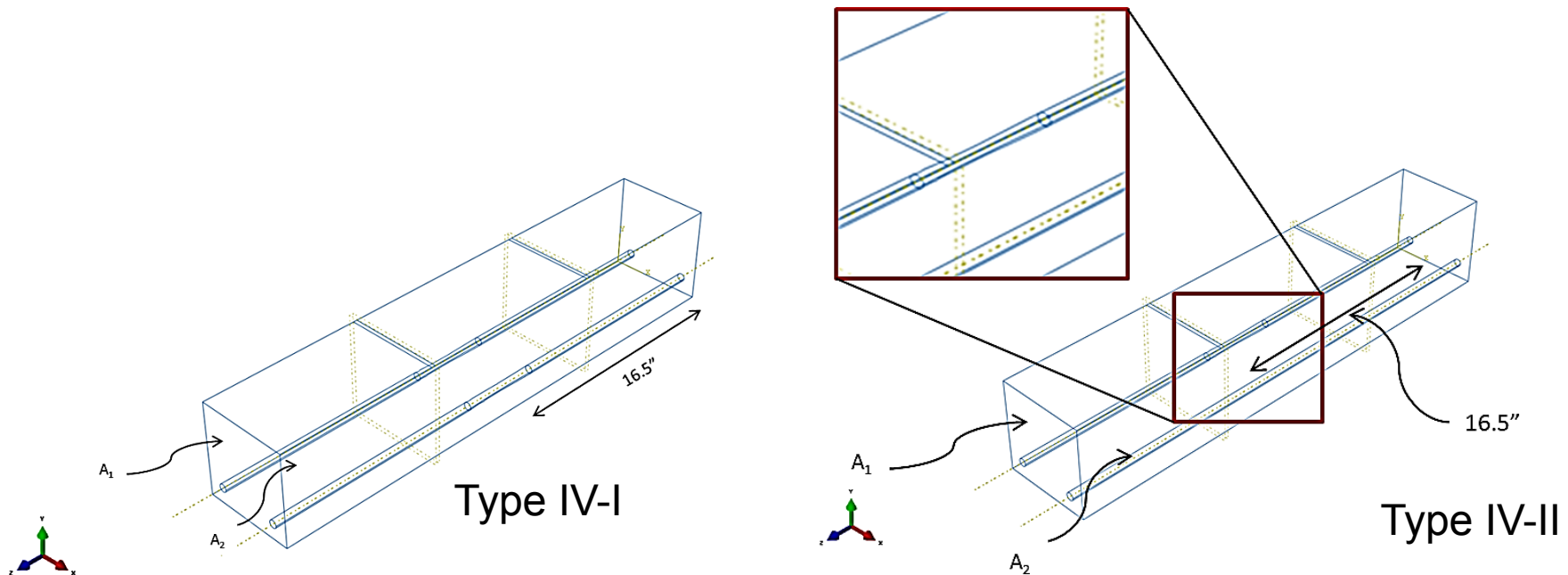
Damage Modeling

- Type III does NOT have any subcategory .
- Damage intensity, $\Delta A_s \rightarrow$ 36%, 30%, 25%, 20%, 15%, and 10%

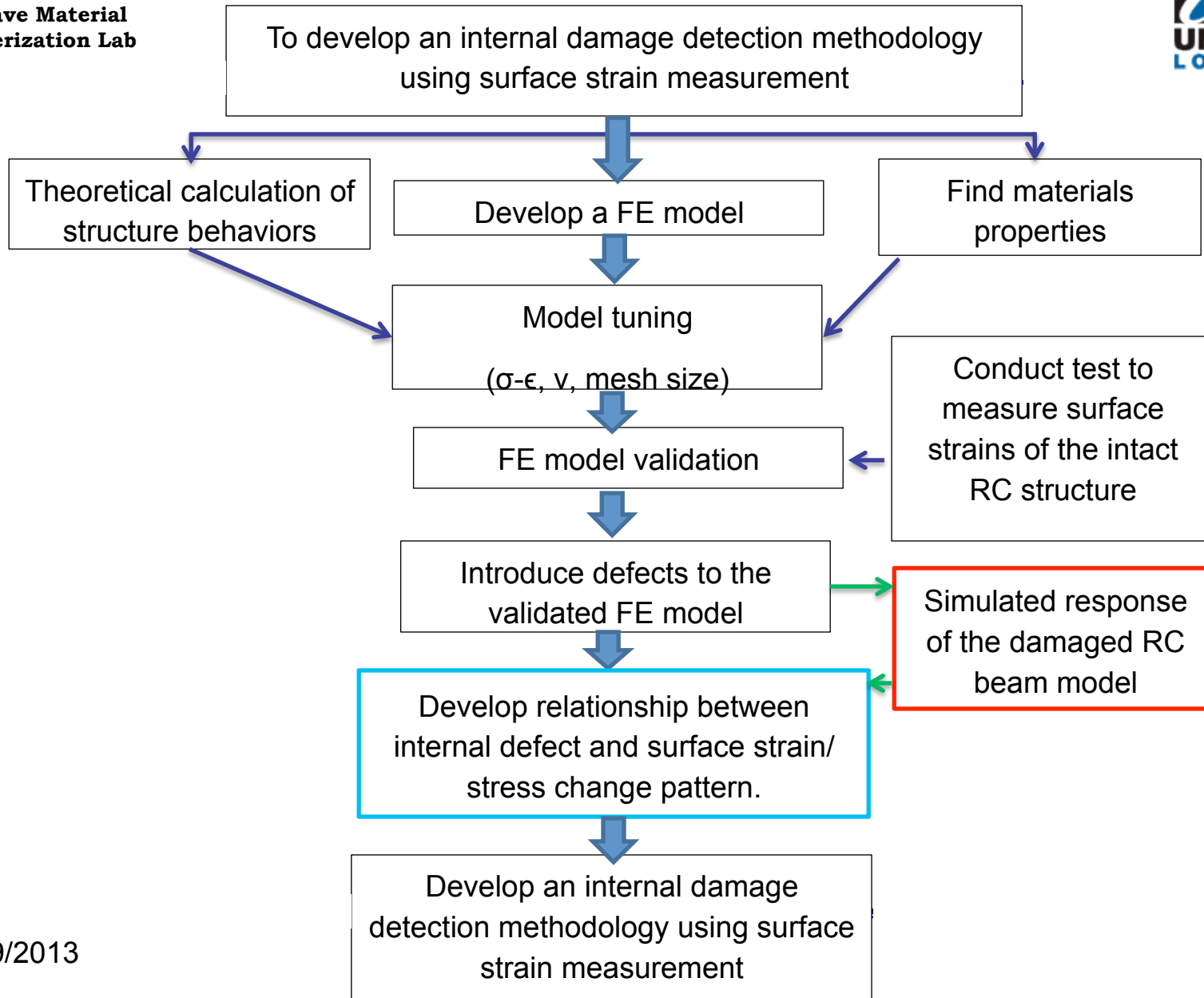


Damage Modeling

- Subcategories of Type IV are
 - (a) Type IV-I (Symmetric) and
 - (b) Type IV-II (Nonsymmetrical)
- Damage intensity, $\Delta A_s \rightarrow 36\%$, 30% , 25% , 20% , 15% , and 10%



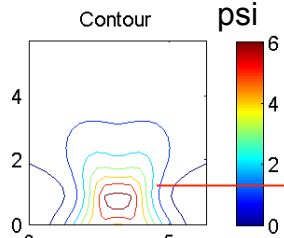
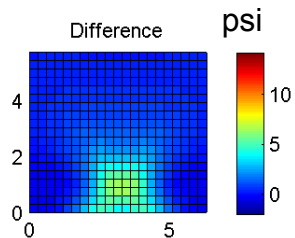
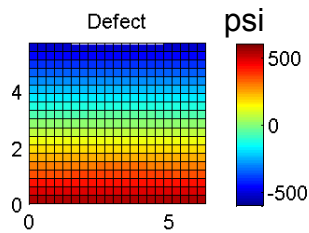
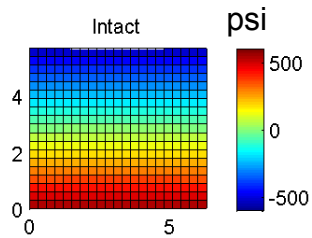
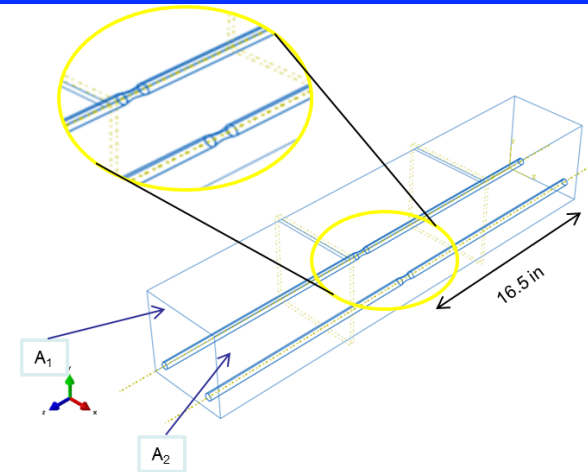
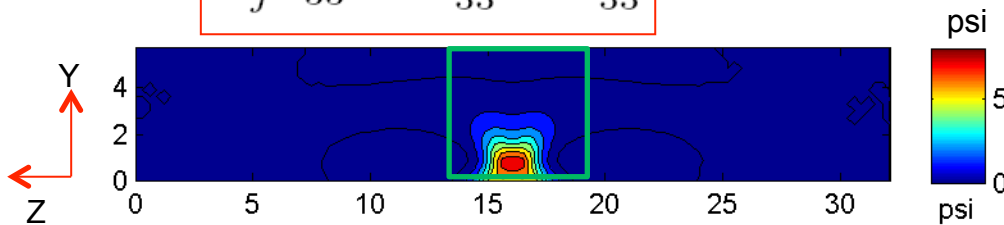
Research Roadmap



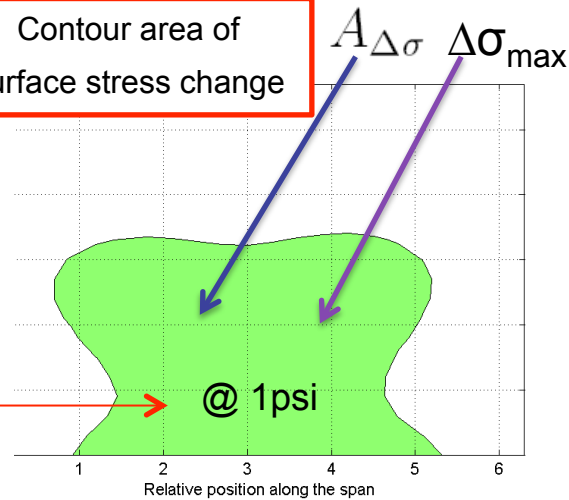
Surface Strain Change and Damage

- Surface stress change of Type I damage:

$$\Delta_j \tilde{\sigma}_{33} = \tilde{\sigma}_{33}^j - \tilde{\sigma}_{33}^o$$



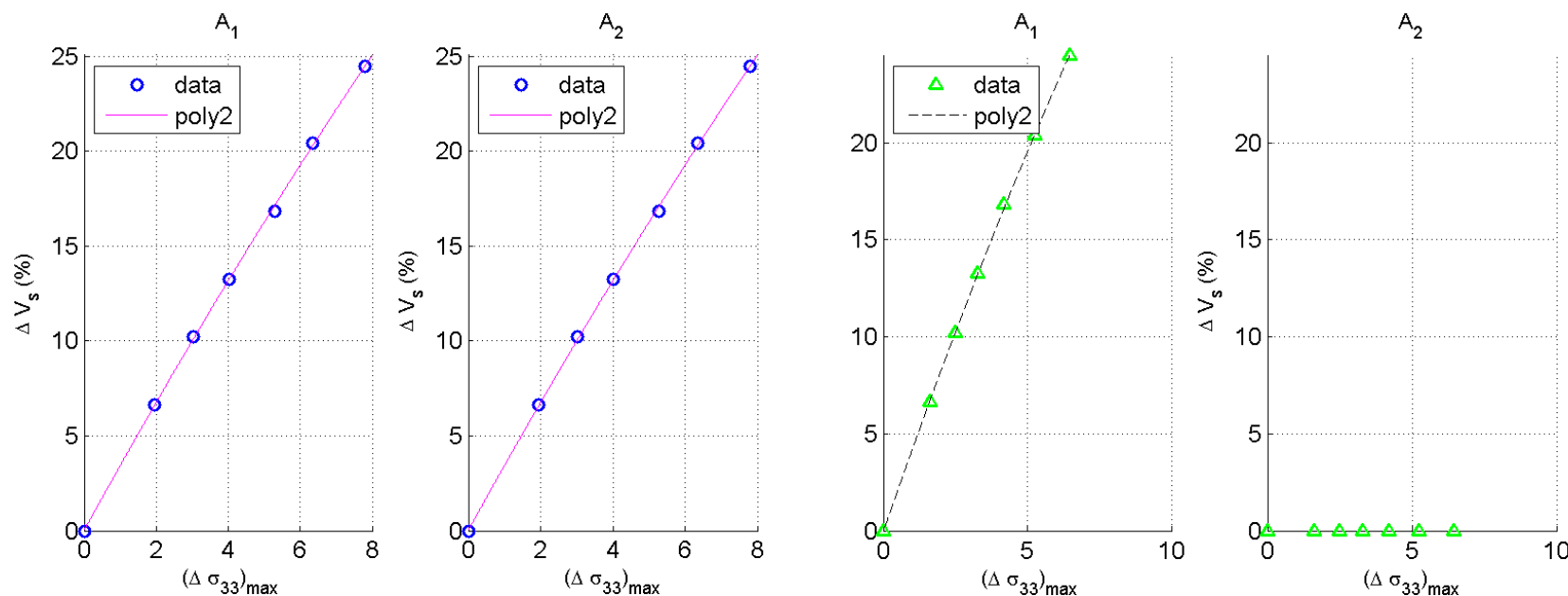
Contour area of surface stress change



ΔA_s (%)	ΔV_s (%)	$A_{\Delta\sigma}$
10	6.632653	3.139
15	10.20408	4.834
20	13.26531	6.085
25	16.83673	7.451
30	20.40816	8.461
36	24.4898	9.72

Surface Strain Change and Damage

- Relationships between $\Delta\sigma_{\max}$ and ΔV_s of Type I damage:
 → Difference of $\Delta\sigma_{\max}$ between side A_1 and A_2



Type I-I

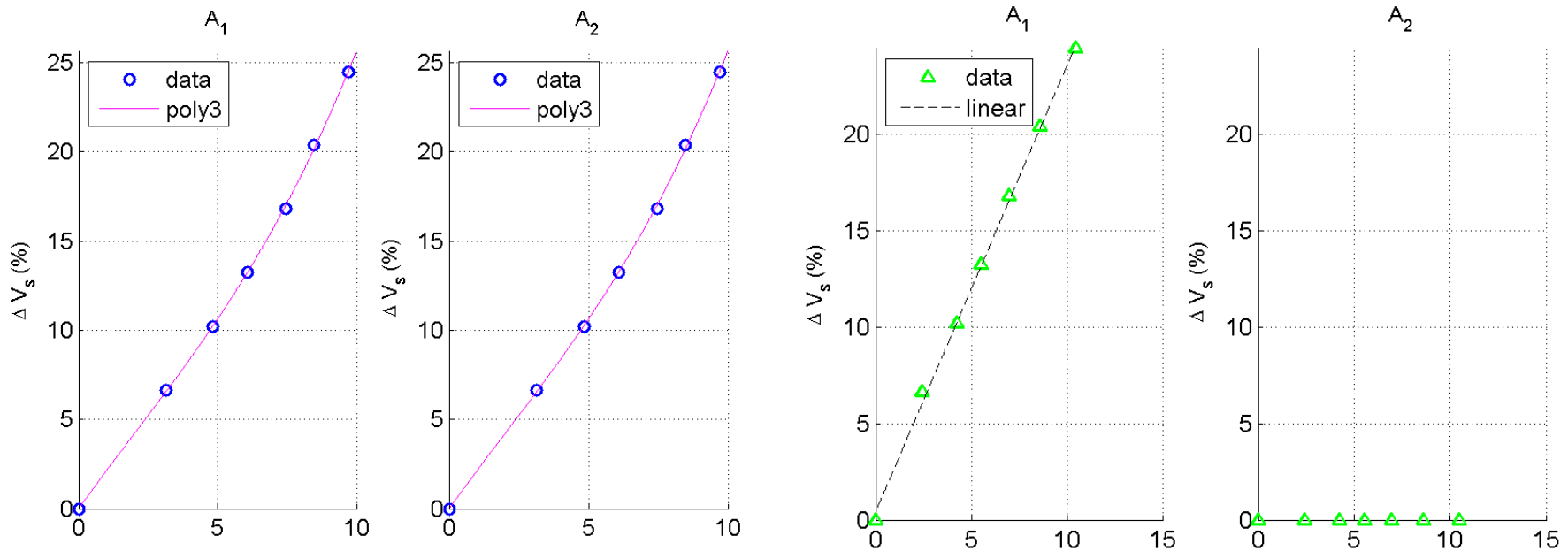
$$\Delta\sigma_{\max 1} \approx \Delta\sigma_{\max 2}$$

Type I-II

$$\Delta\sigma_{\max 1} \gg \Delta\sigma_{\max 2} \rightarrow 0$$

Surface Strain Change and Damage

- Relationships between $A_{\Delta\sigma}$ and ΔV_s of Type I damage:
→ Difference of $A_{\Delta\sigma}$ between side A_1 and A_2

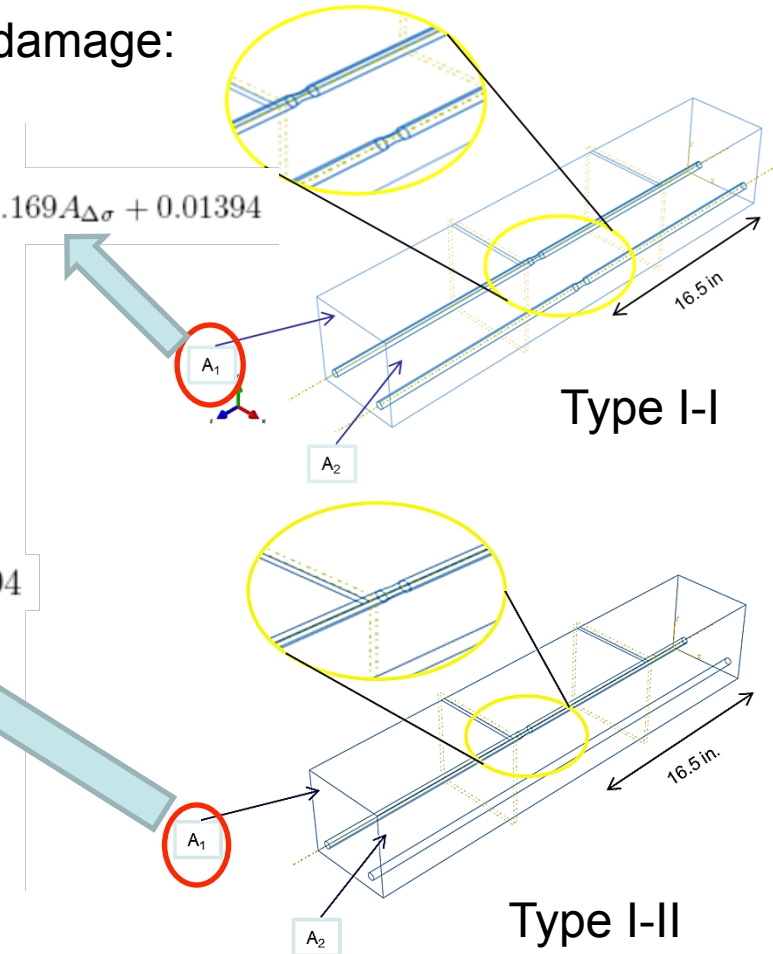
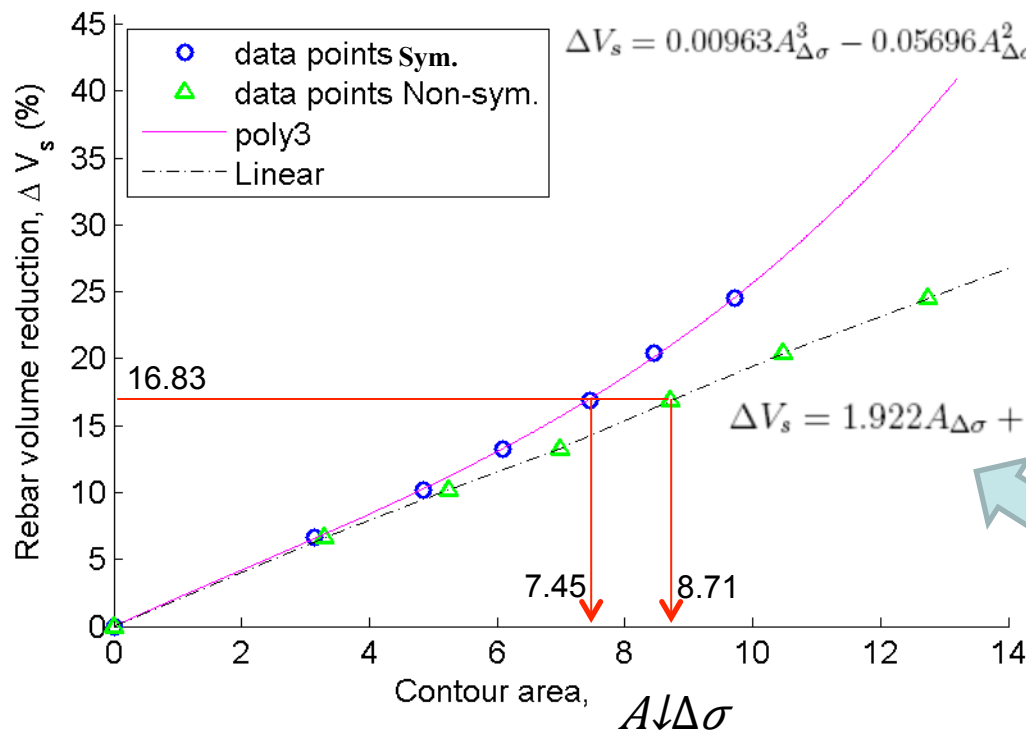


$A \downarrow$
 $\Delta\sigma$ Type I-I $A_{\Delta\sigma}^1 \downarrow A_{\Delta\sigma}^2$

$A \downarrow$
 $\Delta\sigma$ Type I-II $A_{\Delta\sigma}^1 \gg A_{\Delta\sigma}^2$
 $A_{\Delta\sigma}^2 \rightarrow 0$

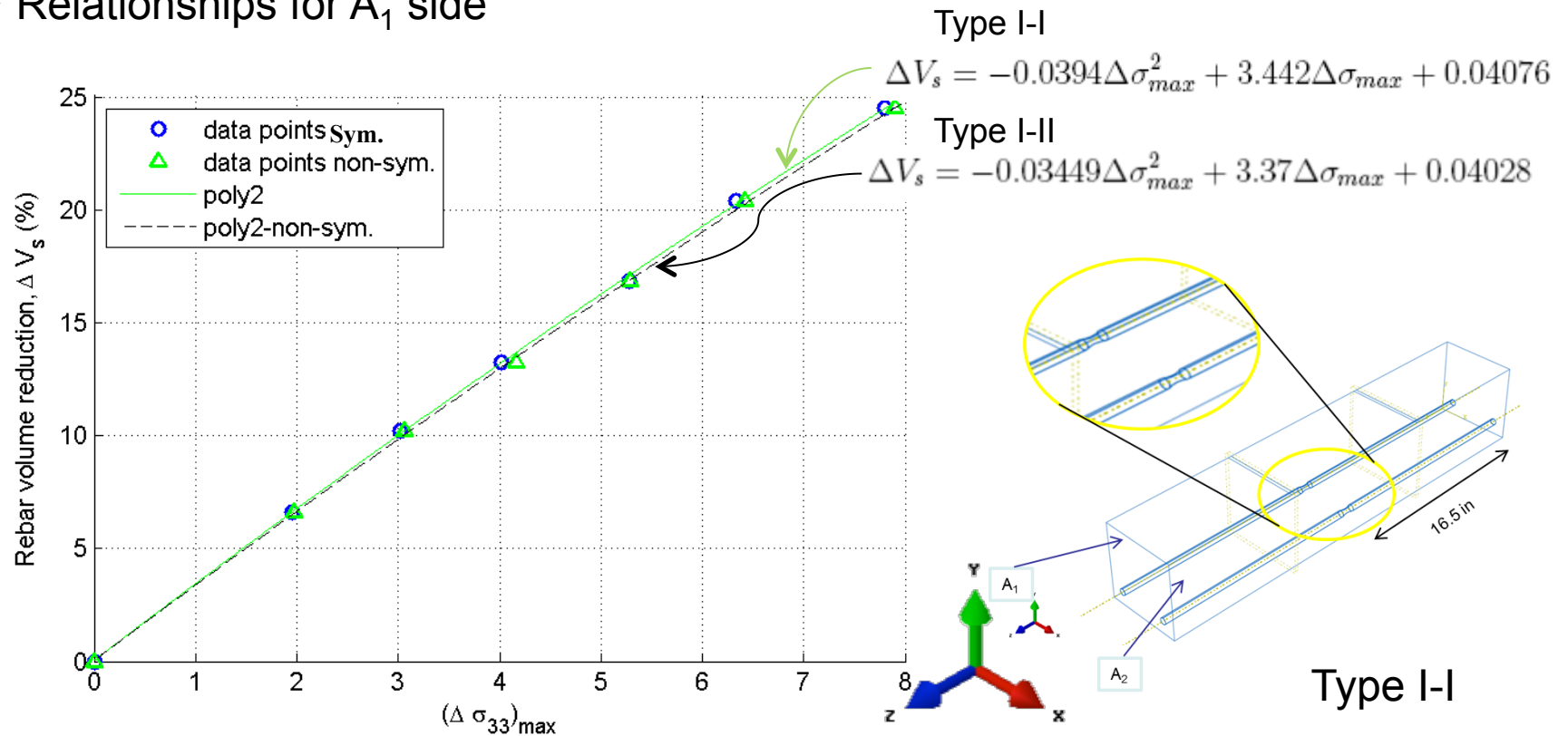
Surface Strain Change and Damage

- Relationship between $A_{\Delta\sigma}$ and ΔV_s of Type I damage:
→ Relationships for A_1 side



Surface Strain Change and Damage

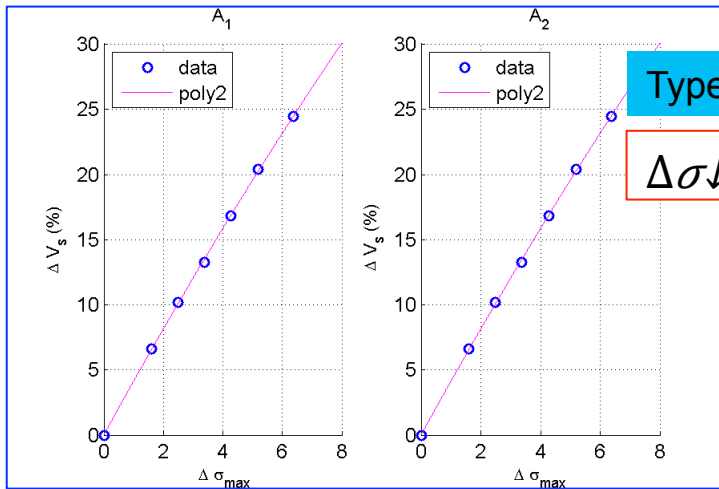
- Relationships between $\Delta\sigma_{max}$ and ΔV_s of Type I damage:
→ Relationships for A_1 side



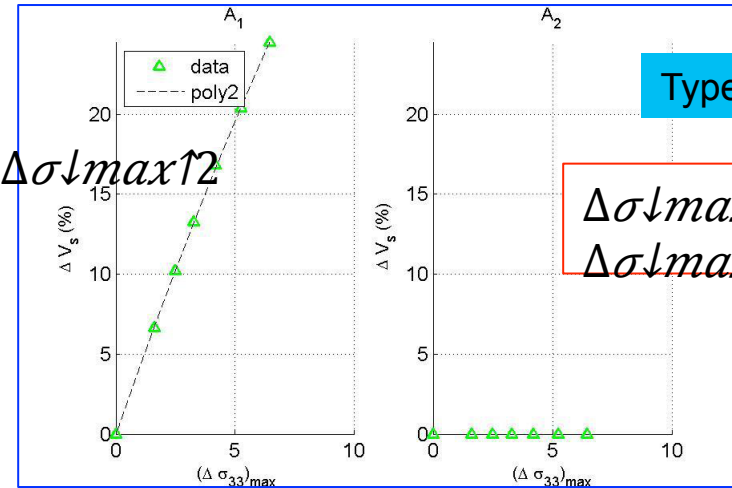
Surface Strain Change and Damage

- Relationship among $A_{\Delta\sigma}$, $\Delta\sigma_{max}$, and ΔV_s of Type II damage:

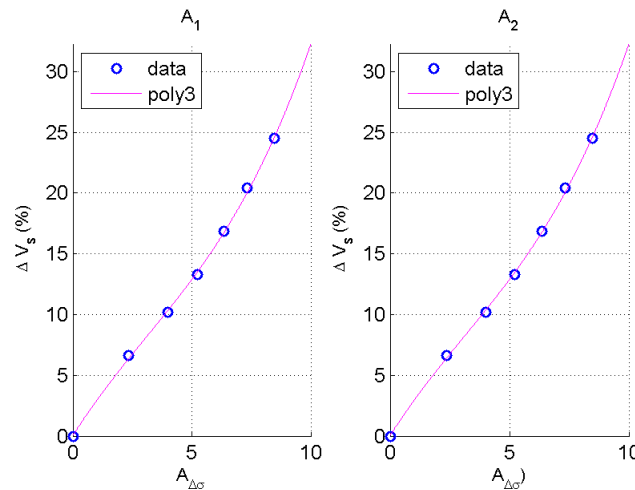
→ Difference of $A_{\Delta\sigma}$ between side A_1 and A_2



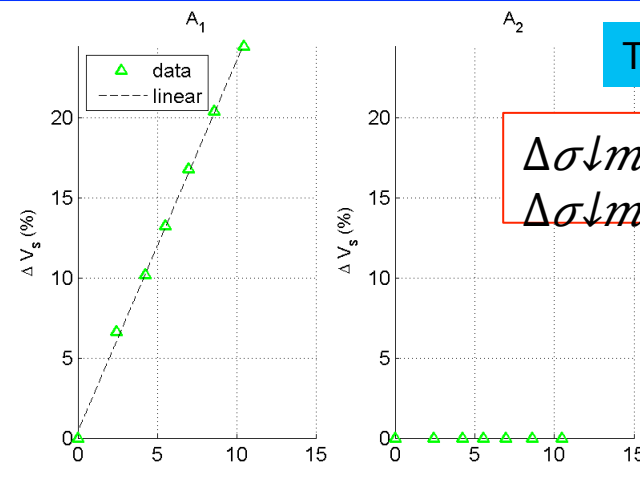
Type II-I
 $\Delta\sigma_{max1} \approx \Delta\sigma_{max2}$



Type II-II
 $\Delta\sigma_{max1} \gg \Delta\sigma_{max2} \rightarrow 0$



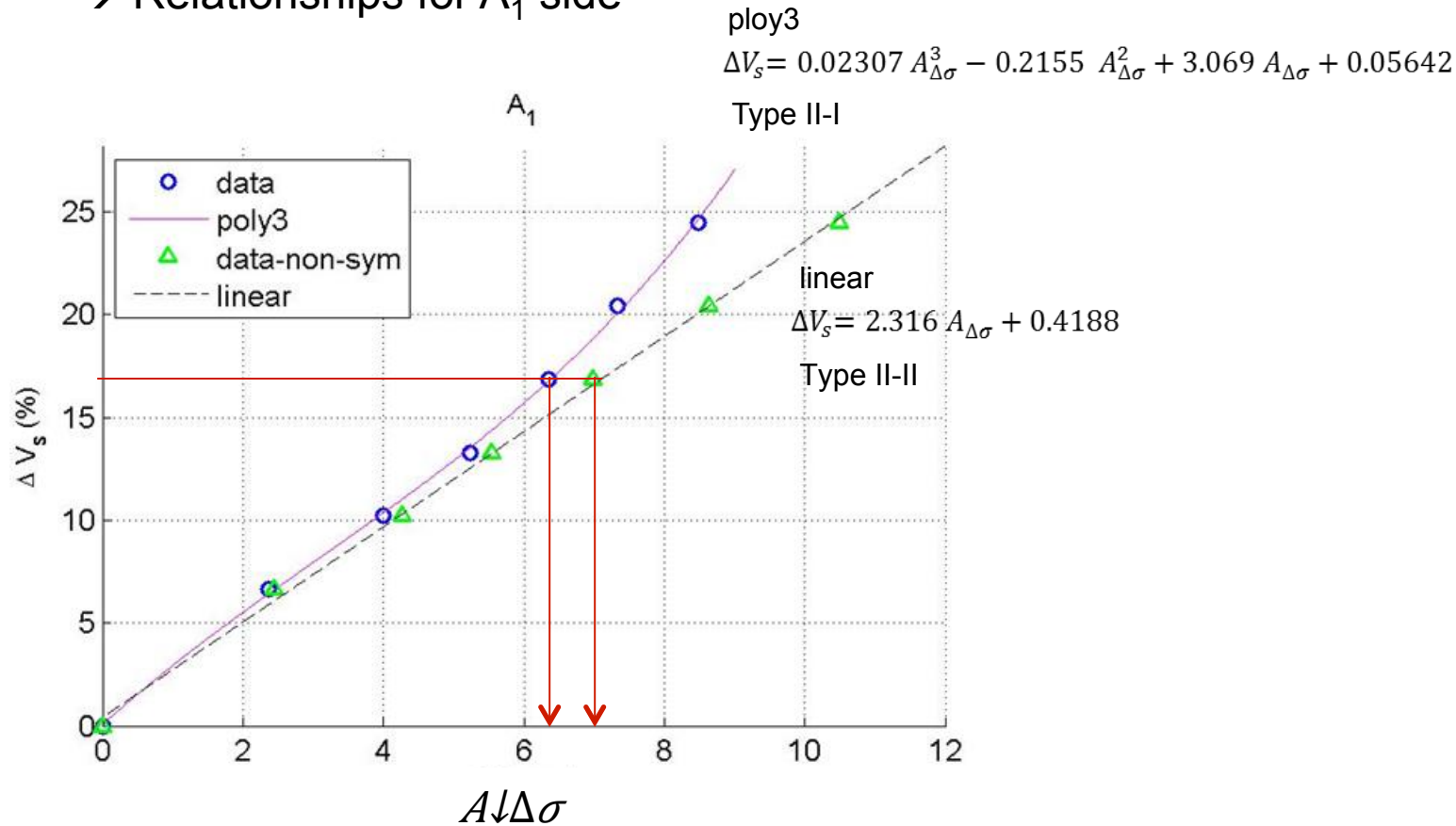
Type II-I
 $A_{\Delta\sigma}^1 \approx A_{\Delta\sigma}^2$



Type II-II
 $\Delta\sigma_{max1} \gg \Delta\sigma_{max2} \rightarrow 0$

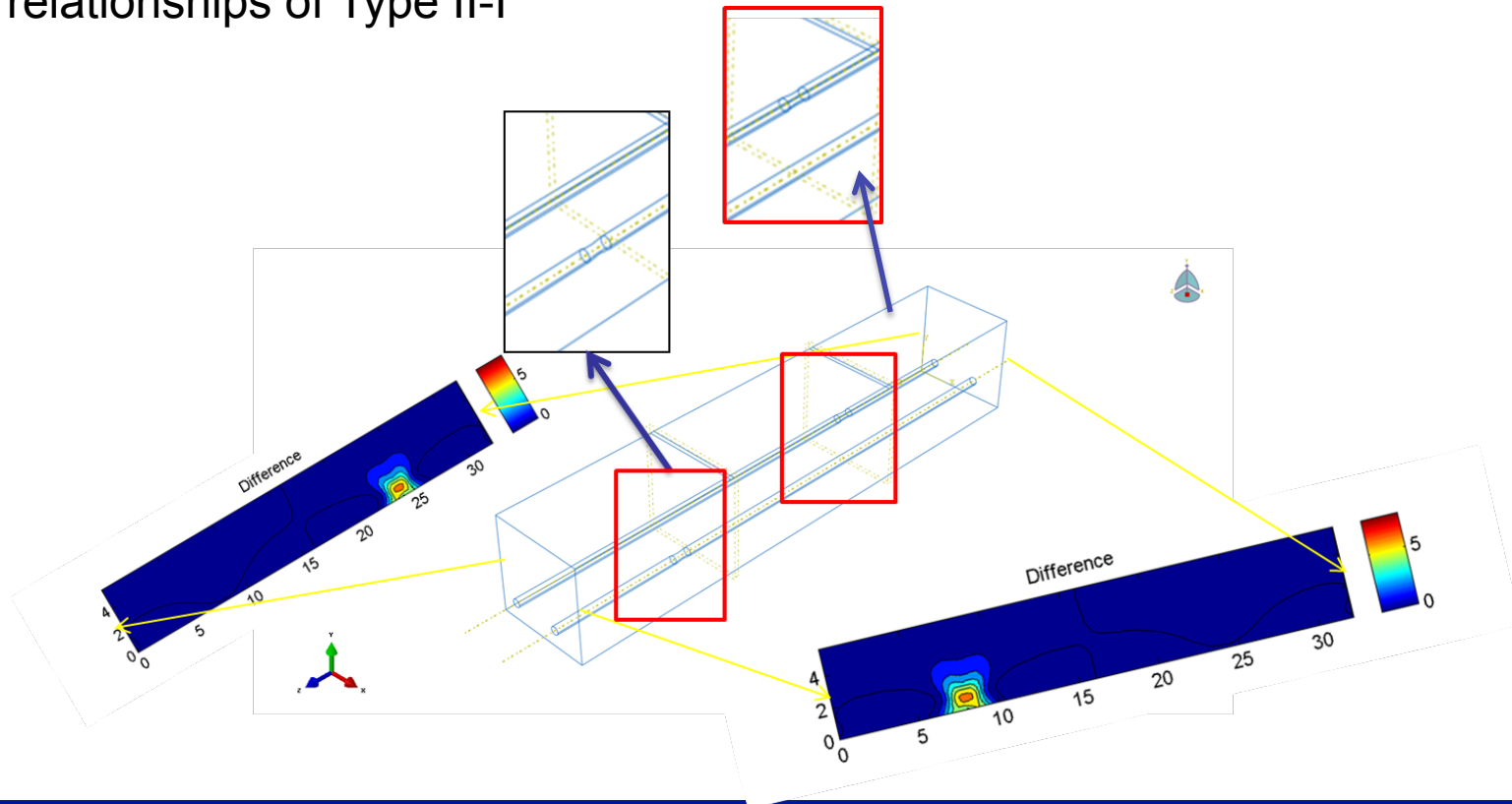
Surface Strain Change and Damage

- Relationships between $A_{\Delta\sigma}$ and ΔV_s of Type II defect:
→ Relationships for A_1 side



Surface Strain Change and Damage

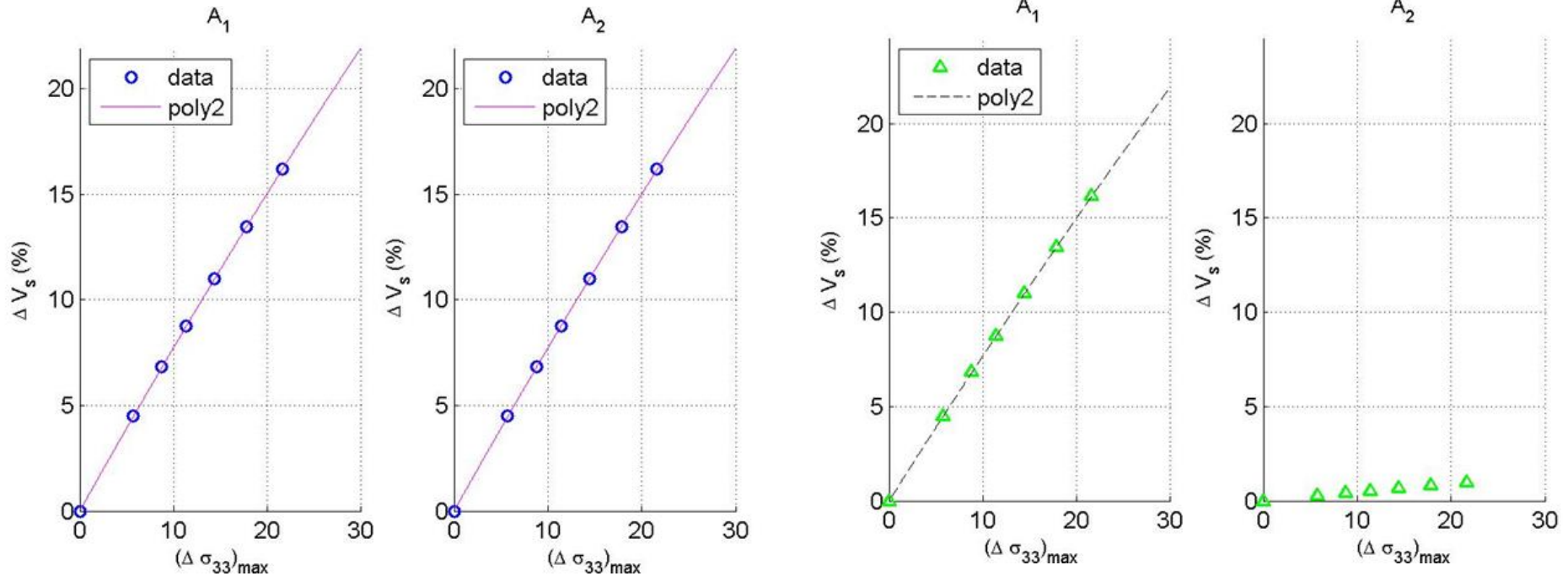
- Surface stress change of defect Type III:
 - Relationships among $A_{\Delta\sigma}$, $\Delta\sigma_{\max}$, and ΔV_s in Type III follow relationships of Type II-I



Surface Strain Change and Damage

- Relationships between $\Delta\sigma_{\max}$ and ΔV_s of Type IV defect:

→ Difference of $\Delta\sigma_{\max}$ between side A_1 and A_2



Type IV-I

$$\Delta\sigma_{\max 1} \approx \Delta\sigma_{\max 2}$$

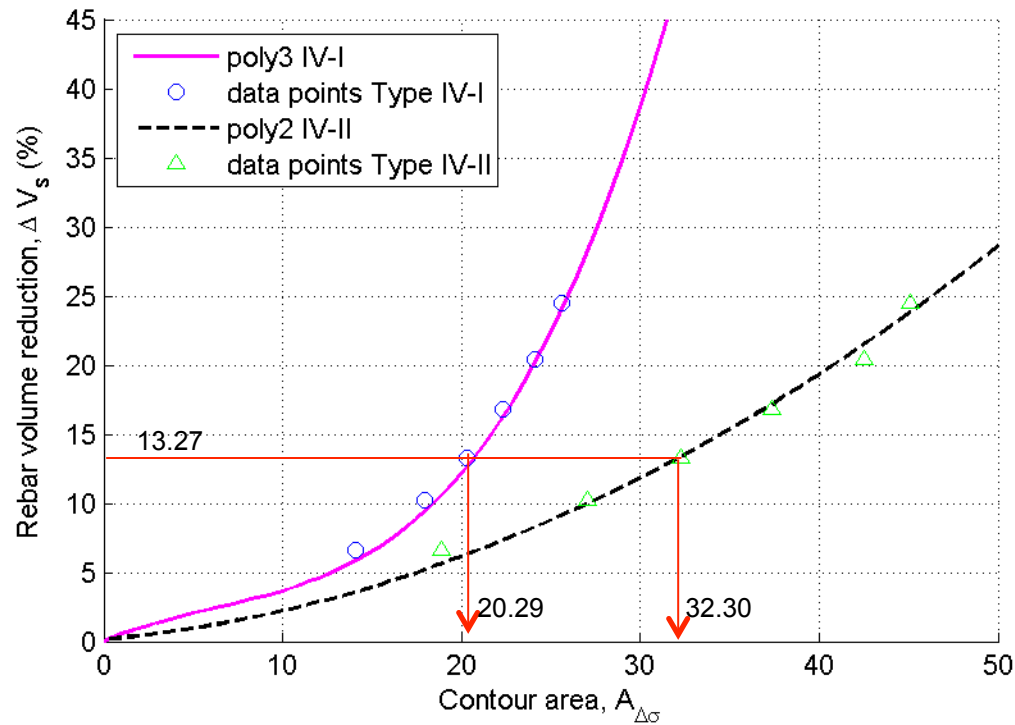
Type IV-II

$$\Delta\sigma_{\max 1} \gg \Delta\sigma_{\max 2}$$

Surface Strain Change and Damage

- Relationship between $A_{\Delta\sigma}$ and ΔV_s of Type IV defect:
 - Type IV-I, $\Delta V_s = 0.002 A_{\Delta\sigma}^3 - 0.0416 A_{\Delta\sigma}^2 + 0.5687 A_{\Delta\sigma} - 0.002163$

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Surface Strain Change and Damage

- Relationships among ΔV_s , $A_{\Delta\sigma}$, and $\Delta\sigma_{\max}$

$$\Delta V_s = p A_{\Delta\sigma}^3 + q A_{\Delta\sigma}^2 + r A_{\Delta\sigma} + C1$$

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Co-efficient Defect types	p	q	r	C1
Type I-I	0.00963	-0.0569	2.1690	0.0139
Type I-II	0.00000	0.0000	1.9220	0.0940
Type II-I	0.02307	0.2155	3.0690	0.0564
Type II-II	0.00000	0.0000	2.3160	0.4188
Type III	0.02307	0.2155	3.0690	0.0564
Type IV-I	0.00200	-0.0416	0.5687	-0.00216
Type IV-II	0.00000	0.0080	0.1800	0.1344

Co-efficient Defect types	A	B	C2
Type I-I	-0.0394	3.4420	0.04076
Type I-II	-0.03449	3.3700	0.04028
Type II-I	-0.05026	4.1590	0.03931
Type II-II	-0.07840	4.3070	0.06134
Type III	-0.07840	4.3070	0.06134
Type IV-I	-0.00208	0.7823	0.00674
Type IV-II	-0.00183	0.7849	0.00622

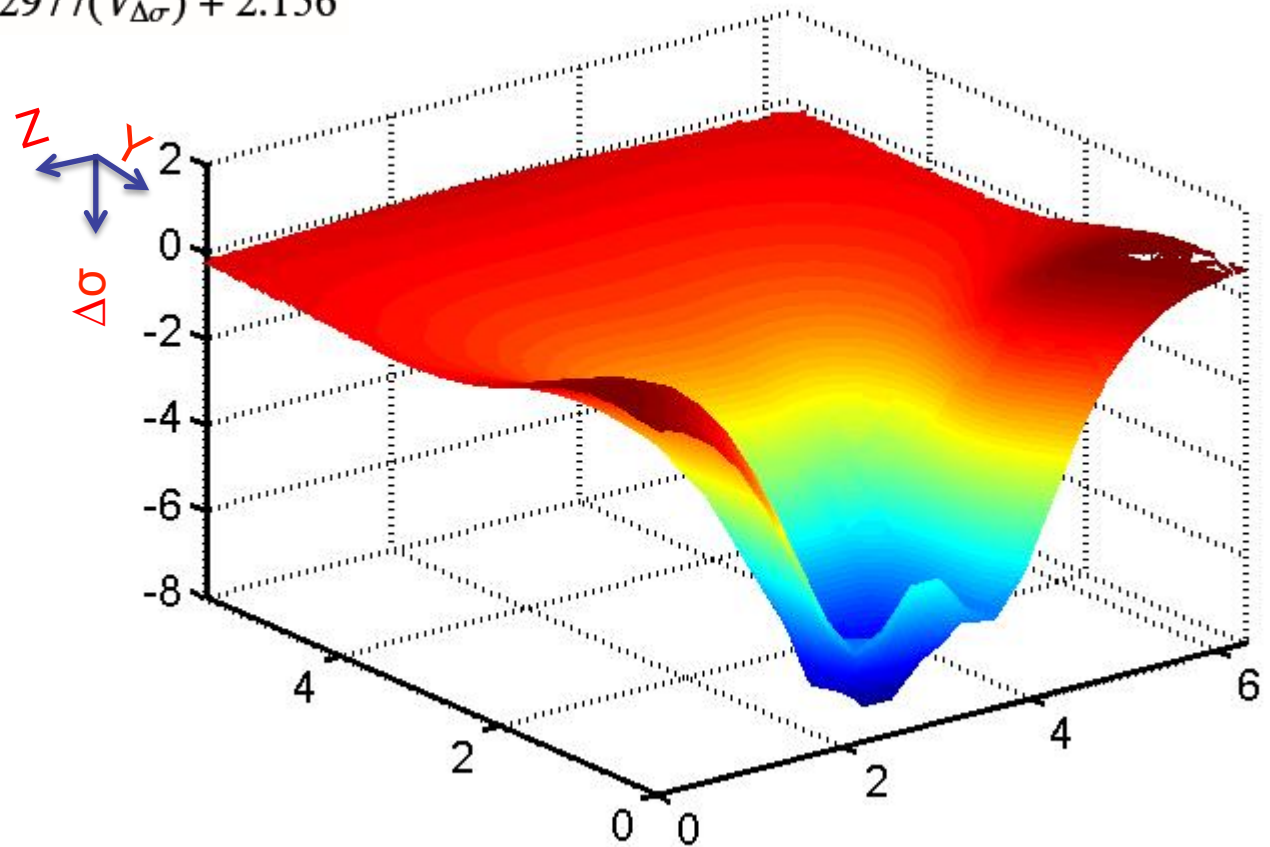
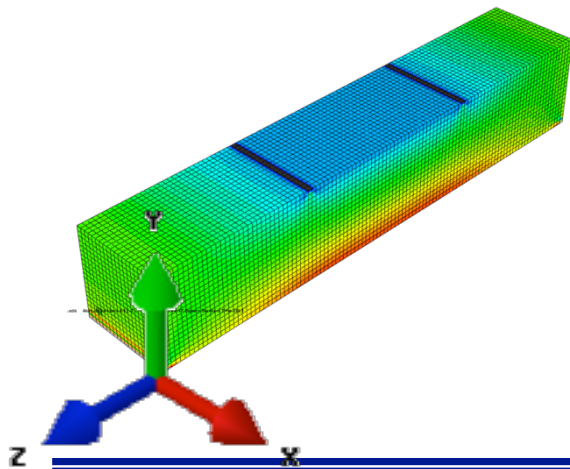
- Relationships can be used to determine the internal defect intensity.

Surface Strain Change and Damage

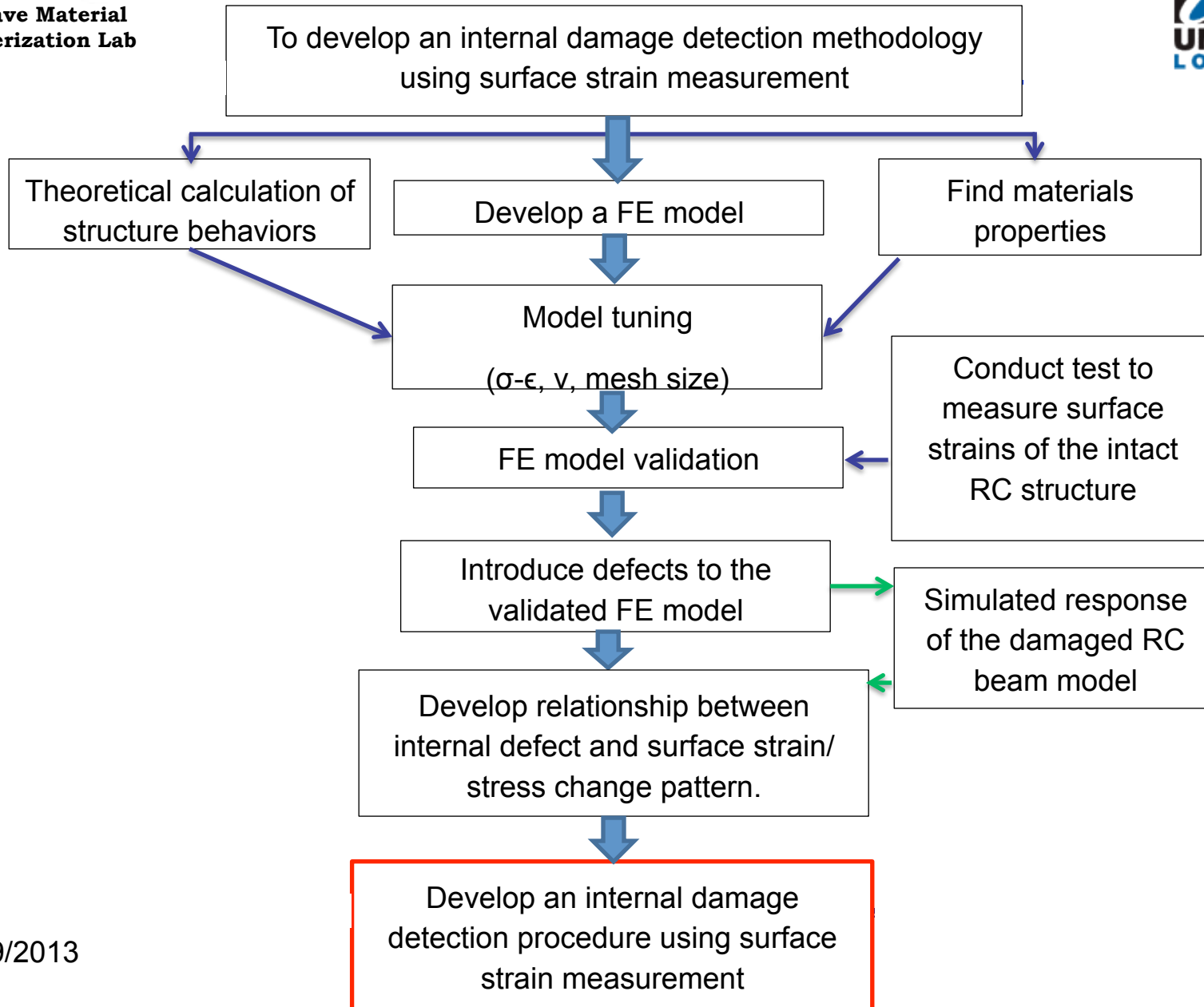
- Relationships among $A_{\Delta\sigma}$ and $V_{\Delta\sigma}$ of Type I-I damage

$$A_{\Delta\sigma} = -0.002891(V_{\Delta\sigma})^2 + 0.2977(V_{\Delta\sigma}) + 2.156$$

- This relationship can be used to find volume loss in rebar using the volume of surface stress change.

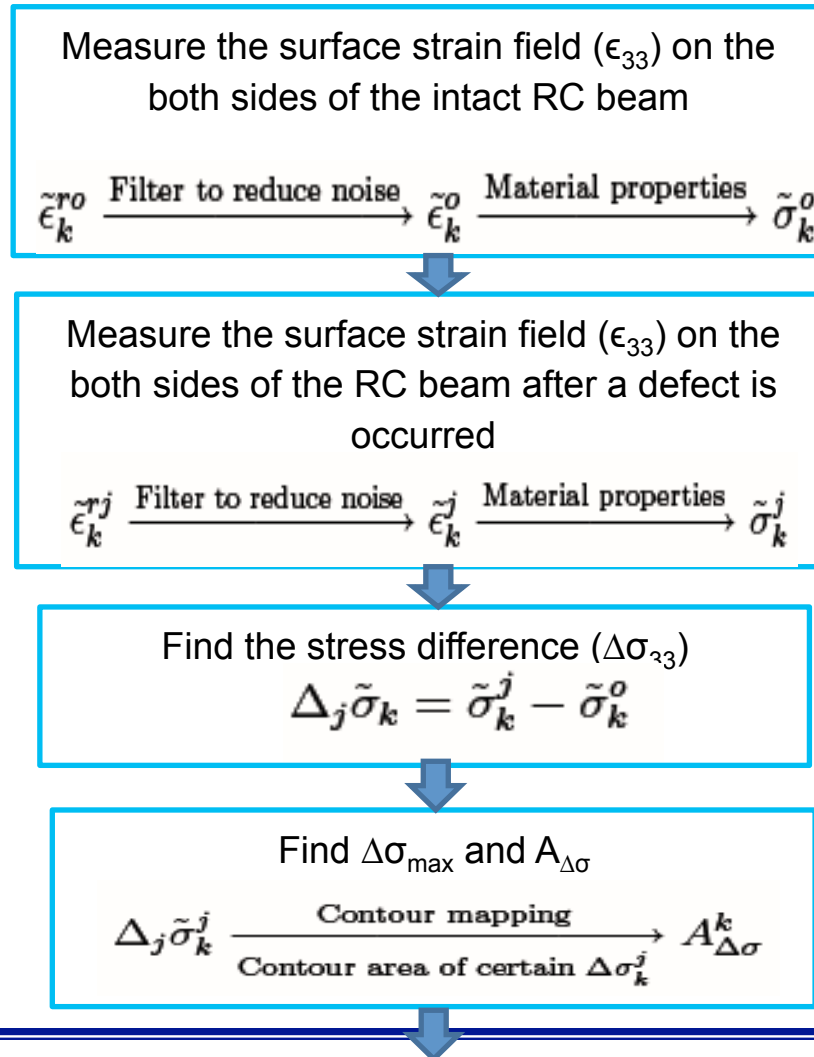


Research Roadmap

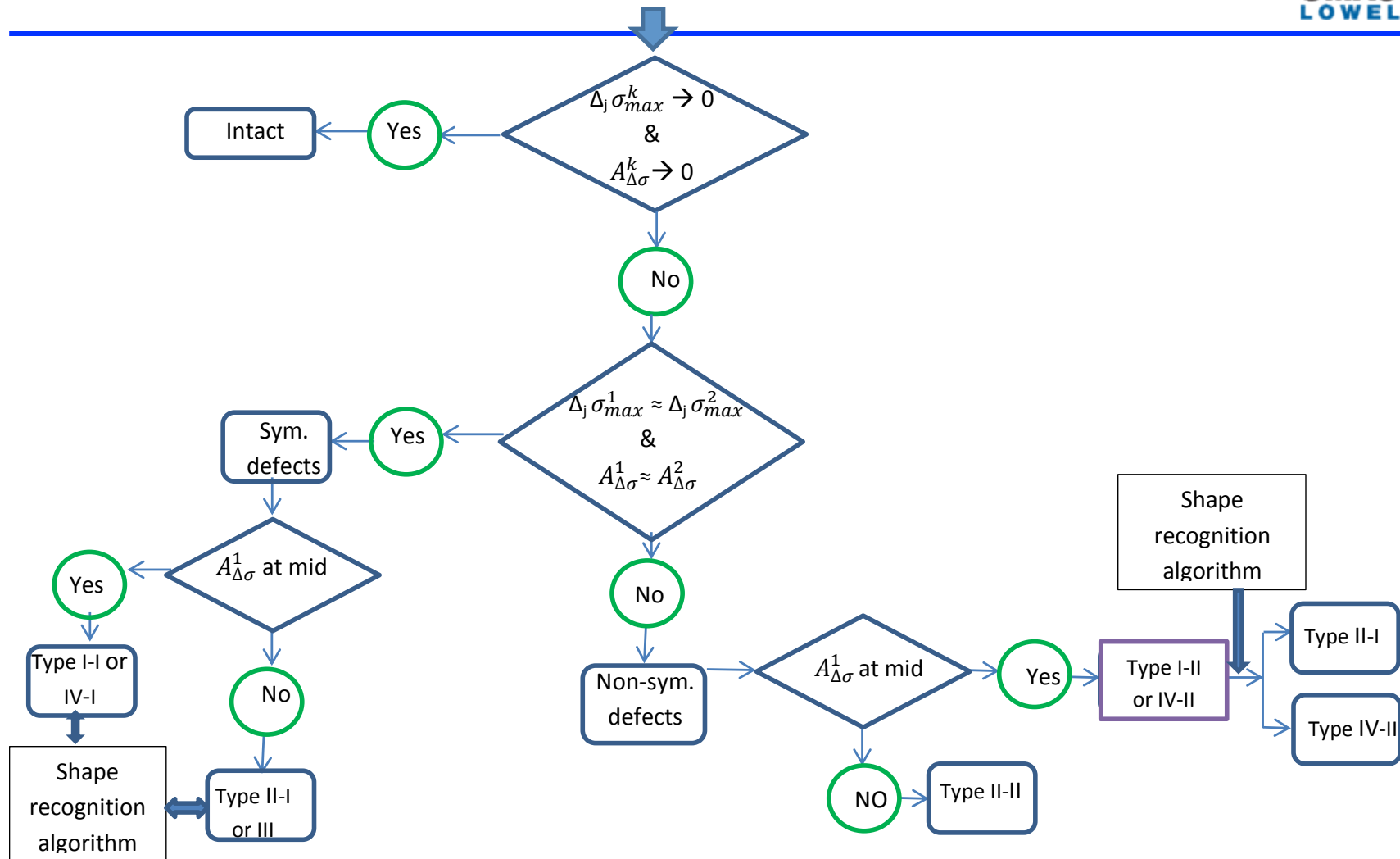


Proposed Damage Detection Procedure

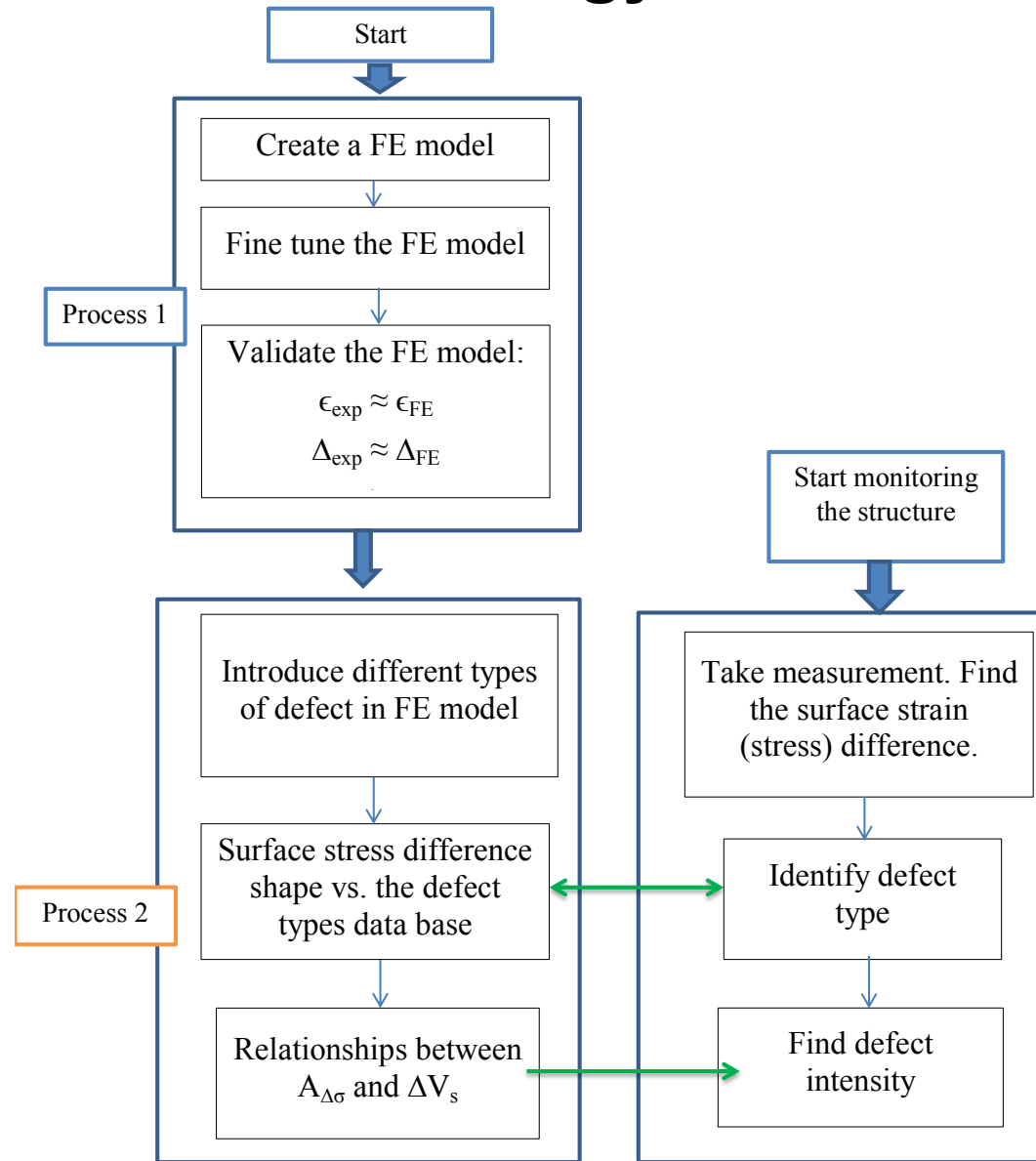
- This damage detection procedure can help experimental sensing systems (e.g., DIC, FOS) used for the subsurface damage detection of RC structures by improving the data interpretation algorithm.
- With this methodology, damage detection procedures for other types of defect (e.g., concrete deterioration, bond slippage between concrete and rebar) can be developed.



Proposed Damage Detection Procedure



Structural Health Monitoring Strategy



Conclusions

- Surface strain of a RC beam can be simulated using FE package ABAQUS®.
- FOS provides consistent measurements of surface strain during four point bending tests.
- Simulated RC beam model response revealed that surface stress/strain field of the RC beam changes due to internal defect.
- Defect introduced in the rebar embedded in a RC beam model can be accurately located using surface stress difference.
- Relationships developed between surface stress-field change and internal defect intensity for four damage scenarios can be used to predict defect intensity.
- Nonsymmetrical damages yield more contour area of stress change than the symmetric damages (in Type I, Type II, and Type IV).
- Maximum stress changes both in symmetric and nonsymmetrical damages are quite identical (1~5%).

Contributions

- A damage detection procedure and methodology are proposed to identify internal defect using surface strain measurements.
- Relationships established between internal defect intensity and surface stress difference ($A_{\Delta\sigma}$ and $\Delta\sigma_{\max}$) can be used to predict artificial internal defect intensity.
- Applied FE modeling technique to simulate artificial internal defect for modeling corrosion in RC structures.

Future Work

- Conduct experiment to confirm the surface strain change pattern.
- Develop a pattern recognition algorithm to recognize the pattern from the experimental works and FE simulations.
- Introduce more defect types (e.g., honey comb in concrete and intolerable slippage between concrete and rebars).

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- Thank you to Professor Tzu-Yang Yu for being my advisor
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Thank you!
Questions?

- Assumptions:
 1. Applicable for given geometric configurations and material properties
 2. Singly reinforced beam (no shear reinforcement)
 3. Lost rebar volume is filled up by concrete
 4. Loading level → elastic
 5. No cracking in the section of the beam